

$$\begin{aligned}
& k_0 \eta_2(t) + k_0 (\eta_2(t) - \eta_{P2}(t)) - \\
& \frac{1}{2} m_0 \left(2 (\cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \alpha'(t) + \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t))) \right. \\
& \quad \left(\cos(\theta(t)) R'(t) + \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t) - R(t) \sin(\theta(t)) \theta'(t) + \right. \\
& \quad \left. \left. \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t)) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \eta_2'(t) \right) \right) - \\
& \quad 2 \cos(\alpha(t)) \alpha'(t) \left(-\cos(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t) - \sin(\alpha(t)) \eta_2'(t) \right) + \\
& \quad 2 (\sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \alpha'(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t))) \\
& \quad \left(\sin(\theta(t)) R'(t) + \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t) + \cos(\theta(t)) R(t) \theta'(t) - \right. \\
& \quad \left. \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t)) - \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \eta_2'(t) \right) \Bigg) - \\
& \frac{1}{2} M_{P2} \left(2 (\cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \alpha'(t) + \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t))) \right. \\
& \quad (\cos(\theta(t)) R'(t) + \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t) - \\
& \quad R(t) \sin(\theta(t)) \theta'(t) + \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t)) - \\
& \quad \left. \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\eta_2'(t) + \eta_{P2}'(t))) \right) - \\
& \quad 2 \cos(\alpha(t)) \alpha'(t) (-\cos(\alpha(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t) - \sin(\alpha(t)) (\eta_2'(t) + \eta_{P2}'(t))) + \\
& \quad 2 (\sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \alpha'(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t))) \\
& \quad (\sin(\theta(t)) R'(t) + \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t) + \\
& \quad \cos(\theta(t)) R(t) \theta'(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t)) - \\
& \quad \left. \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\eta_2'(t) + \eta_{P2}'(t))) \right) + \\
& \frac{1}{2} m_0 \left(2 \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \alpha'(t) \left(\cos(\theta(t)) R'(t) + \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t) - \right. \right. \\
& \quad R(t) \sin(\theta(t)) \theta'(t) + \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t)) - \\
& \quad \left. \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \eta_2'(t) \right) + 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) \\
& \quad \left(\cos(\theta(t)) R'(t) + \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t) - R(t) \sin(\theta(t)) \theta'(t) + \right.
\end{aligned}$$

$$\begin{aligned}
& \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t)) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \eta_2'(t) \Big) - \\
& 2 \cos(\alpha(t)) \alpha'(t) \left(-\cos(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t) - \sin(\alpha(t)) \eta_2'(t) \right) + \\
& 2 \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \alpha'(t) \left(\sin(\theta(t)) R'(t) + \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t) + \right. \\
& \left. \cos(\theta(t)) R(t) \theta'(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t)) - \right. \\
& \left. \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \eta_2'(t) \right) - 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) \\
& \left(\sin(\theta(t)) R'(t) + \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t) + \cos(\theta(t)) R(t) \theta'(t) - \right. \\
& \left. \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t)) - \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \eta_2'(t) \right) - \\
& 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \left(\cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t)^2 - 2 \sin(\alpha(t)) \right. \\
& \left. \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t)) \alpha'(t) + 2 \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \eta_2'(t) \right. \\
& \left. \alpha'(t) - \cos(\theta(t)) R(t) \theta'(t)^2 + \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t))^2 - \right. \\
& \left. 2 \sin(\theta(t)) R'(t) \theta'(t) + 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) \eta_2'(t) + \right. \\
& \left. \cos(\theta(t)) R''(t) + \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha''(t) - R(t) \sin(\theta(t)) \theta''(t) + \right. \\
& \left. \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta''(t) + \psi''(t)) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \eta_2''(t) \right) - \\
& 2 \sin(\alpha(t)) \left(\sin(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t)^2 - 2 \cos(\alpha(t)) \eta_2'(t) \alpha'(t) - \right. \\
& \left. \cos(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha''(t) - \sin(\alpha(t)) \eta_2''(t) \right) - \\
& 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha'(t)^2 + 2 \cos(\theta(t) + \psi(t)) \right. \\
& \left. \sin(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t)) \alpha'(t) + 2 \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \eta_2'(t) \alpha'(t) - \right.
\end{aligned}$$

$$\begin{aligned}
& R(t) \sin(\theta(t)) \theta'(t)^2 + \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta'(t) + \psi'(t))^2 + \\
& 2 \cos(\theta(t)) R'(t) \theta'(t) - 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) \eta_2'(t) + \sin(\theta(t)) R''(t) + \\
& \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \alpha''(t) + \cos(\theta(t)) R(t) \theta''(t) - \cos(\alpha(t)) \\
& \cos(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) (\theta''(t) + \psi''(t)) - \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \eta_2''(t) \Big) + \\
& \frac{1}{2} M_{P2} \Big(2 \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \alpha'(t) (\cos(\theta(t)) R'(t) + \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \\
& (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t) - R(t) \sin(\theta(t)) \theta'(t) + \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \\
& (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t)) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\eta_2'(t) + \eta_{P2}'(t)) \Big) + \\
& 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) (\cos(\theta(t)) R'(t) + \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \\
& (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t) - R(t) \sin(\theta(t)) \theta'(t) + \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \\
& (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t)) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\eta_2'(t) + \eta_{P2}'(t)) \Big) - \\
& 2 \cos(\alpha(t)) \alpha'(t) (-\cos(\alpha(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t) - \sin(\alpha(t)) (\eta_2'(t) + \eta_{P2}'(t))) + \\
& 2 \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \alpha'(t) \\
& (\sin(\theta(t)) R'(t) + \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t) + \\
& \cos(\theta(t)) R(t) \theta'(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t)) - \\
& \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\eta_2'(t) + \eta_{P2}'(t)) \Big) - 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \\
& (\theta'(t) + \psi'(t)) (\sin(\theta(t)) R'(t) + \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t) + \\
& \cos(\theta(t)) R(t) \theta'(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t)) - \\
& \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\eta_2'(t) + \eta_{P2}'(t)) \Big) - \\
& 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \Big(\cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t)^2 - \\
& 2 \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t)) \alpha'(t) + \\
& 2 \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) (\eta_2'(t) + \eta_{P2}'(t)) \alpha'(t) - \cos(\theta(t)) R(t) \theta'(t)^2 + \\
& \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t))^2 - 2 \sin(\theta(t)) R'(t) \theta'(t) + \\
& 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) (\eta_2'(t) + \eta_{P2}'(t)) + \cos(\theta(t)) R''(t) + \\
& \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha''(t) - R(t) \sin(\theta(t)) \theta''(t) + \\
& \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta''(t) + \psi''(t)) - \\
& \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\eta_2''(t) + \eta_{P2}''(t)) \Big) - \\
& 2 \sin(\alpha(t)) \Big(\sin(\alpha(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t)^2 - 2 \cos(\alpha(t)) (\eta_2'(t) + \eta_{P2}'(t)) \alpha'(t) - \\
& \cos(\alpha(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha''(t) - \sin(\alpha(t)) (\eta_2''(t) + \eta_{P2}''(t)) \Big) - \\
& 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \Big(\cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha'(t)^2 +
\end{aligned}$$

$$\begin{aligned}
& 2 \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t)) \alpha'(t) + \\
& 2 \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) (\eta_2'(t) + \eta_{P2}'(t)) \alpha'(t) - R(t) \sin(\theta(t)) \theta'(t)^2 + \\
& \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta'(t) + \psi'(t))^2 + 2 \cos(\theta(t)) R'(t) \theta'(t) - \\
& 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) (\eta_2'(t) + \eta_{P2}'(t)) + \sin(\theta(t)) R''(t) + \\
& \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \alpha''(t) + \cos(\theta(t)) R(t) \theta''(t) - \\
& \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) (\theta''(t) + \psi''(t)) - \\
& \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\eta_2''(t) + \eta_{P2}''(t)) \Big) \Big) + \\
& \left(\mu m_0 \left(2 \left(\frac{L_0}{2} + \eta_2(t) \right) \sin^2(\alpha(t)) - 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \right. \right. \\
& \quad \left. \left(\cos(\theta(t)) R(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \right) \right) - \\
& \quad 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(R(t) \sin(\theta(t)) - \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \right) \Big) \Big) / \\
& \left(2 \left(\sin^2(\alpha(t)) \left(\frac{L_0}{2} + \eta_2(t) \right)^2 + \left(\cos(\theta(t)) R(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \right)^2 + \right. \right. \\
& \quad \left. \left(R(t) \sin(\theta(t)) - \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \left(\frac{L_0}{2} + \eta_2(t) \right) \right)^2 \right)^{3/2} \Big) + \\
& \left(\mu M_{P2} \left(2 (L_0 + \eta_2(t) + \eta_{P2}(t)) \sin^2(\alpha(t)) - 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \right. \right. \\
& \quad \left(\cos(\theta(t)) R(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \right) - \\
& \quad 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (R(t) \sin(\theta(t)) - \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t))) \Big) \Big) / \\
& \left(2 \left(\sin^2(\alpha(t)) (L_0 + \eta_2(t) + \eta_{P2}(t))^2 + \right. \right. \\
& \quad \left(\cos(\theta(t)) R(t) - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \right)^2 + \left(R(t) \sin(\theta(t)) - \right. \\
& \quad \left. \left. \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_2(t) + \eta_{P2}(t)) \right)^2 \right)^{3/2} \Big) = c_0 (\dot{\eta}_{P2} - \dot{\eta}_2) - c_0 \dot{\eta}_2
\end{aligned}$$