

$$\begin{aligned}
& k_0 (\eta_{P1}(t) - \eta_1(t)) - \\
& \frac{1}{2} M_{P1} \left( 2 \left( -\cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \alpha'(t) - \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) \right) (\cos(\theta(t)) R'(t) - \right. \\
& \quad \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t) - \\
& \quad R(t) \sin(\theta(t)) \theta'(t) - \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \\
& \quad (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta'(t) + \psi'(t)) + \\
& \quad \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t))) + \\
& \quad 2 \cos(\alpha(t)) \alpha'(t) (\cos(\alpha(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t) + \\
& \quad \sin(\alpha(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t))) + \\
& \quad 2 (\cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) - \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \alpha'(t)) \\
& \quad (\sin(\theta(t)) R'(t) - \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \\
& \quad \alpha'(t) + \cos(\theta(t)) R(t) \theta'(t) + \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \\
& \quad (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta'(t) + \psi'(t)) + \\
& \quad \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t))) \Big) + \\
& \frac{1}{2} M_{P1} \left( -2 \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \alpha'(t) (\cos(\theta(t)) R'(t) - \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \right. \\
& \quad (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t) - R(t) \sin(\theta(t)) \theta'(t) - \cos(\alpha(t)) \\
& \quad \sin(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta'(t) + \psi'(t)) + \\
& \quad \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t))) - \\
& \quad 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) (\cos(\theta(t)) R'(t) - \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) \\
& \quad (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t) - R(t) \sin(\theta(t)) \theta'(t) - \cos(\alpha(t)) \\
& \quad \sin(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta'(t) + \psi'(t)) + \\
& \quad \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t))) + \\
& \quad 2 \cos(\alpha(t)) \alpha'(t) (\cos(\alpha(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t) + \\
& \quad \sin(\alpha(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t))) - \\
& \quad 2 \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \alpha'(t) (\sin(\theta(t)) R'(t) - \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \\
& \quad (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t) + \cos(\theta(t)) R(t) \theta'(t) + \cos(\alpha(t)) \\
& \quad \cos(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta'(t) + \psi'(t)) + \\
& \quad \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t))) + \\
& \quad 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) (\sin(\theta(t)) R'(t) - \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \\
& \quad (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t) + \cos(\theta(t)) R(t) \theta'(t) + \cos(\alpha(t)) \\
& \quad \cos(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta'(t) + \psi'(t)) + \\
& \quad \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t))) + \\
& \quad 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \Big( -\cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \\
& \quad (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t)^2 + 2 \sin(\alpha(t)) \sin(\theta(t) + \psi(t))
\end{aligned}$$

$$\begin{aligned}
& (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta'(t) + \psi'(t)) \alpha'(t) - \\
& 2 \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t)) \alpha'(t) - \\
& \cos(\theta(t)) R(t) \theta'(t)^2 - \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \\
& (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta'(t) + \psi'(t))^2 - \\
& 2 \sin(\theta(t)) R'(t) \theta'(t) - 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) \\
& (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t)) + \cos(\theta(t)) R''(t) - \\
& \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha''(t) - \\
& R(t) \sin(\theta(t)) \theta''(t) - \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \\
& (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta''(t) + \psi''(t)) + \\
& \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\eta_1''(t) + \eta_2''(t) + \eta_3''(t) + \eta_4''(t) + \eta_5''(t) + \eta_{P1}''(t)) \Big) + \\
& 2 \sin(\alpha(t)) \Big( -\sin(\alpha(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t)^2 + \\
& 2 \cos(\alpha(t)) (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t)) \alpha'(t) + \\
& \cos(\alpha(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha''(t) + \sin(\alpha(t)) \\
& (\eta_1''(t) + \eta_2''(t) + \eta_3''(t) + \eta_4''(t) + \eta_5''(t) + \eta_{P1}''(t)) \Big) + 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \\
& \Big( -\cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha'(t)^2 - \\
& 2 \cos(\theta(t) + \psi(t)) \sin(\alpha(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \\
& (\theta'(t) + \psi'(t)) \alpha'(t) - 2 \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) \\
& (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t)) \alpha'(t) - R(t) \sin(\theta(t)) \theta'(t)^2 - \\
& \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \\
& (\theta'(t) + \psi'(t))^2 + 2 \cos(\theta(t)) R'(t) \theta'(t) + 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\theta'(t) + \psi'(t)) \\
& (\eta_1'(t) + \eta_2'(t) + \eta_3'(t) + \eta_4'(t) + \eta_5'(t) + \eta_{P1}'(t)) + \sin(\theta(t)) R''(t) - \\
& \sin(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \alpha''(t) + \\
& \cos(\theta(t)) R(t) \theta''(t) + \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) \\
& (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) (\theta''(t) + \psi''(t)) + \\
& \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (\eta_1''(t) + \eta_2''(t) + \eta_3''(t) + \eta_4''(t) + \eta_5''(t) + \eta_{P1}''(t)) \Big) \Big) + \\
& \Big( \mu M_{P1} \Big( 2 (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)) \sin^2(\alpha(t)) + \\
& 2 \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (\cos(\theta(t)) R(t) + \\
& \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t))) + \\
& 2 \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (R(t) \sin(\theta(t)) + \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) \\
& (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t))) \Big) \Big) \Big) / \\
& \Big( 2 \Big( \sin^2(\alpha(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t))^2 + (\cos(\theta(t)) R(t) + \\
& \cos(\alpha(t)) \cos(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) + \eta_4(t) + \eta_5(t) + \eta_{P1}(t)))^2 + \\
& (R(t) \sin(\theta(t)) + \cos(\alpha(t)) \sin(\theta(t) + \psi(t)) (L_0 + \eta_1(t) + \eta_2(t) + \eta_3(t) +
\end{aligned}$$