A Thesis

CRYSTAL-STRUCTURE STUDIES

BY X-RAY AND NEUTRON DIFFRACTION

Submitted to the University of Glasgow for the Degree of Doctor of Philosophy in the Faculty of Science

by

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MY MOTHER AND FATHER

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SUMMARY

This thesis is concerned with the study of crystal structures by x-ray and neutron diffraction techniques, and also with the application of the symbolic addition method of solving crystal structures directly from the diffraction data.

Chapter 1 contains a review of direct methods of phase determination in diffraction experiments, the first part of the chapter being concerned with the historical background of the topic and the second part with the practical details of the symbolic addition method as applied to both x-ray and neutron diffraction data.

In Chapter 2, the crystal structure analysis of the stable free radical t-butylferrocenyl nitroxide is described, and the possibility of direct Fe...N or Fe...O bonding is discussed. The relative orientations of the two cyclopentadienyl rings are compared with the orientations of the cyclopentadienyl rings in other ferrocene derivatives, and the dimensions of the nitroxide radical are compared with those published for other nitroxide radicals.

Chapter 3 describes the refinement of the structure of the 1:1 complex of hexahelicene with 4-bromo-2,5,7-trinitrofluorenone, and the resulting dimensions of the hexahelicene molecule are compared with those predicted from molecular-orbital and valencebond calculations in which a planar molecule was assumed. In Chapter 4 the determination of the crystal structure of potassium tri-hydrogen di-succinate directly from neutron diffraction data is described and discussed; the refinement of the structure of potassium tri-hydrogen di-glutarate is described, and the structures of these 'super-acid' salts are discussed, in particular the dimensions of their hydrogen bonds.

Chapter 5 describes the x-ray and neutron diffraction analyses of the crystal structure of the neutral salt a-picoline N-oxide hydrochloride monohydrate, and the structure is described in terms of the disproportionation of a neutral salt into an acid salt and a basic salt. Particular attention is paid to the discussion of the 'acid salt' part of the structure, the bichloride ion C1-H-C1⁻.

In Chapter 6, the structure analyses of the p-nitrosoaniline derivatives 9-nitrosojulolidine and N, N-diethyl p-nitrosoaniline are described, and the extent to which quinonoid-type structures contribute to the resonance hybrids of these compounds is discussed. The dimensions of their nitroso groups are discussed and compared with those of other nitroso compounds.

(The accuracy attained in the neutron analysis of the picoline salt was disappointing in relation to the chemical interest of this structure. It could have been improved had it been possible to use longer counting times.)

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CHAPTER 1

DIRECT METHODS OF PHASE DETERMINATION

IN DIFFRACTION EXPERIMENTS

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1.1, Introduction - The Phase Problem

When electromagnetic radiation falls upon matter it is scattered, and an image of the scatteringmatter may be constructed if the angular distribution of intensity, the frequency and phase of the scattered radiation is known. In mathematical terms, if the Fourier transform of an object is completely determined, the object itself is completely determined, and its form may be obtained by Fourier transformation.

When a beam of x-rays is incident upon a crystal, all the atoms in the path of the beam scatter coherently. In general, the scattered waves interfere with, and destroy one another, but in certain directions, dependent on the dimensions of the unit cell, they interfere constructively to form new wave fronts. This constructive interference is known as diffraction, and a crystal effectively behaves as a three-dimensional grating to x-rays. The resulting pattern of diffraction maxima is the Fourier transform of the unit cell contents sampled at specific points in reciprocal space - the reciprocal lattice points.

The values of the Fourier transform at these points - the structure factors - can be calculated for a structure of N atoms :

$$\mathbf{F}_{\underline{\mathbf{h}}} = \left[\mathbf{F}_{\underline{\mathbf{h}}}\right] \mathbf{e}^{i\phi} \underline{\mathbf{h}} = \sum_{j=1}^{N} \mathbf{f}_{j\underline{\mathbf{h}}} \exp(2\pi i \underline{\mathbf{h}} \cdot \underline{\mathbf{r}}_{j})$$
(1.1)

where $F_{\underline{h}}$ is the structure factor associated with the reciprocal point of Miller indices (hkl), $\phi_{\underline{h}}$ is the phase associated with $F_{\underline{h}}$, $f_{\underline{j}\underline{h}}$ is the atomic scattering factor of the jth atom, and $r_{\underline{j}} = (x_{\underline{j}}, y_{\underline{j}}, z_{\underline{j}})$ is a vector whose components are the co-ordinates of the jth atom. The intensities of the diffraction maxima are proportional to $F_{\underline{h}}^2$.

A more general form of equation (1.1) is :

$$\mathbf{F}_{\underline{\mathbf{h}}} = \int_{\mathbf{V}} \rho(\underline{\mathbf{r}}) \exp(2\pi i \underline{\mathbf{h}} \cdot \underline{\mathbf{r}}) d\mathbf{r}$$
(1.2)

where $\rho(\underline{r})$ is the electron distribution function. $\rho(\underline{r})$ may be expressed in terms of F_h by means of the Fourier inversion theorem, giving :

$$\rho(\underline{\mathbf{r}}) = \frac{1}{V-\infty} \mathbf{F}_{\underline{\mathbf{h}}} \exp(-2\pi i \underline{\mathbf{h}}_{\cdot} \underline{\mathbf{r}})$$
(1.3)

where V is the volume of the unit cell.

The electron distribution can thus be described by a Fourier series, the coefficients of which are the $F_{\underline{h}}$'s. The magnitudes of the $F_{\underline{h}}$'s can be readily derived from the intensities of the diffraction maxima, but there is no way of deriving experimentally the phases $\phi_{\underline{h}}$.

Thus the diffraction experiment does not provide sufficient data to enable the Fourier summation (1.3) to be carried out; the $\phi_{\underline{h}}$ must somehow be found before $\rho(\underline{r})$ can be calculated. This is the phase problem of crystallography.

1.2. Historical Background

In the early days of crystal-structure analysis, when trial and error methods alone were used in solving structures, it was a commonlyheld belief that a direct solution to the phase problem was impossible in principle. Equation (1.3) seems to infer that for any given set of structure amplitudes $F_{\underline{h}}$ there may be associated an arbitrary set of phases $\phi_{\underline{h}}$, each giving rise to an acceptable electron-density function $\rho(\underline{r})$. However, this argument overlooked the important restriction that $\rho(\underline{r})$ must be everywhere non-negative, and it was soon realised that a solution to the phase problem must exist, if only in principle.

The structure factor equations (1.1) form a system of simultaneous equations in which the phases $\phi_{\underline{h}}$ and the atomic positions \underline{r}_{j} are the unknowns, and the $\underline{F}_{\underline{h}}$ are known from experiment. Normally this system of equations is greatly overdetermined by the number of experimental data, so that it should be possible by algebraic means to solve for either the unknown phases $\phi_{\underline{h}}$ or the atomic positions \underline{r}_{j} . Since the equations (1.1) are not linear, simple elimination procedures cannot be used, and it would be an enormous computational task to attempt to solve such a set of equations for anything other than a trivial structure. However, the important point to emerge from the above argument was that the phases $\phi_{\underline{h}}$ (or the atomic positions \underline{r}_{j}) ought to be expressible in terms of the structure amplitudes $\underline{F}_{\underline{h}}$.

The first attempt at deriving relationships between the structure amplitudes and atomic positions, by manipulating the structure factor equations, was by Ott¹ in 1928. His results were extended by Banerjee² to a routine for finding the signs of the structure factors, but the procedure was ineffective for all but the simplest structures.

An alternative and more rewarding approach to the phase problem was adopted by A.L. Patterson^{3,4} in 1934 who investigated the properties of the

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transform of the diffracted intensity distribution. The intensity I at any point in reciprocal space is proportional to the square of the structure amplitude $(F_{\underline{h}})$ at that point. Since $F_{\underline{h}}$ is a complex quantity, we have :

$$I \prec F_{\underline{h}} \cdot F_{\underline{h}}^{*}$$
 (2.1)

where $\underline{F_{\underline{h}}}^{*}$ is the complex conjugate of $\underline{F_{\underline{h}}}^{}$. The transform of this product is, by the convolution theorem, the convolution of the transform of $\underline{F_{\underline{h}}}^{}$ (the electron density) with the transform of $\underline{F_{\underline{h}}}^{*}$ (the electron density inverted at the origin), and can be represented as a Fourier series with the intensities as Fourier coefficients :

$$P(\underline{\mathbf{r}}) = \sum I_{\underline{\mathbf{h}}} \exp(-2\pi i \underline{\mathbf{h}} \cdot \underline{\mathbf{r}})$$
(2.2)

The maxima of this function (the Patterson function) represent the interatomic vectors from which it is possible to determine the atomic positions.

Although a great many structures have been solved with the help of the Patterson function, the more complex ones with the aid of heavy atom substituents in the crystal, no general method of solution has so far resulted. The Patterson function of a structure containing only a moderate number of light atoms tends to have many overlapping peaks, and without some previous knowledge of the structure, interpretation may be very difficult. However, the relative success of the Patterson function did demonstrate that it was possible to extract phase information from a set of phaseless amplitudes, and stimulated a new search for relationships between structure factors and phases.

In 1948 Harker and Kasper⁵ derived inequality relationships between the structure factors, which depended on the positivity of the electron density. To do this, they made use of Cauchy's inequality, which may be written :

$$\left|\sum_{j=1}^{N} a_{j} b_{j}\right|^{2} \leq \left(\sum_{j=1}^{N} |a_{j}|^{2}\right) \left(\sum_{j=1}^{N} |b_{j}|^{2}\right)$$
(2.3)

where the a_j 's and b_j 's may be real or complex quantities. In dealing with inequalities, it was found convenient to define a normalised structure factor, the unitary structure factor (U) which gives the structure factor as the fraction of its maximum possible value :

$$U_{\underline{h}} = \frac{F_{\underline{h}}}{\sum_{j=1}^{N} f_{j}} = \sum_{j=1}^{N} n_{j} \exp(2\pi i \underline{h} \cdot \underline{r}_{j})$$
(2.4)

where $n_j = f_j / \sum_{j=1}^{N} f_j$

 \boldsymbol{U}_h thus has a maximum value of 1.

If \sqrt{n}_j is substituted for a_j , and $\sqrt{n}_j \exp 2\pi i \underline{h} \cdot \underline{r}$ for b, in equation (2.3) the resulting inequality is :

$$\left| \underbrace{\mathbf{U}}_{\underline{\mathbf{h}}} \right|^{2} \leq \left(\sum_{j=1}^{N} \mathbf{n}_{j} \right) \left(\sum_{j=1}^{N} \mathbf{n}_{j} \exp 2\pi \mathbf{i} \underline{\mathbf{h}} \cdot \underline{\mathbf{r}}^{2} \right)$$
(2.5)

Since $|\exp 2\pi i \underline{h} \cdot \underline{r}|^2 = 1$, equation (2.5) becomes

 $\left| \mathbf{U}_{\underline{h}} \right|^{2} \leq \left(\sum_{j=1}^{N} \mathbf{n}_{j} \right)^{2}$

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 $\left| \mathbf{U}_{h} \right|^{2} \leq 1$

or

Although this result is trivial, when Cauchy's inequality is applied to the structure factor equations for structures containing symmetry elements, more useful inequality relationships are found. When a centre is present, the unitary structure factor equation is :

$$\mathbf{U}_{\underline{\mathbf{h}}} = \sum_{j=1}^{N} n_j \cos 2\pi \underline{\mathbf{h}} \cdot \underline{\mathbf{r}}_j$$
(2.6)

and applying Cauchy's inequality we have :

$$\mathbf{U}_{\underline{\mathbf{h}}}^{2} \leq \left(\sum_{j=1}^{N} n_{j}\right) \left(\sum_{j=1}^{N} n_{j} \cos^{2} 2\pi \underline{\mathbf{h}} \cdot \underline{\mathbf{r}}_{j}\right)$$
(2.7)

or
$$U_{\underline{h}}^{2} \leq \frac{1}{2} \sum_{j=1}^{N} n_{j} \left(1 + \cos 2\pi 2 \underline{h} \cdot \underline{r}_{j} \right)$$
 (2.8)

and thus $U_{\underline{h}}^{2} \leq \frac{1}{2} \left(1 + U_{2\underline{h}}\right)$ (2.9)

This inequality can be used to show that if $U_{\underline{h}}$ and $U_{\underline{2h}}$ are both sufficiently large, $U_{\underline{2h}}$ must be positive. Other inequalities may be found for other symmetry elements, and MacGillavry⁶ published a grouptheoretical derivation of Harker-Kasper inequalities which enabled their straightforward determination for any space group.

Karle and Haurtman⁷ investigated the relations between the phases and magnitudes of a set of structure factors on a more general basis by deriving a complete set of inequalities on the basis of the non-negativity of the electron density. They showed that a necessary and sufficient condition for the electron density to be everywhere positive is :

$$\begin{array}{c|c} F_{000} & \overline{F_{\underline{h}}} & \cdots & F_{\underline{h}} \\ F_{\underline{h}_{1}} & F_{000} & \overline{F_{\underline{h}_{1}}} - \overline{\underline{h}}_{2} & \cdots & F_{\underline{h}_{1}} - \overline{\underline{h}}_{n} \\ F_{\underline{h}_{n}} & \cdots & F_{000} \end{array} \\ \end{array} \ge 0 \qquad (2.10)$$

The complete set of inequalities, which include all the Harker-Kasper inequalities, may be expressed in terms of determinants of higher and higher order, and thus of increasing complexity. Only the simpler inequalities have therefore found practical application, but with increasing structural complexity, they cease to be restrictive.

Several structures were solved using inequalities, but they contained comparatively few atoms in the unit cell, and it would be a fair comment that any structure solvable by inequalities could also be solved by some other non-direct methods of phase determination. Nonetheless, it was from Harker-Kasper inequalities that all subsequent direct methods of phase determination were evolved.

Probably the most important single advance in direct methods was achieved by Sayre⁸ who, by examining the relations between the F's of a structure containing fully resolved identical atoms and the F's of the same structure in which the atoms were replaced by squared atoms, derived equations inter-relating the structure factors. The electron density $\rho(\underline{r})$ and its square $\rho^2(\underline{r})$ may be expressed as :

$$\rho(\underline{\mathbf{r}}) = \frac{1}{V} \sum_{\mathbf{h}} F_{\underline{\mathbf{h}}} \exp(-2\pi i \underline{\mathbf{n}} \cdot \underline{\mathbf{r}})$$

$$\rho(\underline{\mathbf{r}}) = \frac{1}{V} \sum_{\mathbf{h}} F_{\underline{\mathbf{h}}} \exp(-2\pi i \underline{\mathbf{n}} \cdot \underline{\mathbf{r}})$$
(2.11)

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where $\frac{F_h}{V}$ is the hth Fourier coefficient,

$$\rho^{2}(\underline{\mathbf{r}}) = \frac{1}{V} \sum_{\underline{\mathbf{h}}} \operatorname{Exp}(-2\pi i \underline{\mathbf{h}} \cdot \underline{\mathbf{r}}) \qquad (2.12)$$

where $\frac{G_{h}}{V}$ is the hth Fourier coefficient of the squared structure.

It can be shown that the Fourier coefficients of the squared structure may be found by the self-convolution of the Fourier coefficients of the original function. Thus :

$$\frac{1}{V}G_{\underline{h}} = \sum_{\underline{k}} \frac{1}{V^2} F_{\underline{k}} F_{\underline{h}-\underline{k}}$$
(2.13)

or
$$G_{\underline{h}} = \frac{1}{V} \sum_{\underline{k}} F_{\underline{h}} - \underline{k}$$
 (2.14)

Equation (2.14) relates the Fourier coefficients of the squared structure to those of the structure itself for a structure containing identical atoms.

If the atomic scattering factor of an atom is denoted by f and that of the squared atom by g, we have :

$$\mathbf{F}_{\underline{\mathbf{h}}} = \sum_{j=1}^{N} \operatorname{fexp}(2\pi i \underline{\mathbf{h}} \cdot \underline{\mathbf{r}})$$
(2.15)

$$G_{\underline{h}} = \sum_{j=1}^{N} gexp(2\pi i \underline{h} \cdot \underline{r})$$
(2.16)

and

$$= \frac{g_{\rm F}}{f_{\rm h}}$$
(2.17)

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Thus

$$\frac{\underline{K}}{\mathbf{f}} = \frac{1}{V} \frac{\mathbf{F}}{\underline{k}} \frac{\mathbf{F}}{\underline{h}} - \underline{k}$$
(2.18)

Equation (2.18) should be valid for a structure containing equal (or nearly equal) atoms, and was used successfully by Sayre to solve in two dimensions the structure of hydroxyproline. The direct application of Sayre's equation to determine signs is nevertheless too complex, especially in three dimensions, to be generally useful.

However, Zachariasen⁹ (1952) and Cochran¹⁰ (1952) were quick to notice that if the F's involved are sufficiently large, equation (2.18) can be simplified to:

$$\mathbf{F}_{\underline{\mathbf{h}}} \sim \mathbf{F}_{\underline{\mathbf{k}}} \mathbf{F}_{\underline{\mathbf{h}}-\underline{\mathbf{k}}}$$
 (2.19)

As the magnitudes decrease in value, equation (2.19) will no longer be even approximately true, but it will still be probable that

$$\mathbf{sF}_{\mathbf{h}} = \mathbf{sF}_{\underline{k}}\mathbf{F}_{\underline{\mathbf{h}}-\underline{\mathbf{k}}}$$
(2.20)

or more generally

$$\mathbf{s}\mathbf{F}_{\underline{\mathbf{h}}} = \mathbf{s} \mathbf{F}_{\underline{\mathbf{k}}} \mathbf{F}_{\underline{\mathbf{h}}-\underline{\mathbf{k}}}$$
(2.21)

where s means 'sign of'.

Using a statistical approach, Cochran and Woolfson¹¹ derived an expression for the probability that the product $U_{\underline{k}}U_{\underline{h}-\underline{k}}$ gives a positive sign for $U_{\underline{h}}$:

 $\sigma_3 = \sum_{j=1}^{N} n_j^3$

$$P_{\pm}(\underline{\mathbf{h}},\underline{\mathbf{k}}) = \frac{1}{2} \pm \frac{1}{2} \tan \left(\frac{\sigma_{3}}{\sigma^{3}} \right) \left| \underbrace{\mathbf{U}}_{\underline{\mathbf{h}}} \underbrace{\mathbf{U}}_{\underline{\mathbf{k}}} \underbrace{\mathbf{U}}_{\underline{\mathbf{h}}} - \underline{\mathbf{k}}} \right|$$
(2.22)

where

and $\sigma = \sum_{j=1}^{N} n_j 2$

For an equal atom structure, equation (2.22) becomes

$$P_{+}(\underline{h},\underline{k}) = \frac{1}{2} + \frac{1}{2} \tanh \left| U_{\underline{h}} U_{\underline{k}} U_{\underline{h}-\underline{k}} \right| \qquad (2.23)$$

Although this simplified form of Sayre's relation $(2.20)_{j}$ used in conjunction with the above probability expression, was a significant advance in the use of sign relationships, it could not be generally used without prior knowledge of the signs of some of the F_{h} .

Karle and Hauptman¹² (1953) developed a statistical approach to the phase problem which yielded phase determining formulae in which phase information is deduced from the magnitudes of the structure factors. They noted that the probability of the sign of a structure factor being positive is one-half as long as no other intensities are known; once a set of intensities is known, the probability deviates from one-half. By a complex mathematical procedure, which involved integrating the atomic coordinates over all positions in the unit cell, they obtained a number of expressions similar in form to (2.22) for the probability that the sign of a structure factor is positive. They expressed their results in terms of the normalised structure factor defined as:

$$\mathbf{E}_{\underline{\mathbf{h}}} = \frac{\underline{\mathbf{U}}_{\underline{\mathbf{h}}}}{\overline{\mathbf{U}}^2 \cdot \frac{1}{2}} \tag{2.24}$$

The first results, which are applicable to the space group PI, may be expressed as :

$$\sum_{1} : sE_{2\underline{h}} \sim s(E_{\underline{h}}^{2}-1) \qquad (2.25)$$

$$\Sigma_2 : sE_{\underline{h}} \sim s\Sigma E_{\underline{k}} E_{\underline{h}-\underline{k}}$$
 (2.26)

$$\sum_{3} : sE_{\underline{h}} \sim s\sum_{\underline{k}} E_{\underline{k}} (E^{2}(\underline{h}+\underline{k})/2 - 1) \qquad (2.27)$$

$$\sum_{4} : sE_{\underline{h}} \sim s\sum_{\underline{k}} (E^{2}_{\underline{k}} - 1)(E^{2}_{\underline{h}-\underline{k}} - 1) \qquad (2.28)$$

If symmetry other than a centre is present then stronger signdetermining formulae result. For example in the space group P_{2_1}/c an additional Σ_1 type formula may be derived :

$$sE_{2h021} \sim s\Sigma(-1)^{h+1}(E_{hk1}^2 - 1)$$
 (2.29)

Since only the magnitudes of the E's are known initially, Σ_1 or Σ_4 must be used to initiate the phase determination. Once sufficient signs have been determined, Σ_2 , which is the same as Sayre's relationship, can be used to determine further signs. Although Karle and Hauptman used this method to solve several structures, it was not always successful, the main difficulty being the unreliability of Σ_1 and Σ_4 . The reasons for this were pointed out by Vand and Pepinsky¹⁵ (1953) and Bullough and Cruickshank¹⁴ (1954). If the signs of the E's are controlled entirely by Σ_1 , this is equivalent to computing a Fourier synthesis using $(E^2_{\underline{h}}-1)$ as coefficients essentially a sharpened Patterson map with the origin removed, and the solution, using this as a start, tends to converge on the high peaks of the Patterson map. In the same way, using Σ_4 , the solution converges on the high peaks of a map of the square of the Patterson density. In recognition of the inadequacies of Σ_1 and Σ_4 , and in the light of their own experiences with direct methods, Karle and Karle¹⁵ in 1963 introduced the symbolic addition method of phase determination. Instead of first determining a basic set of signs using relationships such as Σ_1 and Σ_4 , and then proceeding with Σ_2 using this basic set, the phase determining procedure is initiated and carried out in terms of a small properly chosen set of specified signs and unknown symbols using only the Σ_2 relationship. If x symbols are used, then in principle 2^x Fourier maps must be computed, in order to find the correct solution, although relations are usually found between the unknown symbols which reduce this number. As well as being both simple and reliable, the symbolic addition method has the advantage of being easily carried out by hand, and is now probably the most widely used method of direct phase determination.

So far, only the case of the centrosymmetric space groups has been discussed; in its more general form,¹² Karle and Hauptman's theory can be extended to deal with non-centrosymmetric space-groups. Phase determination in this case is initiated using a formula similar to Σ_2 . If one has three structure factors of indices <u>h</u>, <u>k</u>, and <u>h-k</u>, the expected value of the phase ϕ_h is given by :

 $\phi_{\underline{\mathbf{h}}} \approx \langle \phi_{\underline{\mathbf{k}}} + \phi_{\underline{\mathbf{h}}-\underline{\mathbf{k}}} \rangle \mathbf{k}_{\mathsf{r}}$ (2.3C)

Approximate phases for additional E's can then be calculated using the tangent formula :

$$\tan \phi = \frac{\sum_{\underline{k}} E_{\underline{k}} E_{\underline{h}-\underline{k}} \sin(\phi_{\underline{k}} + \phi_{\underline{h}-\underline{k}})}{\sum_{\underline{k}} E_{\underline{k}} E_{\underline{h}-\underline{k}} \cos(\phi_{\underline{k}} + \phi_{\underline{h}-\underline{k}})}$$
(2.31)

1.3. <u>The Symbolic Addition Method of Direct Phase Determination</u> for Centrosymmetric Crystal Structures

(a) Preparation of normalised structure factors

The observed structure factors (F_{obs}) are first put on an absolute scale and corrected for thermal motion using either a Wilson plot or K-curve.

Wilson¹⁶ pointed out that for absolute intensities

$$\langle I_h \rangle = \sum_{j} f_j^2 = \sigma$$
 (3.1)

and that the observed intensities, I_{hobs} will differ from the I_h by a scale factor k, independent of θ , and a temperature factor. Thus, if we assume a temperature factor of the form $\exp(-Bs^2)$, were $s = \sin\theta/\lambda$, we have :

$$I_{\underline{h}obs} = kI_{\underline{h}}exp(-Bs^2)$$

The reflections can be divided into groups covering different ranges of s, and within each group the ratios :

$$\frac{\Sigma\sigma}{I \text{ hobs}} \quad \text{or} \quad \frac{\Sigma\sigma}{2} = r \quad (3.2)$$

are computed. A plot of log(r) vs. s^2 at the average value of s^2 within each group should thus give a straight line of slope B and inter-

cept - log k. This is known as a Wilson plot.

Alternatively, if (3.2) is plotted directly as a function of s at the average value of s within each group, without assuming a form for the temperature factor, the resulting curve will have an intercept 1/k when s = 0, and the shape of the curve will give the statistical temperature correction, which need not be Gaussian; this is the k-curve.

Having put the observed structure factors on an absolute scale and corrected them for vibrational motion using either of the above methods, the normalised structure factors are calculated according to equation :

$$E_{\underline{h}} = \frac{F_{\underline{h}}^{2}}{\epsilon \sum_{j=1}^{N} f_{j}^{2}}$$

where $F_{\underline{h}}$ is the corrected structure factor magnitude, f_{j} is the jth atomic scattering factor for the jth atom in a unit cell containing N atoms, and ε is a number which corrects for space group extinctions.

The normalised data are then separated into eight subgroups according to the parity of their Miller indices, and listed in order of decreasing |E|. Those E's above a certain arbitrary value, usually $|E| \ge 1.5$, are then used to generate all the possible 'triples' <u>h</u>, <u>k</u>, <u>h-k</u> for use with Σ_2 . For each triple, the probability that

$$\mathbf{s}(\underline{\mathbf{h}}) \cdot \mathbf{s}(\underline{\mathbf{k}}) \cdot \mathbf{s}(\underline{\mathbf{h}} - \underline{\mathbf{k}}) = +1 \tag{3.3}$$

is evaluated, assuming an equal, or nearly equal atom structure, using a formula derived from equation (2.22)

$$P_{+} = \frac{1}{2} + \frac{1}{2} \tanh \frac{1}{\sqrt{N}} \left| E_{\underline{h}} \cdot E_{\underline{k}} \cdot E_{\underline{h}-\underline{k}} \right|$$
(3.4)

(b) <u>Specification of an origin</u>

The first step in the phase determining procedure is to define an origin, since the values of the phases depend, in general, not only on the structure, but also on the choice of origin. For the centrosymmetric space groups, the permissible origins are the eight centres of symmetry in the primitive unit cell. Usually the eight centres are not equivalent, since different centres may be situated differently with respect to the various symmetry elements. As a result, phases may be divided into two classes: those which change sign with a change in origin - structure seminvariants, and those which depend solely on the structure - structure invarients.

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The centrosymmetric space groups may have one, two, four or eight classes of equivalent origins and it is then necessary to assign the values of three, two, one or zero appropriate phases, respectively, in order to specify the origin.

The theory of structure seminvariants has been worked out in detail for all the space groups; tables 17,18,19,20 are given which divide the space groups into types according to the nature of their equivalent sets of permissible origins. Within each type of space group, the invarient and seminvarient phases are listed, as well as the number of phases which require to be assigned in order to define an origin. For example, in the primitive centrosymmetric space groups of the triclinic, monoclinic and orthorhombic classes (Type 1P), three phases require to be assigned in order to define an origin. Phases of reflections whose indices are all even (eee) are structure invarients in this type of space group and thus cannot be used to define an origin. Likewise, any linear combination of three phases whose indices add up to (eee) is also structure invariant; such phases are linearly dependent. Only combinations of three phases which are linearly independent can thus be used to define an origin. In making the phase assignments, the largest suitable $|E_{\underline{h}}|$ are used, the choice being partly determined by the extent to which a particular <u>h</u> enters into the Σ_{2} triples.

(c) Determination of phases

Having specified an origin, one unknown symbol is then assigned to a suitable large $|E_{\underline{h}}|$ which is involved in many Σ_2 relationships. Equation (3.3) is then used to define as many signs of the largest $|E_{\underline{h}}|$ as possible, in terms of both the specified ones and others that have been newly determined. Additional symbols are assigned when required to other large $|E_{\underline{h}}|$ which enter into a large number of Σ_2 relationships. It is possible to proceed in this manner until the phases of all or most of the largest $|E_{\underline{h}}|$ are known in terms of the specified signs and unknown symbols.

As the phase determination proceeds, and relationships involving smaller $|E_{h}|$ are employed, the probabilities determined from (3.4) will

decrease; that is, the relationships will become less reliable, and Karle and hauptman recommend that a relationship should be rejected if $P_+ < 0.97$. However, relationships with lower probabilities can usually be employed in the latter stages of phase determination, if necessary, in an attempt to gain more signs.

Usually no more than three or four unknown symbols are required during a determination, which means that, in theory, there will be 2^3 or 2^4 possible solutions respectively. Fortunately relationships between the unknown symbols often arise during the phase determination, in favourable circumstances providing a unique solution, and in less favourable circumstances leaving only two or four possible solutions. Other criteria, such as the relative number of positive and negative phases, also help in deciding which solutions are likely to be correct.

(d) Calculation of E-maps

Once one or more possible solutions have been determined, their validity is tested by calculating Fourier syntheses. It has been found more useful to calculate syntheses in which the coefficients are E's rather than F's. This is because a large number of the phased E's are derived from fairly high-order reflections which, although they have large |E|'s, have small values for |F| which tend to be swamped in a Fourier synthesis by a few strong low-order F's.

'E-maps' are effectively sharpened Fourier maps, and nearly always contain too many peaks. Choosing a chemically sensible set of peaks is

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usually fairly straightforward for most structures, but structures containing highly symmetrical features, such as several six-membered rings, sometimes give rise to E-maps which have several possible interpretations.

1.4. The Direct Determination of Phases from Neutron Data

Since neutron diffraction data are normally phased initially using the previously determined x-ray structure, a means of determining phases directly from a set of neutron structure amplitudes would be useful when x-ray data are not available, or when a heavy-atom structure determined by x-rays contains poorly resolved light atoms.

It was thought initially²¹ that the methods applicable to x-ray data, in particular the symbolic addition method, are not directly applicable to neutron data, since certain atoms, notably hydrogen, have negative scattering factors for neutrons; x-ray scattering factors are always positive.

In deriving the sign relationship (2.20) from Sayre's equation (2.18) it was shown that the phases and magnitudes of the original and squared structures are the same for the largest normalised structure amplitudes. In the case of neutron diffraction, where some atoms may be scattering with negative scattering factors, the phases and magnitudes of the normalised structure factors for the squared structure may be different from those of the original structure, making the use of equation (2.20) invalid.

Karle²¹ suggested that if the structure amplitudes expected from the squared structure could be calculated from the observed amplitudes,

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the conventional symbolic addition procedure could then be applied, since all the atoms would have positive scattering factors as in the case of x-ray diffraction. This would lead to the squared structure from which the original structure could be derived; the structure of glycolic acid has been solved directly from neutron data by Ellison and Levy²² using this 'squared structure' method.

However, it is likely that the glycolic acid structure could, in fact, have been solved by the conventional symbolic addition method. То see why this is so, let us look more closely at the effect of negative scattering hydrogen nuclei on the structure factors obtained from a typical organic crystal by neutron diffraction. The nuclear scattering lengths (b) of carbon, oxygen and hydrogen are 0.661, 0.577 and -0.378 $\times 10^{-12}$ cms. respectively. Their respective scattering powers are thus in the ratio of $0.661^2:0.577^2:(0.378)^2$ or 0.44:0.34:0.14 - roughly 3:2:1 compared with 36:64:1 for x-rays. It can be seen, therefore, that the 'heavy elements' carbon and oxygen are still the dominant scatterers, though to the extent of an order of magnitude less than for x-rays. The differences in the neutron structure factors of an organic structure containing a moderate proportion of negatively scattering hydrogens and the same structure in which the hydrogens scatter positively can thus be predicted as :

(a) proportionately large differences in amplitude among a number of the weaker F's; many may also have different signs.

(b) proportionately small differences in amplitude among the

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largest F's, and no difference in sign.

Thus, although the phases of some of the structure factors for the squaredstructure may differ from those of the original structure, the important point is that, as long as there is only a moderate proportion of hydrogens in the structure, the phases of largest structure factors will be the same in the original and squared structures.

Also, since the nuclear scattering length, \overline{b} , does not change with increasing Bragg angle θ , it is generally the case with neutron data that large E's correspond to large F's, so that the phases of the largest E's will be the same in the original and squared structures, and it should therefore be permissible to proceed with phase determination using the conventional symbolic addition method. It has been suggested¹⁸ that the symbolic addition method may be used with neutron data when the scattering due to hydrogen is less than $\frac{1}{2}$ of the total scattering :

$$\sum_{H} b_{H}^{2} / \sum_{all \ atoms} b_{j}^{2} < 1_{3}$$

That the symbolic addition method can be successfully applied to neutron data is demonstrated in Chapter 4 where the determinations of the structures of potassium trihydrogen disuccinate and potassium trihydrogen diglutarate are described; the proportion of negative scattering power in these structures is 20% and 22% respectively. The first noncentrosymmetric structure to be solved directly from neutron data - L-proline monohydrate - has been reported¹⁸ by Verbist et al, and they conclude that

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'direct methods can probably be applied to neutron diffraction data for almost any crystal to which they are applicable to x-ray diffration data.

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CHAPTER 2

THE CRYSTAL AND MOLECULAR STRUCTURE

OF t-BUTYLFERROCENYL NITROXIDE

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2.1. Introduction

The first stable organic nitroxide radical, porphyrexide (I), was isolated and characterised by Piloty and Schwerin¹ in 1901; during the years 1912-22 Wieland² prepared a number of relatively stable diaryl nitroxides of type (II), with R_1 and R_2 = aryl, and in 1959 Lebedev and Kazarnovski³ succeeded in isolating the first completely aliphatic nitroxide radical (III).



This was followed shortly afterwards by Hoffmann's synthesis⁴ of di-t-butyl nitroxide. The rapid development of e.s.r. spectroscopy in recent years has stimulated a renewed interest in nitroxide radicals, and a large number have been synthesised and examined. t-Butylferrocenyl nitroxide (IV), believed to be the first stable, neutral ferrocenyl radical to be isolated,⁵ is of particular interest. Its e.s.r. spectrum (Figure 2.1) has some unusual features - an a_N value of 11.75 G which is similar to that found in aryl-t-butyl nitroxides (about 12.0 G) but a g-value of 2.0149 $\stackrel{+}{=}$ 0.0004 which is much larger than the normal value for aryl-t-butyl nitroxides (about 2.006). The smaller coupling (0.8G) in the spectrum, which almost certainly arises from the 2- and 5-ring protons, is less than half that of the ortho-protons in aryl-t-butyl nitroxides (a_{0-H} ca. 2.0 G). These results indicate that the unpaired electron is extensively delocalised and that there is considerable interaction with the iron atom. This could occur either via the metalring π -system ($IV \xrightarrow{a} IV_b \xrightarrow{} IV_c$).



Шa

IVc

and/or by direct Fe-N (or 0) bonding - direct bonding between electrondeficient carbon and iron has frequently been invoked⁶ to explain the unusual stability of a-ferrocenylcarbonium ions (V).


The structure of t-butylferrocenylnitroxide was thus determined in order to examine the possibility of direct bonding, and also to determine the bond lengths and angles of the nitroxide moiety.

2.2. Experimental

The crystals of t-butylferrocenyl nitroxide were deep-red in colour and needle-shaped, with the needle axis along the a-direction. The unitcell dimensions and space-group were determined from rotation, Weissenberg and precession photographs taken with a crystal mounted along its needle axis. Cu-K_a radiation of wavelength 1.5418 $\stackrel{0}{A}$ was used.

Crystal Data

 $C_{14}H_{18}$ NOFe, M = 272.14. Monoclinic, <u>a</u> = 5.90 (1), <u>b</u> = 15.71 (2), <u>c</u> = 14.38 (2) $\stackrel{o}{A}$, β = 109.25 (0.25)^o. <u>U</u> = 1258.2 $\stackrel{o}{A}$, <u>D</u>_m = 1.42, <u>z</u> = 4, <u>D</u>_c = 1.43. μ (Cu-K) = 96.57 cm⁻¹. Space group P₂₁/c (No. 14).

Data Collection

Intensities were estimated visually from equi-inclination Weissenberg

photographs (using Cu-K_a radiation) of reciprocal-lattice nets 0kl - 5kl. A crystal of dimensions 1.0 x 0.25 x 0.15 m m³ mounted along its needle axis was used, and 1,237 independent intensities were measured which were significantly above background. Lorentz and polarisation corrections were applied to the data, but no absorption corrections were applied.

2.3. Structure Determination and Refinement

The structure was solved by the heavy-atom method. The coordinates of the iron atom were determined from a three-dimensional Patterson synthesis, and the signs of the structure factors obtained from the iron contributions were used in computing an electron-density map in which all the remaining sixteen atoms in the molecule were clearly resolved. Structure factors based on all seventeen atoms gave an R value of 29.0%.

Using unit weights, three cycles of full-matrix least-squares refinement of positional and isotropic temperature factors, and batch scale factors, reduced R to 17.3%. A further four cycles of blockdiagonal refinement with anisotropic temperature factors and an overall scale factor, completed the refinement, and reduced R to 9.3%. with $R^{1}(\Sigma W \Delta^{2}/\Sigma W F_{0}^{2}) = 1.6\%$. The weighting scheme used in the final three cycles is represented by the equation :

 $W = \left\{ \left[1 - \exp(-p_1 (\sin \theta / \lambda)^2) / \left[1 + p_2 |F_c| + p_3 |F_c|^2 \right] \right\}$ The final values for the three parameters were $p_1 = 20$, $p_2 = 0.0001$, $p_3 = 0.0005$. The scattering factor curves used for Fe, C, N, and O were those from International Tables for Crystallography (1962).

The values for the atomic coordinates and vibrational parameters are given in Tables 2.1 and 2.2 respectively, and the observed structure amplitudes and calculated structure factors are listed in Table 2.3.

2.4 Discussion of the Structure

The structure and numbering scheme of t-butylferrocenylnitroxide is shown in Figure2.2, and the bond lengths and angles are given in Table 2.4.

The N-O bond length is 1.263 (15) Å, which is intermediate between that of an N-O double bond $(1.20 \text{ Å})^7$ and an N-O single bond $(1.44 \text{ Å}).^7$ This is consistent with the three-electron nitroxide N-O bond postulated by Hoffmann and Henderson,⁴ and later by Linnet⁸ in his double-quartet theory of bonding.

The atoms C(1), N, C(11) and O are coplanar; the mean plane through them is represented by the equation -0.5947 X' + 0.7016 Y +-0.3925 Z' = 3.2126 Å, (the root mean square distance of the four atoms from the plane is 0.005 Å) and makes an angle of only 13.1° with the cyclopentadienyl ring. The Fe....N and Fe....O distances are 3.112 (9) and 3.629 (11) Å respectively, while the C (1) - N distance is 1.393 (14) Å, considerably less than the accepted C-N single bond length of 1.47 Å. These results indicate that direct Fe - N or Fe - O bonding, if any, must be weak, and the radical thus resembles more closely models of the α -ferrocenylcarbonium ion⁹ in which electron delocalisation occurs mainly via the metal-ring π -system.

The structural parameters of several other nitroxides have been determined by x-ray or electron-diffraction techniques, and the relevant bond lengths and angles from these structures (which are labelled 1 to 7) are summarised in Table 2.5. With the exception of di-p-anisylnitroxide (3), which was solved in projection, the values for the N-O distances agree within the limits of experimental error (mean value 1.278 ± 0.008 Å) and apart from di-t-butylnitroxide (2) and the two five-membered ring structures (5 and 7), the C-N-C angles are also remarkably constant (mean value $123.3 \pm 0.9^{\circ}$). In di-t-butyl nitroxide, the bulky t-butyl groups are probably causing a widening of the bond angle in an effort to reduce non-bonded interactions, while in structures 5 and 7, the ring size probably prevents any widening of the C-N-C angle. The dihedral angle which the N-O bond subtends with the C-N-C plane varies from 0° (planar) to 24° (pyramidal). However, examination of the non-bonded distances suggests¹⁰ that steric factors determine the deviation from planarity: in all cases except di-p-anisyl nitroxide the oxygen makes close 0....C contacts, or a close 0....F contact, in the case of structure (1). In t-butylferrocenylnitroxide and di-p-arisyl nitroxide, π -delocalisation over the N-O bond and aromatic system is probably the major factor in achieving planarity. The geometry of the nitroxide radical thus seems to be fairly well defined by the structures so far determined: in the absence of any steric effects, it has a planar

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nitrogen, with an N-O distance ca. 1.28 $\stackrel{\circ}{A}$ and a C-N-C angle ca. 123°. Given the accuracy of the results in Table 2.5, it is not really valid to assess the effects of different substituents on the N-O bond length, but they do suggest that any system into which the lone electron can be delocalised will cause a slight increase in the double-bond character of the N-O bond, as would be expected.

In the ferrocenyl residue, the iron atom is symmetrically placed between eclipsed cyclopentadienyl rings, with an average Fe····C distance of 2.038 \pm 0.007 Å. The average C-C distance in the cyclopentadienyl rings is 1.400 \pm 0.011 Å, and the average internal ring angle 107.99 \pm 1.1°. These values agree well with those of other recently-determined structures of ferrocene derivatives.^{17,18,19,20,21,22,23}.

The mean plane through the substituted cyclopentadienyl ring is defined by the equation -0.3985 X' +0.8172 Y -0.4165 Z' = 3.9346 Å, and the root mean square distance of the atoms from the plane is 0.014 Å. The equation of the mean plane through the unsubstituted cyclopentadienyl ring is -0.4197 X' +0.8037 Y -0.4219 Z' = 0.5533 Å while the root mean square distance of the atoms from the plane is 0.003 Å. The dihedral angle between the two rings is 1.47° , which means that they are coplanar within the limits of experimental error; the perpendicular distance between the rings is 3.31 Å. A point of interest in ferrocene derivatives is the conformation of the two cyclopentadienyl rings. In the case of t-butylferrocenylnitroxide they are eclipsed; in other ferrocenes they vary from being fully eclipsed to the fully staggered. However, as more ferrocene structures are solved, it is becoming apparent that the majority of ferrocenes are nearer the eclipsed than the staggered conformation. This is consistent with electron diffraction results^{24,25} which show that the free ferrocene molecule is eclipsed with a barrier to rotation of 0.9 k.cal.mole⁻¹; thus while crystal packing forces will be the major factor in influencing the conformations in ferrocenes, there will be a tendency to favour the eclipsed conformation where possible.

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TABLES AND DIAGRAMS

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Table 2.1

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Fractional coordinates $(\underline{x}, \underline{y}, \underline{z})$ and absolute orthogonal coordinates (in $\overset{o}{A}$ with $\underline{X}' = \underline{ax}\sin\beta$, $\underline{Y} = \underline{by}$, $Z' = \underline{cz}\cos\beta + \underline{ax}$, and with standard deviations in parentheses).

	<u>x</u>	X	<u>Z</u>	<u>x</u> '	<u>¥</u>	<u>z</u> '
Fe	0.2559	0.2165	0.219	1.425(2)	3.402(2)	-0.183(2)
0	-0.0737	0.3468	0.1420	-0.411(11)	5.449(12)	2.185(11)
N	0.0978	0.3742	0.1162	0.544(10)	5.880(9)	1.480(10)
C(1)	0.1248	0.3367	0.0327	0.695(9)	5.291(10)	0.227(11)
C(2)	0.3198	0.3381	-0.0060	1.781(12)	5.313(14)	-0.708(12)
C(3)	0.2528	0.2911	-0.0918	1.408(15)	4.573(12)	-1.811(11)
C(4)	0.0237	0.2587	-0.1106	0.132(14)	4.064(12)	-1.637(14)
C(5)	-0.0605	0.2829	-0.0330	-0.337(12)	4.444(13)	-0.357(14)
C(6)	0.3828	0.1656	0.1572	2.132(18)	2.602(16)	1.516(13)
C(7)	0.5724	0.1693	0.1188	3.188(13)	2.660(14)	0.595(12)
C(8)	0.4930	0.1194	0.0334	2.745(15)	1.876(13)	-0.479(15)
C(9)	0.2731	0.0866	0.0210	1.521(15)	1.361(14)	-0.229(17)
C(10)	0.2007	0.1156	0.0996	1.118(16)	1.817(14)	1.041(18)
C(11)	0.2586	0.4421	0.1781	1.440(12)	6.946(13)	2.058(12)
C(12)	0.3294	0.5046	0.1171	1.835(17)	7.929(13)	1.043(16)
C(13)	0.1180	0.4845	0.2346	0.657(20)	7.612(20)	3.144(21)
C(14)	0.4858	0.3966	0.2489	2.706(16)	6.231(15)	2.633(16)

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Anisotropic temperature parameters (Uij in $Å^2 \times 10^3$) with standard deviations in parentheses.

	<u>U</u> 11	<u>U</u> 22	<u>U</u> 33	² <u>u</u> 23	<u>2u</u> 31	<u>20</u> 12
Fe	38(1)	30(1)	37(1)	2(2)	38(1)	5(2)
0	82(7)	99(8)	124(9)	-101(14)	157(14)	- 81(12)
N	58(6)	36(5)	60(6)	-34(9)	67(10)	-12(8)
C(1)	31(5)	37(6)	39(6)	11(9)	11(9)	6(8)
C(2)	47(7)	71(9)	63(8)	25(13)	78(13)	27(12)
C(3)	99(10)	50(7)	35(6)	- 12(11)	59(13)	25 (14)
C(4)	68(9)	41(7)	57(8)	-22(11)	30(13)	11(11)
C(5)	43(7)	54(7)	68(8)	-28(13)	11(11)	8 (1 2)
C(6)	120(13)	76(10)	52(8)	61(15)	110(18)	8 7(1 9)
C(7)	60(8)	63(8)	43(7)	20(12)	16(12)	49 (13)
C (8)	69(9)	53(8)	72(9)	24(14)	60(15)	41 (13)
C(9)	74(10)	52(7)	90(10)	44(15)	53(16)	6 (1 4)
C(10)	81(10)	42(7)	130(14)	44(16)	120(20)	-4(14)
C(11)	46(7)	57(7)	51(7)	-35(11)	42(11)	-16(11)
C (12)	109(12)	35(7)	65(10)	15(12)	18(17)	-28(14)
C(13)	114(14)	99(14)	151(18)	-186(27)	168(27)	-101 (22 [†])
C(14)	83(10)	56(8)	70(9)	32(14)	31(15)	4(1 4)

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Table 2.3

Observed structure amplitudes and final calculated structure factors.

HKL	F DBS F CALC	H K L	F OBS F CALC	H K L F OBS F CALC	H K L F DES F CALC	N K L F DES F CALC
0 4.0	11.0 -0.3	10 3 12	4.7 4.1	1 1 4 17.6 -14.4	T-7+15-13+8 +19+9 -	2 7 1 53.2 59.2
0 0 0	20.4 21.6	512	8.7 -9.7 8.3 -11.D	1 2 8 41.9 39.7		2 8 1 14+4 -14+0
0 10 0	28.2 26.3	0 13 12	8.1 12.9	1 4 8 21.5 -20.9	8 =5 54+7 57+2	2 10 1 13.5 11.4
0 14 0	29.2 29.1	0 6 13	16.5 -18.4	1 8 8 20.4 14.4	2 8 -6 28.9 -24.1 1 8 -7 36.0 34.3	2 11 1 24+6 23+6 2 13 1 15+6 +16+0
0 16 0	23.1 -20.8	0 8 13	18+4 20+9	1 12 8 4.7 4.5	1 8 -6 11.4 -8.5	2 17 1 7+3 6+8
0 2 1	23.3 16.5	0 0 0	75.0 65.0	1 15 8 6.6 -7.3	1 8-10 14+1 15+1	2 1 2 12+8 12+6 2 2 2 55+4 57+3
071	78.7 -71.4	0 0 10	12.1 11.9	1 14 6 18.5 19.9	1 9 -2 27.0 29.3	2 3 2 21.9 -18.5
0 9 1	52.8 49.6.	1 2 0	23.5 -30.7	1 2 9 11.4 10.7	1 9 -5 26.4 26.2	2 5 2 48.0 49.8
0 11 1	26.3 -17.5	1 3 0	16.8 16.7	1 2 9 14.1 14.5	1 9 -7 37.7 39.3 1 9 -9 17.2 14.8	2 6 2 15-4 15-2
0 4 2	24.2 25.0	1 5 0	26-1 -31-4	1 5 9 14+5 -12+7	1 9-10 10-1 9-5	2 10 2 28.0 -29.2
0 6 2	24.8 .20.9	1 7 0	6.6 7.4	1 7 9 26.9 28.2	1 9-13 21.7 23.5	2 12 2 21+7 22+2 2 13 2 9+2 -10+1
072	10.5 -7.7	1 8 0	20.7 14.6	1 8 9 23.1 21.7	1 10 -1 41.7 -39.5	2 14 2 12.6 -14.1
0 12 2	27.2 -28.4	1 10 0	21.9 -15.6	1 10 9 8.6 -8.5	1 10 -3 35.0 -34.3	2 1 3 25.3 -23.9
0 14 2	27.4 30.4	1 13 0	28.4 30.5		1 10 -4 21.1 20.6	2 2 3 11.0 14.6
0 16 2	.14+6 15+2	1 17 0	21.2 20.4	1 2 10 28.1 27.6	1 10 -6 19.3 15.1	2 4 3 14.5 -14.1
0 2 3	59.2 -62.7	1 2 1	5.9 4.9		1 10 -7 11.8 -12.4	2 5 3 51.8 -54.4
0 4 3	21.1 20.5	1 5 1	9.7 -5.5	1 12 10 10.5 10.4	1 10-12 11.5 11.0	2 7 3 49.9 51.7
0 6 3	51.4 -47.5	1 4.1	18-2 -13-2	1 2 11 13.3 12.3	1 11 -2 16+7 -14+7	2 8 3 16+6 -13+5 2 9 3 27+4 -29+8
073	55+8 +56+0	1 10 1	49.5 -48.1	1 7 11 26.4 29.5	1 11 -3 13.0 -12.8	2 11 3 1247 11+1
υ 9 3	64.9 64.9	i iż i	14.4 13.1	1 0 12 28.8 -31.1	1 11 =5 22.0 +23.2	2 0 4 57.2 -64.4
0 10 3	23.5 -26.1	1 10 1	10.8 10.7	1 2 12 17.3 18.3	1 11 -6 16+9 -14+6	
0 14 3	8.7 -7.7	1 2 2	44.6 -44.7	1 5 13 15+7 -1++1	1 11 -9 14+2 -12+4	2 3 4 30.2 -31.5
0153	13.1 12.2	1 6 2	7.1 -8.4 - 13.1 10.7	1 7 13 14.6 16.2	1 11-11 22.0 -13.7	2 4 4 15.9 -11.3
6 2 4	30.4 -34.7	1 4 2	21.0 -19.9	1 0 14 13.8 -15.1	1 12 -1 16.5 16.5	2 7 4 21+5 -19+6
0 4 4	30.2 36.0	1 10 2	8.7 -6.6	1 2 14 14.9. 15.8	1 12 -5 12.1 12.7	2 10 4 14-5 6-5
0 5 4	9.4 5.8	1 11 2	26.6 -24.8	1 4 14 8.3 -8.7	1 12 -6 10.0 -10.2	2 11 4 9-1 15-1
0 7 4	28.7 24.5	1 15 2	25.7 -26.7	1 1 -4 75.5 -82.7	1 12 -8 24+1 -25+3	2 13 4 10.5 -8.1
0 20 4	21.3 -22.6	1 17 2	17.6 16.8	1 1 -6 58.6 -55.3	1 12-10 10-5 -17.8	2 14 4 20+6 -12+4
0 11 4	21.3 -19.5	111	10.4 -10.1	1 1 -9 10.0 9.4	1 12-12 14+2 -13+1	2 1 5 9.5 7.6
0 12 4	21.2 -20.0	1 4 3	7.4 5.7	1 1-10 25.3 -22.7	1 13 -2 17+2 15+4	2 2 3 18+9 18+1 2 3 5 16+7 12+5
0 16 4	25.3 -28.5	1 5 3	7.8 -7.8	1 1-12 14.0 -10.1	1 13 -4 17.3 13.0	2 4 5 17+3 -1++2
0 2 5	22.2 -28.0		50.3 52.7	1 1-14 12-1 9-1	1 13 -7 6.7 9.7	2 6 5 31.5 30.1
0 3 5	21.2 -20.9	1 8 7	76.9 76.7	1 1-15 13-1 13-5	1 13 -0 17+1 14+7	2 7 5 32.6 32.9
0 5 5	34.9 33.9	1 10 3	36.4 -37.8	1 2 -6 60.1 -55.5	1 13-10 9+0 8+7	2 9 5 29.3 -25.5
0 0 5	30.8 -29.9	1 11 3	19.5 16.2	1 2 -7 27.6 -27.2	1 14 -1 8.7 -8.5	2 0 6 41.6 -44.6
0 8 5	47.7 44.7	1 10 3	8.7	1 2 -9 17.0 -16.2	1 14 -6 20-5 19-7	2 2 6 17.6 17.0
0 10 5	33.2 -30.8	1 2 4	40.3 39.4	1 2-12 20.5 -15.5	1 14 -9 8.9 -3.9	2 4 6 18.7 -21.2
0 11 5	24.3 -23.1	1 3 4	23+2 23+7	1 2-14 12+1 -12+1	1 14-10 14-3 16-4	2 5 6 11+4 10+2
0 1 6	38.7 -35.0	1 5 4	9.1 -9.6	1 3 -2 42.9 92.7	1 15 -4 28.3 -29.5	2 9 6 10.5 -8.5
0 2 6	44.6 -42.5		35.4 36.7 22.3 -20.2	1 3 -4 42.2 47.8	1 15 -6 16+4 -14+7	2 11 6 10+6 10+0 2 13 6 9+9 -11+7
0 4 6	9.9 10.9	1 1 4	33.6 -29.8	1 3 -6 7.8 -0.8	1 15-12 7+9 -2+6	2 14 6 11.3 -13.6
0 5 6	40.0 -45.8	1 10 4	13.1 -11.3	1 3 -6 10.9 9.1	1 16 -4 19.2 -17.3	2 17 6 5.3 -10.2
076	12.2 10.2	1 11 4	8.4 -6.8	1 3 -9 24-1 -23-1	1 16 -6 21.0 -22.5	2 4 7 20.0 -22.4
0 9 6	10.3 14.4	1 15 4	23.0 -22.7	3-11 27.5 -25.3	1 17 -1 7.7 -0.0	2 7 7 21.3 22.0
0 10 6	8.2 -5.6 13.8 -13.5	1 16 4	8.9 8.3	1 3-13 28-9 -29-1	1 17 -4 14+7 13+7	2 8 7 21.7 -18.6 2 9 7 15.0 -16.8
0 12 6	10.0 -5.4	1 1 5	15.5 -14.9	1 4 -3 21.0 15.0	1 17 = 6 6+7 3+5	2 10 7 10.6 10.2
0 13 6	10.0 5.7	1 2 5	8.3 -6.2	1 4 - 22.5 24.3	1 16 -1 7.6 7.1	2 12 7 10.0 -10.0
0 15 6	10.0 -15.5	1 4 2	48.4 51.6	4 -7 25-1 23-6	1 18 -2 9+5 10+6 1 18 +3 7+6 8+7	2 16 7 8+5 3+3
0 10 0	7.5 9.1		42.4 -40.8	4-10 24-4 22-7	1 18 -4 9.0 9.9	2 2 4 12.2 13.0
0 16 6	6.1 8.7 26.5 #29.3	175	47.7 43.4 50.2 47.5	1 4-12 20+7 18+4	1 18 -5 8.9 8.3	2 3 3 20.8 -23.6
0 3 7	12.8 -11.8	1 9 5	34.7 -35.8	j 5 + 1 7+6 -5+1 1 5 -2 37+2 -35+5	1 0 -4 9.3 3.3	2 5 6 17.9 16.6
047	27.5 27.8	1 12 5	12.3 11.0	1 5 -3 23-2 23-1	1 0 -8 69+2 67+3	2 11 8 12.2 10.3
0 6 7	20.3 -16.5	1 18 5	7.4 9.9 37.7 -56.1	1 5 -5 11+4 12+5	1 0-10 50+9 52+1 1 0-12 28+4 26+3	2 13 5 17+6 -16+1 2 14 5 9+4 -8-7
0 8 7	42.7 44.2		29.2 -32.8	5 -6 8.7 -6.5	1 0-14 17+2 17+1	2 15 5 16+8 17+2
0 7	23.0 22.6	1 2 6	49.8 48.0 30.5 30.2	1 5 -7 3/11 3001	2 4 -1 10.9 21-1	2 4 9 10.4 17.5
0 1 8	62.2 -65.9	1 4 4	31.5 -27.7	1 5-15 13-3 -12-4	7 5 -1 40.0 -42.7	2 8 9 21+5 -22+2
028	24.7 -23.5	1 6 6	17.2 15.5	1 5-13 24+0 21+5	2 7 -1 60.3 61.6	2 10 4 13.9 15.3
0 5 5	14.8 -15.2	17.	20.9 -20.0	1 5-14 17.4 14.7 1 5 -2 24.5 -19.5	2 9 -1 11-3 11-4 2 9 -1 50+8 -52+7	2 12 * 0.6 -7.2
0 8 8	0.4 9.5	- i 🕴 i	13.4 12.4	42.0 -37.7	2 10 -1 11.4 -0.2	2 1 10 18.4 19.9
0 13 0	12.8 13.9	111 •	17.3 14.7	1 • -5 57.C -58.6	a 11 −1 20+7 31+0 2 13 −1 32+7 +11+ [#]	2 J 10 21.4 .2.11
0 2 9	12.9 -13.1	1 14 4	13.5 -12.8	1 4 44 1047 -1344.	2 17 -1 10+7 9+8	2 5 10 12.9 15.0
049	19.4 21.5	1 15 +	10.7 -12.3	7:	2 1 0 7.9 7.6	2 9 10 8.3 -7.5
0 7 4	22.3 -23.4	1 17 •	9.6 11.5	1 6 -9 11+2 -7+4 1 6-10 19+6 -40+1	2 2 0 23+3 29+8 2 3 0 19+3 -13+3	ζ 4 13 - 10+2 - 10+2 2 6 11 - 17+1 - 18+8
0 10 9	21.3 -18.3		16-2 -17-6	1 4-11 17+2 14+4	2 4 0 44.8 -52.4	2 8 11 15.8 -16.2
0 12 9	12.8 14.5	1 3 7	33.2 32.7 18.7 18.3	7 -1 10.7 -17.1	2 6 0 20+7 25+1	2 1 12 20.3 22.4
B 2 10	9.2 .9.2	;;;;	24.7 -27.7	1 7 -3 19.7 -19.5	2 9 0 10+7 -10+6	2 3 12 11+9 -11+0 2 4 13 10+2 -11+4
0 3 10 0 4 10	16.2 18.7		30.5 -31.4 19.0 17.4	7 .5 42.3 -41.1	2 12 0 25+3 27+5	2 6 13 10.7 12.8
0 11 10	16.7 -16.4	1 1 2	21.9 19.9	1 7 -0 6.0 3.0	z 14 D 30+8 -32+1 2 1 1 9+1 -7+9	z 8 13 13+6 -13+6 2 1 -4 12+0 -16+7
0 2 11	13.8 -16.0 17.1 18.4	1 10 7	17.3 -14.7	1 7 -2 15-5 15-	2 2 1 17.6 19.1	2 1 -5 25.2 -23.1
0 6 11	25.5 -31.6	1 11 7	12.4 10.7 8.6 10.1	1 7-10 12-0 9.9	2 4 1 7.e -5.5	2 1 -7 19+6 -19+5
0 10 11	10.5 -20.2	11.	12.7 -12.1	1 7-11 34+4 +24+4	Z 5 1 31+7 +34+9 Z 6 1 13+7 +13+9	2 1 -8 49.4 -48.5 2 1 -9 17.3 -14.1

Table 2.3 (cont'd)

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	•			-		100110	0/		
•••• •	F IFS F LALC	4	· UCS · CALL	4 K L	FORS F CALL	нкі	F 055 F CALC		
2 1-10	53.0 -49.2	2 15 -6	24+1 -21+7	3 1 -9	18+5 +18+3	4 13 -3	15.7 15.2	4 4 - 1	22.7 -24.3
2 1-12	23+1 -22+4	2 15 +0	15.7 -19.0	3 1-11	23.3 -23.8	4 1 = 2	10.5 -12.9	4 4 - 9	21.8 -22.5
2 2 - 1 - 1 -	12.07 -17.02	2 10 -2	22.7 25.4	3 2 - 4	0.9 8.4	4 2 - 2	29.7 -30.4	4 4-10	15.7 13.0
2 2 - 4	45.7 53.3	7 10 +4	11+5 15+1	3 2 -5	10+1 11+3	4 4 -2	31.5 34.0	4 4-11	28.2 -30.1
2 2 -5	15.6 -14.9	2 17 -3	10.4 10.1	1 2 - 6	17.5 19.5	4 5 - 2	13.4 -12.0	4 4-15	12.5 -12.2
2 2	21.7 22.2	2 17 -	11.7 12.5	1 2 -1	20.0 20.0	4 10 -2	26.0 21.7	4 5 - 4	10.5 10.8
2 2 - 9	29.4 -29.6	2 6 -6	14.8 .30.7	3 2 - 9	37.6 35.9	4 11 +2	10.1 8.5	4 5 - 5	20.2 30.1
2 2-11	17.1 -17.5	2 0 -8	20.2 -24.2	3 2-10	42.9 40.8	4 12 -2	20.0 -20.3	4 5 - 6	12.0 0.4
2 2-13	18.4 -18.0	2 0-1.	15.7 -15.1	3 2-12	10.5 16.6	4 1 -1	16.0 18.7	4 5 -0	25.4 29.0
2 2 - 17	3.7 3.2	3 5 - 7	27.7 31.7	3 3 - 3	39.2 45.4	4 2 -1	0.1 2.9	4 5-10	19+6 21+2
2 3 - 3	31.8 34.3	3 9 - 2	20.5 -20.4	3 3 - 5	38.8 39.7	4 3 - (31.9 - 39.6	4 5-12	14.3 12.8
2 3 -4	35.7 39.4	J 16 -?	12+5 10+1	3 3 - 6	17.1 -18.2		11.9 -12.0	4 4 -4	9.4 .9.8
2 3 -6	71.9 27.5	2 13 -2	21.0 -21.0	3 3 - 1	24.9 .24.9	4 7 -1	17.9 -18.0	4 6 -5	28.3 28.8
2 3 - 7	42.4 45.6	2 15 -2	70.4 20.4	3 3 - 9	25.0 24.8	4 9 -1	10.0 8.6		14.9 -18.0
2 3 - 1	34.9 37.9	3 1 -1	15-9 -17-1	3 3-11	44+0 41+3	4 11 -1	17.5 -16.6	4 6 - 1	22.2 -23.6
2 3-10	45.9 44.4	3 7 -1	11.5 11.5	3 3-15	6.7 8.1	4 13 -1	9.5 10.5	4 6 - 9	10.8 17.1
2 3-12	30.4 24.5	3 4 -1	27.2 -27.0	3 4 - T	38.0 -43.7	4 0 0	65.1 41.6	4 6-11	14.3 16.4
2 3-14	14.1 16.0	J 6 - 1	27.5 27.0	2 4 - 1	27.4 -26-7	4 2 9	27.6 -32.7	4 4-15	14.4 20.3
2 4 - 2	21.9 20.2	3 8 - 1	20.0 -23.9	3 4 - 6	31.7 -33.2	4 4 5	26.3 27.*	4 7 -4	14.3 -13.3
2 4 -4	4c.J -54.3	3 10 -1	32.3 30.2	3 4 -7	28.6 -27.8	4 10 5	20.2 17.2	4 7 - 5	30.3 -33.7
2 4 -5	5.5 7.4	a 12 -1	9.4 -9.2	3 4 -	20.0 -18.5	4 11 0	10+1 ++5	4 7 - 7	15.3 -14.0
2 4 -0	6.0 -5.4	3 14 -1	4.1 4.7	3 4-10	22.9 -20.4	4 14 5	14+1 13+*	4 7 -8	13.7 / +12+5
2 4 - 9	32.6 29.7	323	10.9 -16.5	3 4-12	32.0 -31.0	4 1 1	17.5 18.5	7-10	10.1 -11.8
2 4-11	24.0 21.9	3 3 2	20+2 -40+1	3 4-13	13.3 9.4		20.9 -21.9	4 8	20.1 -16.9
2 4-12	12.9 -11.2	3 4 2	26.9 30.1	3 4-14	10.4 -9.2	451	17.4 16.2	4 8-11	20.0 -19.2
2 4-13	12.7 11.1	3 9 2	22.07 -22.0	3 5 -4	43.8 44.4	4 4 1	10-5 -11-2	4 8-13	18.2 -19.9
2 4+15	20.0 19.9	3 11 1	1 10.+	3 5 - 5	31.9 -31.7	4 7 1	16+5 +16+6 5+8 8-0-	4 9 -5	23.3 26.2
2 5 - 2	19.5 -21.4	3 1 J F	26.5 -28.1	3 6 -6	36.7 27.1 43.1 -40-4	4 9 1	20.0 30.1	4 9 .7	23.8 23.9
2 5 - 3	37.7 -42.2	3 15 1	19.2 20.9	3 5 - 9	34.3 -33.1	4 10 1	14.3 -12.9	4 9-10	11.4 -12.1
2 5 - 6	30.4 -28.9	5 4 i	20.0 -29.7	3 5-10	14.5 12.2	4 11 1	11+5 -13+2	4 10 -7	10.1 9.8
2 5 -7	39.0 -40.2	3 6 1	25.0 22.0	3 5-11	31.5 -30.8	4 2 7	28.4 -28.4	4 10 -*	20.0 21.4
2 5 -0	35.1 -36.4	371	32.3 -30.1	3 5-15	19.9 -19.0	4 4 2	21.6 23.4	4 10-11	22.3 16.6
2 5-11	12.6 11.0	3 9 1	14+3 11+7	3 4 - 3	\$5.2 56.6	4 6 2	13.4 -13.6	4 10-13	11.3 12.4
2 5+17	30.3 -32.2	3 10 1	20.4 17.5	3 6 -5	49.8 48.8	4 10 2	14.2 11.4	4 11 44	14.3 13.6
2 5-14	17.7 -17.6	3 12 1	13-3 -11-2	3 6 - 6	31-9 32-5	4 14 2	11.1 10.4	4 11 -7	11.0 -14.5
2 6 - 3	17.2 19.0	3 2 2	10.3 .7.7	3*	19.7 18.1	4 1 3	14+5 18+4	4 11 -8	19.8 22.4
2 6 -5	30.2 -37.7	3 3 2	38.7 -38.2	3 6 - 9	14.2 14.4	4 2 3	17.9 -16.3	4 11-10	22.3 21.5
2 6 -6	46+2 41+1	3 4 2	10.5 14.5	3 6+12	21.1 19.9	4 5 3	10.6 17.3	4 12 -4	16.3 -17.3
2 6 - 7	34.1 -37.2	3 5 2	10.9 .9.5	3 7 - 7	14.5 15.2	4 7 3	23.8 .24.3	4 12 -6	14.0 -10.9
2 6-10	12.3 10.3	372	16+3 -15+3	37-4	19.5 -18.1	4 6 3	24.0 24.5	4 12 -8	11.0 -9.3
2 6-11	25.5 -27.3	362	8.6 -5.3	3 7 - 5	25.9 26.5	4 10 3	19.8 -16.5	4 12-11	9.4 -10.3
2 0-13	21.0 -17.7	3 0 2	76.4 25.4	. 3 7 -7	28.1 27.4	4 12 3	9.0 8.2	4 13 -4	9+6 -7+3
2 7 - 2	17.6 17.5	3 13 2	18.3 -17.2	3 7 - *	30.6 29.8	4 0 4	18.8 19.4	4 13 -4	13.3 -15.8
2 7 -4	16.8 -10.9	3 15 2	17.9 17.3	3 7-11	21.1 18.5		9.5 -10.4	4 13-10	12.9 -15.4
2 7 - 5	34.1 45.7	3 1 3	13.6 13.1	3 6 - 3	26.7 -26.4	4 3 4	9.6 5.7	4 14 +4	14.7 .18.4
2 7 - 9	22.3 15.0	5 5 5	20.3 -21.0	3 8 -4	12.7 +11.6	4 4 4	11.6 -5.7	4 14 -4	15.1 14.0
2 7-10	12+6 13+2	3 4 3	15.0 -11.5	3 4 -5	33-1 -35-7	4 10 4	13.6 11.1	4 0 - 1	9.0 9.7
2 7-12	10-0 11-5	3 5 3	22-1 21-0	3 8 - 7	9.2 -8.4	4 2 5	11.5 +11.2	4 0-10	21.8 23.9
2 8 - 2	19.6 10.5	3 7 3	24.2 -23.8	3 9 - 3	16.7 .15.3	4 3 5	14+1 -17+9	4 0-12	17.4 13.2
2 8 -5	35.3 38.5	383	23.5 -21.8	3 9 -4	16.9 -14.5	4 4 5	20-2 20-1		7.6 -11.7
2 8 -7	19.3 16.9	3 9 3	15.0 12.6	3 9 - 7	21.4 -23.3	4 6 5	20+2 +14+5	4 14 -0	8.6 -10.2
2 8 - 9	17+6 15+5	3 10 3.	10.9 -040	3 9-10	13.3 -12.8	4 7 5	16.4 -15.6	5 1 -3	5.8 -2.6
2 6-13	24.7 25.5	3 2 4	21.6 -20.2	3 4-11	15.2 -14.9		19.8 14.7	5 2 - 1	12.7 -14.0
7 9 - 3	35.7 .34.4	3 3 4	23.9 -23+4	3 10 -3	12.5 7.6	4 10 5	10.6 -11.7	5 5 - 3	13.7 11.7
2 0 -5	31.7 -33.5	3 5 4	13.6 15.0	2 10 -5	12.7 14.2	4 0 6	10.1 9.0	5 6 -3	36.0 -30.9
2 9 -7	2:+2 -19.9	5 11 4	15.3 12.1	3 10 -6	14.9 -15.1	4 1 6	16.5 -19.5	5 7 - 3	25.6 24.9
29-8	17+6 15+4	3 13 4	15.8 -15.1	3 10 -7	13.1 11.3	4 7 6	9.7 5.7	5 10 +3	13.8 -14.1
2 9 - 9	15.5 34.4	315	19.4 17.4	3 10 -8	13.2 -14.9	4 3 7	10.0 -7.5	5 12 -3	10.3 10.8
2 9-11	1	3 4 5	17.2 -15.7	3 10-12	12.3 -15.0	4 4 7	13.9 13.6	5 2 -4	10.0 -8.1
2 9-13	11.9 9.4	3 5 5	20.9 27.2	3 11 -3	13.0 13.7		9.5	5 11 +4	10.7 -8.7
2 10 -2	22.7 -25.5	365	18:0 17:2	3 11 +5	15.2 15.1	- 4 7 7	16.6 -10.4	5 12 -4	12.7 -11.2
2 10 -5	11.08 01902	3 8 5	18.7 -20.0	3 11 -6	13.2 10.3		12+4 11+7	5 13 -4	9.4 9.3
2 10 -7	**8 *7.3	3 9 5	18.9 16.8	2 !! -?	15.4 12.9	4 3 6	13.4 11.5	5 1 -2	22.7 .24.4
2 10-15	13.0 -12.7	3 10 5	15.3 14.7	3 11 - 4	14.3 12-4	4 5 8	10.5	5 2 - 2	7.0
2 10-11	24.2 26.2	3 13 5	11.6 12.0	3 12 -3	24.4 -26.4	4 1 -4	12.9 10.2	5 3 -2	17.9 17.9
2 11 -5	12.4 10.5	3 0 6	18.8 23.2	3 12 -4	10.9 -1.4	4 1 -7	12.2 12.8	5 5 -2	12.2 -13.8
2 11 -4	17.9 -15.2	316	20.0 21.1	3 12 -0	15.3 .12.4	4 1 - 0	28.6 26.3	52	12.9 -12.4
r 11 -7 2 11 -F	12.4 -25.9	366	15.2 -14.2	3 12 -8	31.7 27.4	<u>.</u>	20.4 21.6	5 7 -2	13.4 10.6
1 11 -9	15.2 215.7	3 12 6	15.9 -14.7	3 12-10	17.4 16.2	4 1-10	13.7 .0.8	5 12 -2	10.2 .8.4
2 11-15	10.1 -17.1	3 3 7	13-1 -12-0	3 13 -4	10.4 11.7	4 1-12	23.9 25.4	5 13 -2	13.0 14.1
2 11-12	13.4 -14.0	357	10.0 17.3	3 13 -4	15.1 -10.0	4 2 -4	34.2 -37.0	2 1 1	7.4 4.9
2 12 -5	13.9 11.5	377	22.4 -21.4	2 12 -7	18.3 -17.4	4 2 -5	22.2 -20-5	7 3 -1 5 4 -1	23.0 22.1
2 12 -6	10.3 21.4	3 8 7	15.2 -15.8	3 13 -9	14.0 -13.6		7.3 7.0	5 5 -1	9.0 6.8
2 12 -7	15.0 17.2	3 10 7	10+2 14+4	3 14 -5	12.7 11.7	4 2 -8	27.3 -26.3	<u> </u>	29.5 -25.2
2 12 -0	14.7 14.1	5 11 7	11.7 -10.5	3 14 -6	14+5 -14+7	4 2 - 4	24.7 30.3	5 7 -1	26.5 21-3
2 12-12	17 3.4	308	22.4 20.9	3 14 -8	10.7 -10.1	4 2-11	40.3 38.1	5 10 -1	11.1 .12.0
2 13 -3	15.0 -11.7	310	10.0 9.8	3 15 -6	13.4 13.0	4 2-13	11+4 11+2	5 12 -1	4.4 8.7
2 13 -5	21.0 21.0		15.4 -6.3	3 0 + 4	22.6 -20.4	4 3 -4	18.3 -16.4	- 3 0 0	17.3
2 13 -7	16.2 -18.2	334	13.1 -12.3	3 0 -•	10.7 6.4	4 3 - 4	19.7 -21.0	5 5 0	15.0 15.0
212 -0	25.3 24.9	3 5 1	12.7 12.1	3 0-10	23.3 .24.8	4 3 -7	21+1 -19+1		
2 13-10	25.9 -27.5	5 6 10	18.0 18.8	3 9-12	24.4 -24.1	4 3 .	1947 -2043		
2 14 -3	9.2 4.6	3 2 10	17.6 -16-2	2 0-14	10+# +7+1	4 3-10	20.7 -26-5		
2 14 -4	71.7 -22.0	3 4 10	12.3 10.0	1 1 3	35.8 31.6	4 3-12	14.3 -14.0		
2 14 -7	17.0 -16.5	5 1 - 4	18.6 22.8	4 3 - 2	41.4 -34.0	4 3-13	14.2 11.0		
2 14 -0	12.0 -11.1	3 1 -5	23.3 -25.0	4 4 - 3	24.6 -20.0	4 4 + 4	9.5 7.4		
2 14 -9	11-5 -10-5	1 1 -	37.0 39.1	4 7 - 3	34.8 -36.4	4 4 -5	24.0 -25.6		
2 14-10	17.6 -16.4	5 1 - 9	25.4 29.3	4 11 -3	14.3 -13.4	• • -•	25.6 27.4		

Table 2.4

Bond lengths $(\stackrel{0}{\mathbb{A}})$ and angles (degrees) with standard deviations in parentheses.

Fe - C distances

Fe - C(1)	2.067(10)	Fe - C(6)	2.006(14)
Fe - C(2)	2.014(14)	Fe - C(7)	2.065(13)
Fe - C(3)	2.006(12)	Fe - C(8)	2.040(14)
Fe - C(4)	2.056(14)	Fe - C(9)	2.044(14)
Fe - C(5)	2.055(12)	Fe - C(10)	2.026(16)

Mean value = 2.038 ± 0.007 .

C - C distances in cyclopentadienyl rings

C(1) - C(2)	1.433(16)	C(6) - C(7)	1.402(20)
C(2) - C(3)	1.380(17)	C(7) - C(8)	1.401(19)
C(3) - C(4)	1.385(20)	C(8) - C(9)	1.352(21)
C(4) - C(5)	1.415(19)	C(9) - C(10)	1.409(24)
C(5) - C(1)	1.457(16)	C(10) - C(6)	1.367(23)
	Mean value :	= 1.400 ± 0.011	

Other bond lengths

N - O	1.263(15)	C(11) - C(12)	1.466(19)
N - C(1)	1.393(14)	C(11) - C(13)	1.495(24)
N - C(11)	1.508(15)	C(11) - C(14)	1.564(20)

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Table 2.4 (cont'd)

Bond angles in the cyclopentadienyl rings

C(5) - C(1) - C(2)	106.5(1.0)	C(10) - C(6) - C(7)	110.8(1.3)
C(4) - C(5) - C(1)	106.5(1.1)	C(9) - C(10) - C(6)	106.7(1.4)
C(3) - C(4) - C(5)	108.7(1.1)	C(8) - C(9) - C(10)	104.6(1.4)
c(2) - c(3) - c(4)	110.2(1.1)	C(7) - C(8) - C(9)	111.0(1.3)
C(1) - C(2) - C(3)	108.0(1.1)	C(6) - C(7) - C(8)	104.0(1.2)

Mean value = 108.0(1.1)

Other bond angles

· .

	C(1) - N - C(11)	125.4(0.9)	
N - C(11) - C(12)	111.7(1.0)	C(13) - C(11) - C(14)	111.1(1.2)
N - C(1) - C(5)	122.0(1.0)	C(12) - C(11) - C(14)	110.1(1.1)
N - C(1) - C(2)	131.5(1.0)	C(12) - C(11) - C(13)	110.2(1.3)
C(11) - N - 0	118.5(1.0)	N - C(12) - C(14)	107.4(1.0)
C(1) - N - O	116.1(1.0)	N - C(11) - C(13)	106.4(1.1)

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Table 2.5

	•			
Structure	N-0 (A)	C-N-C (deg.)	(deg.)	Ref.
1	1.26±0.03	120.9 * 2.0	21.9	9
2	1.28±0.03	126.0 * 3.0	assumed planar	10
3	1.23 - 0.05	124.0 [±] 5.0	0	11
4	1.291±0.007	125.4 [±] 0.5	15.8	12
5	1.277±0.008	114.7 ⁺ 0.7	0	13
6	1.308±0.022	121.0 [±] 1.5	24	14
7	1.267±0.008	114.8 [±] 0.5	0	15
Bu ⁺ -ferrocenyl nitroxide	1.263 [±] 0.015	125 .4±0.9	0	
. –				

Average

1.278±0.022 123.3±2.4



-40-Table 2.6

Short contact distances (A)

(a) Intermolecular contacts less than 3.6 Å.

$$C(10) \cdots O(2^{I})$$
 3.434 $C(17) \cdots O(2^{I})$ 3.515
 $C(5) \cdots O(2^{I})$ 3.511

(b)	Some	important	intramol		
	0(2)	•C(16)	2.596	C(5)····C(15)	3.149
	0(2)	•C(17)	3.244	Fe····N	3.112
	-1.2 5		Fe••••0	3.629	

Position I is at 1 + x, y, z.







Figure 2.2 : The molecular structure of t-butylferrocenylnitroxide.





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CHAPTER 3

1.

THE CRYSTAL AND MOLECULAR STRUCTURE OF THE 1:1 COMPLEX OF HEXAHELICENE WITH 4-BROMO-2,5,7-TRINITROFLUORENONE.





(2)

3.1. Introduction.

Hexahelicene (1) was first synthesised in 1956 by Newman et al¹ .and its structure is of great interest because of the severe overcrowding of the terminal rings. To relieve this overcrowding, the molecule must assume a non-planar conformation and the two aspects of the structure which are of most interest are (;) the extent of the deviation from planarity, and (\ddot{u}) the effect, if any, which this deviation from planarity has on the bond lengths and angles of the molecule. Preliminary answers to these questions were given when the structure of the 1:1 complex of hexahelicene with 4-bromo-2.5.7-trinitrofluorenone (2) was solved by Robertson et al². The hexabelicene molecule was shown to have the expected helical structure, but because of the large number of atoms in the asymmetric unit (100) and the large number of observed intensities (6,254), only a limited least-squares refinement of the structure was possible using the computing facilities then available at Glasgow. However, the introduction of the XRAY70 system of programs onto the Univac 1108 computer at the National Engineering Laboratory. East Kilbride, enabled the refinement of the structure to be completed. The details of this refinement are described in section 3 of this chapter, and the resulting structural parameters are discussed in section 4.

3.2 Experimental.

Crystal Data.

Data Collection.

The intensity data were collected using a small crystal of dimensions 0.25 x 0.15 x 0.15 mm³ mounted along <u>a</u>. Multiple-film equi-inclination Weissenberg photographs were taken of the Okl - 8kl reciprocal lattice nets using CuK_a radiation, and the intensities of some 6254 reflections were measured. No absorption corrections were applied to the data.

Refinement of the Structure.

The structure was solved by the heavy-atom method, and a random sample of about 2,000 reflections were used in the initial refinement. The hexahelicene and 4-bromo-2,5,7-trinitrofluorenone (B.T.N.F) molecules were refined during alternate cycles of isotropic least-squares refinement, and convergence was reached with R = 19%. The resulting atomic parameters were used as the starting point for the refinement on the Univac 1108. Two cycles of full-matrix, isotropic least-squares refinement were carried out, using the XRAY70 program ORFLS, after which R was 18%. A difference map calculated at this stage revealed the presence of a diffuse circle of electron density around the origin, indicating that a disordered solvent molecule (benzene) is located at that point in the unit cell. The omission of this solvent molecule explains the relatively large discrepancy between the observed and previously-calculated densities (1.52 and 1.49 respectively); the density calculated with the solvent molecule included is 1.52.

The difference map also showed that one of the two ETNF molecules in the asymmetric unit was disordered about the 2-fold rotation axis of the fluorenone residue (along the line of the carbonyl group), the two orientations being populated approximately in the ratio 2:1. Because of the 2-fold symmetry of the 2,7-dinitrofluorenone residue, the only difference in the two orientations is the interchange of the 4-bromo and 5-nitro groups. The disorder was thus accounted for by introducing two sets of atoms for the 4-bromo and 5-nitro groups, the coordinates of each set of atoms being those determined from the difference map. Each disordered atom was assigned an isotropic temperature factor which had the same value as that of the corresponding atom in the other ETNF molecule, and a further two cycles of leastsquares refinement were carried out, during which only the disordered bromine atom positional and population parameters were allowed to vary.

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with the population parameters of the disordered nitro group being constrained to be equal to the population parameters of the appropriate bromine atoms. The R-value was reduced to 17%, and the resulting population parameters for the two sets of atoms were 0.69 and 0.31. These values were not refined during the subsequent cycles of leastsquares analysis.

The refinement was completed with four cycles of block-diagonal least-squares analysis with anisotropic temperature factors, during which neither of the partially-occupied nitro positions were refined. Hydrogen atoms were included in their calculated positions (Table 3.3), but were not refined, and electron density was included around the origin to allow for the disordered solvent molecule. The final value of R was 10.9%. During the final two cycles of refinement, the data were weighted according to the following scheme:

Weight $(W) = X \times Y$

If $A \times F_{obs} > F_{calc}$, W = 0.000000001.

If $\sin\theta > B$, X = 1, else X = $\sin\theta/B$.

If $C > F_{obs}$, Y = 1, else $Y = C/F_{obs}$.

The final values of A, B, and C were 0.1, 1.0, and 20.0 respectively. The final fractional coordinates and temperature factors are listed in Tables 3.1 and 3.2 respectively, while the observed structure amplitudes and calculated structure factors are listed in Table 3.4. The atomic numbering system is shown in Figure 3.1.

The estimated standard deviations of one of the hexabelicene molecules

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are, on average, about twice those of the other hexahelicene molecule in the asymmetric unit; this can be attributed to a slight disorder of the molecule, as a result of the proximity of its ring 5, in particular atoms C(15) and C(16), to the disordered BTNF bronc and nitro groups. The hexahelicene and BTNF molecules which are not disordered are jointly labelled Complex 1, while the disordered hexahelicene and BTNF molecules are labelled Complex 2.

3.3 Description and Discussion of the Structure.

A view of the structure projected along \underline{a}^* is given in Figure 3.2. The unit cell contains four hexahelicene molecules and four HTNF molecules, with a disordered solvent molecule occupying a cavity between adjacent hexahelicene and BTNF molecules at the origin. Two of the hexahelicene molecules are the left-handed enantiomer and two the right-handed enantiomer, each of the former being related to each of the latter by a centre of symmetry. The determination of the absolute configuration of (-)-2-bromohexahelicene by Lightner et al³ enabled them to show that (-)-hexahelicene has the absolute configuration of a left-handed helix. Each BTNF molecule is sandwiched between two hexahelicene molecules, with rings 2 and 3 of the BTNF molecule lying almost parallel to rings 1 and 2 or 5 and 6 of each of the adjacent hexahelicene molecules, at approximately van der Waals distances. Intermolecular C...C contact distances less than 3.5Å are listed

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in Table 3.5. The crystal structure is thus built up of alternate donor (hexahelicene) and acceptor (BTNF) molecules, orientated to allow the maximum overlap of their respective π -molecular orbitals. However, the C...C contacts in Table 3.5 indicate more effective overlaps between the Complex 1 hexahelicene molecule and the two BTNF molecules than between the Complex 2 hexahelicene molecule and the BTNF molecules.

The bond lengths of the hexahelicene and ETNF molecules are listed in Table 3.6, and their bond angles in Table 3.7. The dimensions of the Complex 1 hexahelicene molecule agree well with those determined for 2-bromohexahelicene³ and the isomorphous 2-methylhexahelicene⁴, and indicate that the helical conformation of the hexahelicene molecule is achieved with little deviation of the bond lengths and angles from their expected values. No meaningful comment can be made about the bond lengths and angles of the disordered hexahelicene molecule because of their high estimated standard deviations. Moreover, comparison of equivalent bond lengths and angles in the two hexahelicene molecules suggests that the standard deviations of the disordered molecule are too optimistic. The following dicussion of the bond lengths and angles in hexahelicene is thus based on the parameters of the Complex 1 molecule only.

Since the hexahelicene molecule has a two-fold axis of symmetry (along the bond C(11) - C(24)), the bond lengths of the two equivalent

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halves of the molecule can be averaged, and the resulting values are given in Table 3.8; the average root mean square difference in the bond lengths of the equivalent halves of the molecule is 0.020\AA . In addition to the mean observed bond lengths, Table 3.8 lists the lengths of the same bonds as predicted by molecular-orbital and valence-bond calculations. The molecular-orbital bond lengths $(D_{m,0})$ were calculated from bond-orders (p) which resulted from a π -electron calculation⁵ in which a planar hexahelicene molecule was assumed. The relationship⁶ $D_{m,0} = 1.50 - 0.16p$ was used to calculate the bond lengths.

Hexahelicene has 21 different Kekulé structures, and the doublebond character of each bond in the molecule was assessed by averaging these 21 resonance structures. The resulting bond numbers (n) - the double-bond characters + 1 - were used to calculate bond lengths $(D_{v.b.})$ using the relationship derived by Pauling⁷:

$$D_{v.b.} = D_1 - (D_1 - D_2) \cdot 1 \cdot 84(n-1)/(0 \cdot 64n + 0 \cdot 16)$$

The values used for D_1 and D_2 were 1.504 and 1.334 respectively. The average root mean square differences between the calculated and mean observed bond lengths are 0.019Å and 0.018Å for the $D_{m.o.}$ and $D_{v.b.}$ respectively. None of the differences between the observed and calculated bond lengths listed in Table 3.8 are statistically significant.

It is worth commenting at this point on the observation by

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Lightner et al^{3,4} that the six bonds bordering the 'inner core' of the helix are all longer than average. They argue that since this is the region of the molecule most subject to distortion, a decrease in the double-bond character of these six bonds is to be expected. However, both the molecular-orbital and valence-bond approximations predict longer than average lengths for the inner core bonds (Table 3.8) from calculations based on a planar molecule.

Inspection of the Complex 1 hexahelicene bond angles shows that only the angles around the inner core deviate significantly from the normal value of 120° , the largest deviation being that of angle C(23) - C(24) - C(25) which has a value of 127° .

The distortion of the molecule is not evenly distributed between the six rings. The deviations of the atoms from the mean planes through the aromatic rings are given in Table 3.9, and show that rings 3 and 4 are subject to the greatest distortion. Rings 2 and 5 also show significant deviations from planarity, but rings 1 and 6 are planar within the limits of experimental error. The dihedral angles between successive mean planes (Table 3.10) show the same trend, although the differences in the angles are not statistically significant.

A view of the hexahelicene molecule showing its helical structure is given in Figure 3.3. The intramolecular non-bonded C...C contacts which define the pitch of the helix are given in

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Table 3.11. The shortest such contacts are C(1)...C(22) and the symmetrically-related C(21)...C(26); both are 2.966(13)Å, and compare well with the value predicted from theoretical calculations⁸ of 3.004Å.

The dimensions of the two BTNF molecules do not differ significantly from those determined by Pollard⁹. The two benzene rings of each molecule are twisted out of the plane of the fluorenone residue in order to relieve the steric strain caused by the juxtaposition of the bromo and nitro groups at the 4 and 5 positions. The nitro groups at the 2 and 7 positions are essentially coplanar with their respective aromatic rings, whereas the 5-nitro group is forced out of coplanarity with the aromatic ring because of the proximity of the 4-bromo group. The equations of the mean planes of the C-nitro groups and of the aromatic rings in the BTNF molecules are given in Table 3.12, while the dihedral angles between the planes are given in Table 3.13.

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TABLES AND DIAGRAMS

. . • Fractional atomic co-ordinates (x 10^5 for bromine and x 10^4 for all other atoms, with standard deviations in parentheses).

Complex 2

Complex 1

	x	У	Z	x	У	Z
Br(1)	57836(12)	4977(5)	23437(7)	59186(14)	8756(7)	64090(8)
Br(2)				76618(60)	15992(26)	80593(31)
N(1)	115(10)	180(5)	2457(7)	217(12)	213(6)	6000(7)
N(2)	7 932(10)	4464(4)	4413(5)	7335(12)	4228(6)	10 049(6)
N(3)	7 283(8)	1955(4)	2397(5)			
0(1)	93(11)	- 421(5)	1970(8)	388(11)	-355(5)	5511(7)
0(2)	-8 93(8)	390(5)	2761(7)	-952(11)	375(8)	6162(8)
0(3)	2574(9)	2975(4)	4442(5)	1895(7)	2970(4)	8393(4)
0(4)	7415(11)	4931(4)	4909(5)	8598(12)	4246(6)	10 262(6)
0(5)	9100(9)	4543(4)	4207(5)	6656(13)	4723(6)	10294(6)
0(6)	8427(11)	1926(5)	2489(7)			
0(7)	6418(11)	1698(5)	1834(6)			
C(1)	7392(8)	3618(4)	5926(4)	3775(10)	2810(6)	1995(5)
C(2)	8695(9)	3980(5)	5833(5)	2386(13)	2613(8)	2204(7)
C(3)	9644(10)	3595(5)	5360(5)	1761(14)	3113(9)	2736(9)
C(4)	9256(10)	2857(6)	4964(5)	2425(15)	3763(9)	3091(8)
C(5)	7943(10)	2477(5)	5024(5)	3858(18)	4051(7)	2944(7)
C(6)	7447(13)	1711(5)	4523(6)	4622(24)	4727(8)	3385(8)

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Table 3.1 (cont'd)

	x	У	Z	x	У	z
C(7)	6098(11)	1368(5)	4501(6)	5937(20)	4922(7)	3278(8)
C(8)	5118(10)	1746(5)	50 1 3(5)	6709(14)	4482(9)	2721(10)
C(9)	3615(11)	1377(5)	4902(6)	8128(22)	4666(13)	2657(12)
C(10)	2672(11)	1757(6)	5328 (6)	8868(13)	4221(10)	2239(10)
C(11)	3156(9)	2451(5)	5969(5)	8254(27)	3521(12)	1653(12)
C(12)	2114(10)	2827(6)	6402(6)	8764(19)	2944(16)	1151(16)
C(13)	2584(10)	3484(6)	7025(6)	8256(19)	2324(11)	620(10)
C(14)	4067(9)	3751(5)	7326(5)	6676(22)	2173(11)	404(10)
C(15)	4508(11)	4406(5)	8047(5)	5943(35)	1563(12)	-1 79(12)
C(16)	5917(12)	4654(5)	8380 (6)	4435(37)	1350(8)	-533(8)
C(17)	6998(9)	4233(5)	8079(5)	3546(22)	1975(8)	-226(8)
C(18)	8445(11)	4436(6)	8490(6)	2114(20)	1985(9)	- 511(8)
C(19)	9435(1 0)	3972(6)	8264(6)	1539(17)	2503(11)	-295(8)
C(20)	8969(9)	3291(5)	7634(5)	2330(12)	3214(8)	315(7)
C(21)	7618(9)	3081(5)	7196(5)	3672(10)	3249(5)	648(5)
C(22)	6606(8)	3560(8)	7397(5)	4395(13)	2645(5)	427(5)
C(23)	5124(8)	3358(4)	6950(5)	5845(14)	2695(7)	792(8)
C(24)	4 682(8)	2764(4)	6173(5)	6565(11)	3282(8)	1472(8)
C(25)	5611(9)	2457(4)	5606(5)	5936(11)	3746(6)	2142(7)
C(26)	6977(8)	2860(4)	5544(5)	4535(11)	3530(5)	2333(5)
C(27)	4103(10)	909(5)	2603(6)	4130(9)	1068(5)	6770(6)
C(28)	2761(12)	455(5)	2411(7)	2842(11)	581(6)	6293(7)

.

(cont'd)

	x	У	Z	x	y	2				
C(29)	1570(9)	701(5)	2683(6)	1533(10)	779(6)	6499(7)				
C(30)	1611(9)	1403(5)	3232(6)	1384(10)	1418(6)	7097(7)				
C(31)	2940(9)	1863(4)	3390(5)	2657(9)	1 864(5)	7561(6)				
C(32)	3361(11)	2643(5)	3989(6)	2824(10)	2626(6)	8194(6)				
C(33)	4846(9)	2896(4)	3925(5)	4383(10)	2842(5)	85 1 6(5)				
C(34)	5653(10)	3592(4)	4279(5)	5078(11)	3480(5)	9148(6)				
C(35)	7007(10)	3709(5)	4053(6)	6522(11)	3 535(5)	9376(5)				
C(36)	7562(10)	3186(5)	3480(6)	7285(10)	2980(5)	9063(5)				
C(37)	6679(9)	2486(5)	3102(5)	6528(10)	2339(5)	8443(6)				
C(38)	5350(8)	2314(4)	3331(5)	5105(8)	2262(4)	8114(5)				
C(34)	4193(8)	1656(4)	3057(5)	4043(9)	1691(5)	7456(5)				
Assumed coordinates of the disordered nitro group.										
N(3)	7321	1786	8277							
0(6)	8574	1818	8234	Population	parameter =	0.69				
0(7)	6587	1149	8105							
N(3')	5 357	085 7	6340							
0(6')	6536	1321	6511	Population :	parameter =	0.31				
0(7')	47 14	0179	6064							
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Table 3.2

Anisotropic thermal parameters (Uij x 10^4 for bromine, Uij x 10^3 for all other atoms). Standard deviations are in parentheses.

Complex 1

	^U 11	U ₂₂	U ₃₃	^U 12	^U 13	U23
Br(1)	686(7)	561(5)	928(8)	161(4)	168(5)	153(4)
N(1)	53(5)	80(5)	121(7)	-6(4)	-12(4)	44(4)
N(2)	89(6)	58(4)	54(4)	-10(3)	-19(4)	25(2)
N(3)	35(4)	60(4)	83(5)	-4(3)	14(3)	21(3)
0(1)	83(6)	77(5)	183(10)	-28(4)	4(4)	17(5)
0(2)	46(4)	96(5)	180(8)	0(3)	6(4)	55(4)
0(3)	83(4)	69(5)	93(5)	28(3)	40(3)	24(3)
0(4)	129(7)	56(4)	80(5)	- 9(4)	-14(4)	28(3)
0(5)	91(5)	79(4)	81(5)	-42(4)	-13(4)	36(3)
0(6)	86(6)	85(5)	153(8)	26(4)	23(5)	28(5)
0(7)	114(6)	105(5)	107(5)	49(4)	62(3)	56(3)
C(1)	43(4)	40(3)	38(4)	0(3)	-4(3)	11(2)
C(2)	43(5)	60(4)	43(4)	-6(3)	-2(3)	21(3)
C(3)	42(5)	75(5)	51(5)	1(4)	6(3)	17(3)
C(4)	47(5)	79(5)	52(5)	13(4)	8(3)	19(3)
C(5)	58(5)	48(4)	50(5)	11(3)	13(3)	20(3)
C(6)	101(8)	55(5)	46(5)	24(5)	10(5)	12(4)
C(7)	67(6)	56(5)	53(5)	4(4)	2(4)	8(3)

		Table 3.	- 58 - 2 (cont'	a)		
:	^U 11	U ₂₂	U ₃₃	^U 12	U ₁₃	U ₂₃
C(8)	60(5)	47(4)	41(4)	-4(3)	-8(3)	13(3)
C(9)	78(6)	53(4)	49(5)	-21(4)	-15(4)	20(3)
C(10)	59(6)	78(5)	56(5)	-11(4)	-9(4) ·	36(3)
C(11)	46(5)	68(4)	42(4)	-2(3)	-2(3)	30(3)
C(12)	53(5)	97(5)	66(5)	7(4)	6(3)	49(3)
C(13)	52(5)	92(5)	73(5)	24(4)	17(3)	58(3)
C(14)	43(5)	72(4)	56(4)	21(3)	127(3)	40(2)
C(15)	73(6)	65(5)	42(4)	26(4)	5(4)	27(3)
C(16)	79(7)	55(4)	59(5)	23(4)	22(4)	26(3)
C(17)	57(5)	59 (4)	36(4)	7(3)	3(3)	18(2)
C(18)	62(6)	67(6)	47(5)	-11(4)	-6(4)	15(4)
C(19)	44(5)	75(5)	64(5)	2(4)	3(4)	23(3)
C(20)	40(5)	63(4)	58(5)	9(3)	3(3)	22(3)
C(21)	39(4)	59(4)	42(4)	14(3)	8(3)	24(2)
C(22)	43(4)	45(3)	42(4)	5(3)	3(3)	24(2)
C(23)	34(4)	51(4)	46(4)	9(3)	6(3)	24(2)
C(24)	40(4)	51(3)	44(4)	2(3)	0(3)	22(2)
C(25)	51(5)	41(3)	37(4)	-3(3)	-6(3)	12(2)
C(26)	43(4)	40(3)	39(4)	8(3)	5(3)	15(2)
C(27)	49(5)	64(5)	80(6)	14(3)	15(4)	28(3)
C(28)	65(6)	45(4)	91(6)	-6(4)	0(5)	17(3)
C(29)	41(5)	55(4)	90(6)	-7(3)	0(4)	30(3)
C(30)	41(5)	55(4)	71(5)	5(3)	6(3)	25(3)
C(31)	51(5)	46(4)	53(4)	7(3)	9(3)	18(3)

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Table 3.2 (cont'd)

	^U 11	U ₂₂	U ₃₃	U ₁₂	U ₁₃	U ₂₃
C(32)	63(6)	52(4)	62(5)	10(4)	14(4)	23(3)
C(33)	51(5)	39(3)	40(4)	3(3)	-3(3)	9(3)
C(34)	63(5)	42(4)	48(4)	0(3)	-4(4)	13(3)
C(35)	65(6)	49(4)	55(5)	-1 1(3)	-16(4)	23(3)
C(36)	48(5)	54(4)	67(5)	-2(3)	0(4)	26(3)
C(37)	41(5)	54(4)	49(5)	5(3)	9(3)	17(3)
C(38)	36(4)	43(4)	48(4)	0(3)	4(3)	11 <u>(</u> 3)
C(39)	44(4)	38(3)	47(4)	0(3)	2(3)	15(2)

Complex 2

Br(7)	46(7)	51(7)	67(9)	7(5)	9(5)	12(6)
Br(2)	69(6)	56(5)	93(8)	16(4)	17(5)	15(4)
N(1)	75(7)	98(7)	105(8)	- 5(5)	2(5)	35(5)
N(2)	98(7)	89(6)	62(5)	-2(5)	0(4)	26(3)
0(1)	93(6)	88(6)	145(9)	-18(4)	-27(5)	14(5)
0(2)	62(6)	200(13)	131(9)	0(6)	-7(5)	-2(9)
0(3)	62(4)	89(4)	85(4)	35(3)	22(3)	48(2)
0(4)	106(7)	110(7)	81(6)	-6(5)	- 22(5)	1 0(5)
0(5)	146(9)	93(6)	83(6)	27(6)	14(5)	- 5(5)
C(1)	57(6)	80(5)	46(5)	13(4)	2(3)	27(3)
C(2)	64(7)	119(8)	74(6)	1(5)	8(4)	58(4)
C(3)	72(7)	147(10)	92(8)	39(6)	23(5)	63(5)

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Table 3.2 (cont'd)

	^U 11	U ₂₂	U ₃₃	U ₁₂	^U 13	U ₂₃
C(4)	87(8)	143(10)	91(8)	65(7)	38(5)	58(5)
C(5)	153(12)	68(6)	60(7)	24(7)	-34(6)	18(4)
C(6)	221(19)	89(7)	75(7)	42(9)	-1 5(9)	33(5)
C(7)	164(14)	65(6)	65(6)	10(7)	-22(7)	19(4)
C(8)	74(7)	137(7)	1 52(8)	- 26(5)	-38(5)	117(3)
C(9)	138(14)	205(11)	149(9)	-10(8)	-24(8)	142(4)
C(10)	49(7)	163(10)	134(9)	- 24(5)	-20(5)	99(5)
C(11)	208(19)	156(11)	109(10)	79(11)	40(10)	102(5)
C(12)	197(20)	237(15)	166(13)	76(12)	33(11)	165(6)
C(13)	125(9)	192(11)	130(8)	109(8)	83(5)	118(5)
C(14)	170(13)	143(10)	109(8)	78(9)	75(7)	93(5)
C(15)	346(26)	160(11)	101(9)	119(13)	109(10)	10(5)
C(16)	437(36)	63(7)	49(7)	19(12)	47(10)	8(5)
C(17)	203(15)	76(7)	71(6)	7(8)	49(7)	32(4)
C(18)	162(14)	108(10)	55(7)	-61(10)	-8(8)	21(6)
C(19)	97(10)	191(14)	64(7)	-47(9)	-4(6)	59(5)
C(20)	60(7)	135(8)	57(5)	- 9(5)	0(4)	47(4)
C(21)	54(5)	71(5)	45(4)	10(3)	5(3)	27(3)
C(22)	105(8)	61(5)	37(4)	-5(4)	8(4)	21(3)
C(23)	100(7)	96(6)	92(6)	53(5)	56(4)	66(3)
C(24)	36(5)	133(7)	117(7)	7(4)	9(4)	96(3)
C(25)	64(6)	67(5)	79(6)	-5(4)	-16(4)	44(3)
C(26)	72(6)	61(4)	38(4)	22(4)	0(4)	16(3)
C(27)	35(5)	63(4)	72(5)	17(3)	17(3)	35(3)

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Table 3.2 (cont'd)

	^U 11	U ₂₂	U ₃₃	^U 12	^U 13	U ₂₃
C(28)	50(6)	69(5)	92(6)	-9(4)	-2(4)	32(4)
C(29)	26(5)	87(6)	84(6)	-8(4)	-7(4)	35(4)
C(30)	45(5)	75(5)	85(6)	10(4)	13(4)	35(4)
C(31)	44(5)	67(4)	67(5)	5(3)	8(3)	34(3)
C(32)	46(5)	73(4)	67(5)	21(3)	19(3)	45(3)
C(33)	59(5)	60(4)	54(4)	16(3)	16(3)	31(2)
C(34)	73(6)	62(4)	55(5)	9(4)	14(4)	26(3)
C(35)	74(6)	56(5)	42(5)	-2(4)	5(4)	12(3)
C(36)	57(6)	69(5)	45(5)	-3(4)	-7(3)	22(3)
C(37)	57(5)	64(4)	63(5)	19(3)	14(3)	34(3)
C(38)	29(4)	51(4)	62(4)	8(3)	7(3)	24(2)
C(39)	46(5)	53 (4)	64(4)	9(3)	4(3)	31(2)

Temperature factors assigned to the disordered nitro group.

$$U_{iso}$$
 (x10³).

- N(3) 48
- 0(6) 82
- 0(7) 82
- N(3') 48
- 0(6') 82
- 0(7') 82

Hydrogen atom positions $(x, y, z \times 10^3)$ calculated assuming a C-H distance of 1.09 Å. Each hydrogen atom has the same number as the carbon atom to which it is bound.

Complex 1

	x	У	Z		x	У	Z
H(1)	667	394	630	H(2)	898	457	611
H(3)	1069	389	532	H(4)	1009	257	458
H(6)	823	140	419	H(7)	514	79	410
н(9)	326	81	447	H(10)	152	153	518
H(12)	93	258	623	H(13)	178	380	727
H(15)	369	471	834	H(16)	627	519	891
H(18)	877	497	901	H(19)	1057	414	858
H(20)	969	290	751	H(21)	732	256	670
H(28)	268	-1 6	202	H(30)	54	147	340
H(34)	524	404	472	H(36)	864	331	332

Complex 2

	x	У	z		x	У	Z
H(1)	423	239	153	H(2)	183	204	192
H(3)	66	295	287	H(4)	187	415	353
H(6)	410	5 1 4	384	H(7)	654	547	368

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- 63 -Table 3.3 (cont'd)

	x	У	z		x	У	Z
Н(9)	865	523	298	H(10)	1006	441	234
H(12)	999	304	126	H(13)	898	195	36
H(15)	658	1 59	1032	H(16)	408	82	901
H(18)	145	1 47	904	H(19)	110	282	1024
H(20)	169	323	-18	H(21)	425	377	112
H(28)	288	7	576	H(30)	31	157	719
H(34)	449	397	943	н(36)	843	303	929

Observed Structure Amplitudes and Calculated Structure Factors

-0,1,6	-1 182 -172 0 240 227	7 186 -181 9 173 163	1 226 -107 2 213 240	-7 120 124 -8 91 -80	-4,7,6	-0113.6	-13 215 202 -11 140 152	-2 164 137 -1 296 -249	-\$ 117 -78 -\$ 123 \$2) 12 271 -249 13 115 107	**,7,2
-4 145 150 -7 156 161 -5 124 -133	2 132 -124	14 92 93	9 107 -92 9 131 -191 7 179 176	1 102 126	-15 105 -131 -19 79 -36 -12 113 165	3 70 77 4 288 308 5 113 -150	-10 178 172 -9 92 74 -8 199 150	0 105 -208 1 430 -413 2 639 674	-3 48 -49 -2 47 91 -1 273 -279	14 124 124	-14 116 -118 -11 221 227 -12 162 -111
4 315 423 5 149 -207 4 311 211	5 76 47 6 181 179 7 147 -145		8 106 114 9 189 -199 10 112 144	-7,1+,L -6 18 -119	-10 185 -214	7 103 97 8 104 115 9 71 -71	-6 361 -3.5 -5 646 564 -4 552 -540	-5.10.L	1 277 353 2 197 -179 5 90 52	-15 174 221	-10 110 -110 -1 101 173 -0 235 111 -7 160 -105
7 141 120 8 197 -97 9 195 -175	+ 75 52 -8,10,6	-9 237 234 -8 110 90 -7 314 -315	11 87 71 -7.10,L	-4 107 143 -7,80,L	-7 219 -189 -6 182 -168 -5 265 129	-+.14,L	-3 321 -245 -2 94 147 4 241 354	-5.8.L	6 96 126 7 79 -69 8 96 -149	-12 253 238 -15 268 -275 -8 389 358	-6 270 -344 -6 665 718 -9 161 176
11 05 47 12 65 110 13 152 -197	-13 137 134 -8 160 138	-6 127 -66 -5 526 552 -5 145 -155	-13 100 15	-6 72 -110	-4 161 -137 -3 273 279 -2 165 -136	-14 122 -137 -12 126 137 -10 270 -245	5 479 -442 6 187 130 7 64 35	3 124 -117 9 370 -388 8 186 183	* 138 181 10 64 -1 11 80 -86	-7 201 -145 -6 184 -200 -5 374 -347	-1 2:7 -231 -2 440 -429 -1 167 -167
15 97 115 -412.L	-5 134 121 -5 78 -41 -3 77 128	-2 100 11 4 300 327	-10 105 -73 -9 170 181	-10 72 -44 -10 83 120	0 246 275	-7 102 -110 -6 141 130 -5 130 121	178 139 10 178 -174 12 299 319	10 00 76 11 127 108	-5.15.L	-4 764 721 -3 495 497 -2 250 -264 3 1024-1117	0 2+3 44 1 410 677 2 614 -443 3 724 745
-0 103 -101 -5 110 -05	-2 84 -49 -1 241 -312 0 241 253	7 134 -114 9 246 247 10 289 -289	-5 217 -253 -5 80 60 -1 156 155	-9 62 108 -3 71 -69 -2 69 -83	3 72 +45 6 143 130 7 255 -210	-9 76 78 -2 99 -192 -1 279 255	14 148 -200 17 124 151	-5,*.6	+15 73 97 +17 72 53 +15 79 -75	4 435 -461 5 1104 1018 6 114 91	4 276 284 5 77 -01 6 73 -13
-3 212 206 9 169 -202 5 59 -69	1 •• • 2 109 •1.1 5 122 115	12 125 126	0 169 -138 1 309 -305 2 151 167	-1 45 88 0 40 47	8 154 177 11 80 -00	0 96 89 1 202 -193 3 137 140	-8,3,L .13 244 -240	-10 110 123 -13 132 -122 -11 152 137	+13 141 130 +10 127 -114 -4 304 -313	7 352 -359 8 257 238 9 194 -179	7 77 -72 8 161 181 9 95 135
7 266 231 8 195 -109.	7 134 -133 9 140 148 10 77 -87	-7,4,L	5 113 -97 7 114 105	-7,22,6	-6,0,L -17 95 135 -15 84 -113	5 77 -115 6 163 -193 7 105 191	-10 94 113 -9 127 -1,7 -7 295 -223	-10 114 -122 -9 320 -325 -0 40 -78 -7 147 171	-4 220 144 -7 71 40 -4 340 -410 -5 49 87	10 230 251 12 143 -162 13 169 179	12 142 143
11 120 -129 12 77 92 15 74 84	-0.11,L	-7 107 -103	+ 122 -147 10 88 40 11 101 104	-6.1.L -10 105 108	-14 105 -87 -13 80 89 -12 80 87	0 105 130 9 65 -76 10 71 -69	-5 420 403 -4 314 222 -3 462 -504	-6 453 444 -5 446 -656 -1 227 -244	-4 118 134 -2 47 99 0 81 -57	-1,3,6	-17 115 115
-8,3,L	-13 40 40 -12 75 -67 -6 109 109	-5 329 314 -5 87 -52 -3 289 -310	-7.11,L	-8 149 -111 -7 145 181 -6 80 -51	-11 78 56 -10 100 -100 -9 103 89	-4.15,L	-2 62 52 3 255 267 4 196 247 5 344 -345	-3 461 495 -2 242 217 -1 135 109	1 97 130 3 129 -195 9 90 81	-16 47 -102 -15 248 -319 -13 151 134	-11 462 -448 -10 317 342 -9 142 -123
-7 78 -101 -7 191 224 -6 102 -111	-5 147 131 -9 170 145 -3 137 -133	3 228 275 9 129 145 5 350 -369	-10 149 -154 -9 147 -134 -8 102 -95	-1 110 106 -3 76 -31 -2 116 173	-7 275 -258 -6 146 -138 -5 270 274	-13 124 -136 -12 97 -97 -10 253 242	4 79 -80 7 143 147 8 150 -130	1 260 -278 2 366 415 3 108 121	-5.14,4	-10 +55 -177 -6 202 209 -7 126 125	-7 333 -357 -8 656 -633 -8 756 759
-5 246 -230 -9 76 69 -3 221 245	1 74 62 2 148 -135 7 85 -97	6 76 -30 7 195 -119 8 168 198	-7 164 168 -6 379 369 -5 395 -930	6 444 -472 10 370 397 11 107 -93	-4 117 100 -1 376 -340 0 376 384	-* 177 234 -* 155 -10* -6 208 212	10 88 -103 12 104 820 13 107 -149	4 378 -384 5 195 206 6 131 88	-18 71 97 -17 70 -102 -15 70 -69	-6 70 -92 -5 384 -902 -4 76 76	-3 363 365 -3 172 -173 -2 278 -223
2 272 -287 279 -217 172 -166	-8,12,L	12 149 146	-2 83 -86 -1 111 107 0 75 81	13 141 -160	2 342 -341 3 114 112 4 143 150	-2 112 -118 0 105 105 1 245 -245	•\$,9,L	6 139 137 9 162 -169 10 73 22	-11 116 -135 -9 103 117 -7 156 146	-2 405 -471 2 243 275 4 457 -403	G 265 -218 1 586 596 2 273 -335
10 210 109 12 77 -59 15 125 194	-12 11 14 -1 119 -101 -1 112 137	-13 121 147 -12 116 -127	1 87 -104 2 156 130 3 91 50	-4.2,6	4 104 -98 7 108 -103 8 88 61	2 80 97 3 105 135 8 116 -129 7 70 82	-13 100 200 -12 102 -112 -11 242 -202 -10 245 211	11 184 185 12 98 -124	-6 157 -186 -9 217 243 -3 291 -221 -2 132 104	5 672 642 6 230 236 7 110 35 8 229 720	3 73 -08 4 546 003 5 315 -142 4 225 -218
-8,4,L -7 174 183	1 140 157 2 170 -197 3 78 -72	-10 133 144 -9 176 -147 -8 194 203	6 105 107 6 95 37 9 156 -102	-8 154 -136 -7 159 168 -4 77 79	10 80 -117 -617,L	46 74 7 71 -71	-7 67 68 -8 144 -175 -7 112 -128	-14 137 -139 -13 103 -110	3 151 -149 9 157 149 8 115 -129	9 277 270 11 93 -53 12 274 -317	8 12C 144 9 152 141 10 219 -220
-6 129 115 -5 209 -210 -5 68 -63	4 140 203 7 73 -73	-7 83 -33 -6 246 -240 -5 249 274	11 77 82 -7,12,L	-5 389 -349 -9 335 249 -3 52 17	-13 80 79	-4.16,L	-6 184 195 -5 288 203 -9 150 -236	-11 126 121 -7 214 -220 -8 62 40	-5.17.L	13 302 311 14 211 233 15 (44 -329	11 229 -236 12 188 237 19 143 -125
-2 120 -116 3 287 -367 9 110 119	-5 109 102	-3 165 -79 -2 53 55 -1 161 -176	-13 122 -137 -11 106 •2 •6 113 -62	4 82 -42 7 74 -20 10 111 78	-7 67 37 -6 253 -291 -5 129 -40	-6 105 130 -4 165 -145 -3 89 -64	-2 515 548 2 190 134 4 179 190	-4 307 280 -5 117 -127 -4 430 -414	-17 75 62 -16 73 59 -19 151 -192	-1,0,1	
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Table 3.4 (cont'd)

Table 3.4 (cont'd)

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Table 3.4 (cont'd)

Intermolecular C...C contacts less than 3.5° between the hexahelicene and ETNF molecules. Standard deviations are in parentheses.

(a) Between hexahelicene (Complex 2) and BTNF (Complex 1).

- C(1)C(38)3.425(16)C(3)C(32)3.268(23)C(2)C(31)3.272(21)C(5)C(34)3.463(20)
- (b) Between hexabelicene (Complex 1) and ETNF (Complex 1).
 - C(1)C(34)3.390(13)C(4)C(36)3.489(17)C(2)C(35)3.401(14)C(7)C(39)3.464(15)C(3)C(35)3.472(15)C(9)C(31)3.455(16)

(c) Between hexahelicene (Complex 1) and BTNF (Complex 2).

C(13) C(32)	3.380(19)	C(17) C(35)	3.347(16)
C(14) C(32)	3.471(17)	C(18) C(35)	3.385(17)
c(15) c(34)	3.431(18)	C(19) C(36)	3.497(17)
c(16) c(34)	3.333(18)	C(20) C(36)	3.444(15)
C(17) C(34)	3.456(16)	C(21) C(37)	3.436(16)

(d) Between hexahelicene (Complex 2) and BTNF (Complex 2).

 $C(18) \dots C(32) \quad 3.291(21) \quad C(19) \dots C(32) \quad 3.257(22)$ $C(21) \dots C(34) \quad 3.379(16)$

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Bond lengths (A), with standard deviations in parentheses.

	Complex 1	Complex 2
C(1) - C(2	1.385(12)	1.426(16)
C(2) - C(3) 1.387(13)	1.341(19)
C(3) - C(4) 1.360(13)	1,252(21)
C(4) - C(5) 1.386(14)	1.468(22)
C(5) - C(6	1. 439(12)	1.338(18)
C(6) - C(7	1.333(15)	1.284(28)
C(7) - C(8	1.438(13)	1.392(21)
C(8) - C(9	1.443(13)	1.344(25)
C(9) - C(10) 1.341(15)	1.261(27)
C(10) - C(1	1) 1.412(11)	1. 400(23)
C(11) - C(1	2) 1.416(14)	1.349(35)
C(12) - C(1	3) 1.351(13)	1,241(29)
C(13) - C(1	4) 1.391(12)	1.449(26)
C(14) - C(1	5) 1.436(11)	1.317(25)
C(15) - C(1	6) 1.340(14)	1. 433(43)
C(16) - C(1	7) 1.418(14)	1.561(32)
C(17) - C(1	8) 1.418(13)	1.411(28)
C(18) - C(1	9) 1.385(15)	1.194(28)
C(19) - C(2	1.385(11)	1.470(19)
c(20) - c(2	1) 1.360(11)	1.338(15)

	• / • •		
	Table 3.6 (cont'd)		
:	Complex 1	Complex 2	
C(21) - C(22)	1.420(12)	1.425(16)	
C(22) - C(17)	1.414(9)	1.471(15)	
C(22) - C(23)	1.471(11)	1.444(18)	
C(23) - C(14)	1.405(12)	1.399(24)	
C(23) - C(24)	1.443(9)	1.378(15)	
C(24) - C(11)	1,421(11)	1.543(26)	
C(24) - C(25)	1.418(11)	1.451(16)	
C(25) - C(8)	1.401(9)	1.480(16)	
C(25) - C(26)	1.451(11)	1.430(15)	
C(26) - C(5)	1.439(12)	1.463(16)	
C(26) - C(1)	1.395(10)	1.391(13)	
Br(1) - C(27)	1.885(10)	1.874(9)	
Br(2) - C(37)		1,903(12)	
N(1) - C(29)	1,506(12)	1.497(12)	
N(1) = O(1)	1.190(13)	1.189(14)	
N(1) - O(2)	1.174(14)	1.206(16)	
N(2) - C(35)	1,502(11)	1,500(11)	
N(2) - 0(4)	1.216(12)	1,207(16)	
N(2) - 0(5)	1.189(13)	1,221(17)	
N(3) - C(37)	1.531(11)		
N(3) - O(6)	1.082(13)		
N(3) - 0(7)	1,159(12)		
0(3) - C(32)	1,215(13)	1,181(12)	
C(27) - C(28)	1.367(13)	1.411(11)	
C(28) - C(29)	1.332(14)	1.371(14)	

	Table 3.6 (cont'd)	
	Complex 1	Complex 2
C(29) - C(30)	1.375(11)	1.362(14)
C(30) - C(31)	1.369(11)	1.370(11)
C(31) - C(32)	1.498(10)	1,498(12)
C(32) - C(33)	1.433(13)	1.460(12)
C(33) - C(34)	1,369(10)	1.377(11)
C(34) - C(35)	1.375(14)	1.357(15)
C(35) - C(36)	1.363(13)	1.377(14)
C(36) - C(37)	1.403(11)	1.387(11)
C(37) - C(38)	1.381(12)	1,382(12)
C(38) - C(33)	1.423(10)	1.417(12)
C(38) - C(39)	1.471(10)	1.472(10)
C(39) - C(31)	1.398(12)	1.393(13)
C(39) - C(27)	1.398(12)	1.407(11)
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Bond angles (degrees), with standard deviations in parentheses.

					Comp	lex 1	Co	omplex 2
C(26)	-	C(1)	-	C(2)	121	6(0.7)	1	21.4(0.9)
C(1)		C(2)	-	C(3)	120,	7(0.8)	,	21.3(1.2)
C(2)	-	C(3)	-	C(4)	119,	1(0.9)	4	20.3(1.4)
C(3)	-	C(4)	-	C(5)	121,	.9(0 . 9)	1	24.8(1.3)
C(4)	-	C(5)	-	C(6)	120,	,0(0.7)	1	16.4(1.0)
C(26)		C(5)	-	C(6)	118	3(0.8)	1	19.3(1.5)
C(4)	-	C(5)	-	C(6)	121,	5(0.9)	1	23.9(1.4)
C(5)	-	C(6)	-	C(7)	121,	4(1.0)	1	20.9(1.6)
C(6)	-	C(7)	-	C(8)	120,	7(0.8)	1	25.7(1.2)
C(7)	-	C(8)	-	C(25)	120,	7(0.8)	1	18.8(1.2)
C(25)	-	C(8)	-	C(9)	120,	7(0.8)	1	15.8(1.4)
C(7)	-	C(8)	-	C(9)	118	6(0.7)	4	25.5(1.4)
C(8)	-	C(9)		C(10)	118,	2(0.8)	1	24.1(1.9)
C(9)	•••	C(10)	-	C(11)	121,	8(0.8)	1	24.1(1.6)
C(10)	-	C(11)	-	C(24)	119	7(0.8)	1	18.8(1.8)
C(24)	-	C(11)	-	C(12)	120,	8(0.7)	1	104.9(1.6)
C(10)	-	C(11)	-	C(12)	119	5(0.8)	1	36.4(2.2)
C(11)	-	C(12)	-	C(13)	119.	3(0.8)	1	38.1(2.5)
C(12)	-	C(13)	-	C(14)	121.	5(0 . 9)	1	14.2(2.1)
C(13)	-	c(14)	_	C(23)	120	1(0.7)	1	20.7(1.4)

- 72 -Table 3.7 (cont'd)

	Complex 1	Complex 2
C(23) - C(14) - C(15)	120.0(0.7)	116.0(2.1)
C(14) - C(15) - C(16)	121.4(0.9)	131.3(2.5)
C(15) - C(16) - C(17)	120.7(0.8)	114.0(1.4)
C(16) - C(17) - C(22)	120.0(0.7)	112.9(1.6)
C(22) - C(17) - C(18)	118,5(0,8)	118.0(1.4)
C(17) - C(18) - C(19)	121.4(0.8)	125.9(1.3)
C(18) - C(19) - C(20)	118.4(0.8)	120 . 5(1.5)
C(19) - C(20) - C(21)	122.7(0.9)	117.9(1.4)
C(20) - C(21) - C(22)	119.8(0.7)	123.8(0.9)
C(21) - C(22) - C(17)	118.9(0.7)	113.7(1.2)
C(17) - C(22) - C(23)	118.8(0.7)	123.3(1.2)
C(21) - C(22) - C(23)	122.2(0.6)	123.0(0.8)
C(22) - C(23) - C(14)	117.3(0.6)	119.9(1.1)
C(14) - C(23) - C(24)	118.6(0.7)	115.7(1.3)
C(22) - C(23) - C(24)	124.1(0.7)	123.9(1.2)
C(23) - C(24) - C(11)	115.9(0.7)	123.2(1.2)
C(11) - C(24) - C(25)	117.4(0.6)	108.6(1.0)
C(23) - C(24) - C(25)	126.7(0.7)	128.1(1.0)
C(24) - C(25) - C(8)	118.6(0.7)	123.3(1.1)
C(8) - C(25) - C(26)	117.0(0.7)	112.9(1.0)
C(24) - C(25) - C(26)	124.0(0.6)	123.8(0.8)
C(25) - C(26) - C(5)	119.6(0.6)	121.5(0.9)
C(5) - C(26) - C(1)	116.5(0.7)	115.5(1.0)
C(25) - C(26) - C(1)	123.8(0.7)	122.9(0.9)
C(39) - C(27) - C(28)	118,5(0,9)	120.6(0.8)

- 73 -Table 3.7 (cont'd)

	Complex 1	Complex 2
C(27) - C(28) - C(29)	121,6(0,8)	116.5(0.9)
C(28) - C(29) - C(30)	123.3(0.8)	125.4(0.8)
C(29) - C(30) - C(31)	114.3(0.8)	116.1(0.9)
C(30) - C(31) - C(39)	124.8(0.7)	123.7(0.8)
C(39) - C(31) - C(32)	107.8(0.7)	109.1(0.7)
C(30) - C(31) - C(32)	127.1(0.8)	126.9(0.9)
C(31) - C(32) - C(33)	106.5(0.8)	104.7(0.8)
C(32) - C(33) - C(38)	108.9(0.6)	109.5(0.6)
C(38) - C(33) - C(34)	122.2(0.8)	123.0(0.9)
C(32) - C(33) - C(34)	128.4(0.8)	127.4(0.9)
C(33) - C(34) - C(35)	117.2(0.8)	116.6(0.9)
C(34) - C(35) - C(36)	124.4(0.8)	124.4(0.8)
C(35) - C(36) - C(37)	117.0(0.9)	116.8(0.9)
C(36) - C(37) - C(38)	122.0(0.8)	122.7(0.9)
C(37) - C(38) - C(3 3)	116.9(0.7)	115.8(0.7)
C(33) - C(38) - C(39)	107.9(0.7)	107.7(0.7)
C(37) - C(38) - C(39)	135.0(0.7)	136.3(0.8)
C(38) - C(39) - C(31)	108.0(0.6)	107.7(0.7)
C(31) - C(39) - C(27)	116.2(0.7)	116.7(0.7)
C(39) - C(27) - Br(1)	122.3(0.6)	122.5(0.6)
Br(1) - C(27) - C(28)	118.8(0.8)	116.8(0.7)
C(28) - C(29) - N(1)	119.8(0.8)	113.5(0.9)
C(29) = N(1) = O(1)	115.6(1.0)	119.3(1.0)

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Table 3.7 (cont'd)

			Complex 1	Complex 2
C(29)	- N(1)	- 0(2)	119.0(0.8)	115.0(1.0)
0(1)	- N(1)	- 0(2)	125.4(1.0)	125.6(1.1)
N(1)	- C(29)	- C(30)	116.6(0.8)	121.2(0.9)
C(31)	- C(32)	- 0(3)	125.2(0.9)	127.5(0.8)
0(3)	- C(32)	- C(33)	128.3(0.7)	127.8(0.8)
C(34)	- C(35)	- N(2)	119.6(0.8)	118.5(0.9)
C(35)	- N(2)	- 0(4)	115.7(0.9)	116.8(1.0)
C(35)	- N(2)	- 0(5)	117.7(0.8)	115.7(1.0)
0(4)	- N(2)	- 0(5)	126.5(0.8)	127.4(1.0)
N(2)	- C(35)	- C(36)	116.0(0.9)	117.0(0.9)
C(36)	– C(37)	- N(3)	114.0(0.8)	
C(37)	- N(3)	- 0(6)	116.7(0.8)	
C(37)	- N(3)	- 0(7)	111.1(0.8)	
0(6)	- N(3)	- 0(7)	131.8(1.1)	
N(3)	– C(37)	- C(38)	128.3(0.6)	
C(36)	- C(37)	- Br(2)		113.8(0.7)
Br(2)	- C(37)	- C(38)		123.4(0.6)

Comparison of the mean observed bond lengths (D_{obs}) in the Complex 1 hexabelicene molecule with those obtained from valence-bond $(D_{v.b.})$ and molecular-orbital $(D_{m.o.})$ calculations assuming a planar structure. All bond lengths are in \mathring{A} , and the atom numbers are those given in Figure 3.1.

Bo	ond	D V.b.	D m.o.	D obs.
1	- 2	1.38	1.39	1.37
2	- 3	1.42	1.41	1.39
3	- 4	1.38	1.39	1.37
4	- 5	1.42	1.41	1.40
5	- 6	1.45	1.42	1.43
6	- 7	1.35	1.38	1.34
7	- 8	1.45	1.42	1.44
8	- 9	1.44	1.42	1.42
9	-10	1.36	1.38	1.35
10	-11	1.44	1.41	1.42
11	-24	1.39	1.42	1.42
24	-25	1.44	1.42	1.43
25	-26	1.45	1.43	1.46
26	- 1	1.42	1.41	1.41
25	- 8	1.38	1.41	1.40
26	- 5	1.41	1.41	1.41

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Mean planes through the aromatic rings of the hexahelicene molecules, together with the root mean square and maximum deviations of the atoms from the planes (Å). The planes are defined by the equation AX' + BY'+ CZ' = D, where X', Y', and Z' are absolute orthogonal coordinates (in Å), with $X' = axsin\beta sin\gamma^*$, $Y' = -axsin\beta cos\gamma^* + by sind$, $Z' = axcos\beta$ + by cosa.

Ring	Complex	Devia	tions	Equation	n of pla	ne coeff	icients
		r.m.s.	max.	A	B	C	D
1	1	0.015	0.022	-0.471	0.175	-0.865	-8.810
1	2	0.016	0.025	-0.462	0.274	-0.843	-1.251
2	1	0.058	0.097	-0.392	0.339	-0.855	-7. 648
2	2	0.039	0.066	-0.373	0.400	-0.837	-0.081
3	1	0.074	0.115	-0.205	0•472	-0.858	-6.420
3	2	0.093	0.144	-0.172	0•449	-0.877	1.447
4	1	0.078	0.123	0.016	0 .5 35	-0.845	-5.331
4	2	0.072	0.124	-0.087	0 . 411	-0.907	3.083
5	1	0.055	0.085	0.210	0.489	-0.847	-4.887
5	2	0.064	0.107	0.299	0.312	-0.902	4.014
6	1	0.024	0.033	0.342	0.342	-0.875	-5.283
6	2	0.020	0.030	0.388	0.173	-0.905	3.882

Dihedral angles (degrees) between the mean planes through the aromatic rings of the hexahelicene molecules.

Between	rings:	Complex	Angle
1 and	2	1	10.5
1 and	2	2	8.8
2 and	3	1	13.2
2 and	3	2	12.1
3 and	A	1	13.2
3 and	4	2	15.1
4	, E	4	11 4
4 and 4 and	5	2	13.5
5 and 5 and	6 6	1 2	11•4 9•5

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Intramolecular non-bonded C...C contacts $(\stackrel{\circ}{A})$ in the hexabelicene molecules, with standard deviations in parentheses.

Contact	Complex 1	Complex 2
C(1) C(22)	2.966(13)	2.942(15)
C(1) C(23)	3.090(12)	3.029(18)
C(1) C(21)	3.046(14)	3.039(17)
C(21) C(26)	2.966(13)	3.015(14)
C(21) C(25)	3.075(11)	3.099(14)

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Mean planes through the aromatic rings and C-nitro groups of the BTNF molecules, together with the root mean square deviations (Δ) of the atoms from the planes. The planes are defined by the equation AX' + BY' + CZ' = D, where X', Y', and Z' are absolute orthogonal coordinates (in A), with $X' = axsin\beta sinY'', Y' = -axsin\beta cosY'' +$ $bysing, Z' = axcos\beta + bycosg + cz_o$

Plane	Complex	$\Delta(\overset{\circ}{\mathbb{A}})$	Equatio	n of pla	ne coef	ficients
			A	В	С	D
Ring 1	1	0.043	-0.239	0.233	-0.943	-4.283
Ring 1	2	0.038	0.002	0.479	-0.876	-9.397
Ring 2	1	0.039	-0.325	0.318	-0.891	-4.088
Ring 2	2	0.032	0.148	0.394	-0.907	- 9•757
Ring 3	1	0.019	-0.438	0.310	-0.844	-4.416
Ring 3	2	0.029	0.291	0.326	-0.900	- 9•377
C(29)-NO2	1	0.001	-0,250	0.325	-0.912	-4.008
C(29)-NO2	2	0.008	0.004	0.390	- 0.921	-10.133
C(35)-NO2	1	0.007	-0.425	0.278	-0.861	-4.600
C(35)-NO2	2	0.010	0.314	0.271	-0.910	-9.648
C(37)-NO2	1	0.017	0.300	0 .7 08	-0.640	2.129
C(37)-NO2	2	0.013	- 0 . 159	-0.174	-0.972	-14.658

Dihedral angles (degrees) between the mean planes of the aromatic rings and C-nitro groups of the BTNF molecules.

Planes	Dihedral	angle
	Complex 1	Complex 2
Ring 1 - Ring 2	7.5	7.1
Ring 2 - Ring 3	7.1	9.1
C(29)-NO ₂ - Ring 1	5.5	6.4
C(35)-NO ₂ - Ring 3	2.5	2.9
C(37)-NO ₂ - Ring 3	51.1	39•4









Figure 3.2: The crystal structure projected along the <u>a</u>*axis. The complex 1 and 2 molecules are labelled(1)and(2)respectively.



зÅ 0

Figure 3.3: The Complex 1 hexahelicene molecule viewed along \underline{a}^* , showing the shortest intramolecular contacts.

CHAPTER 4

THE CRYSTAL AND MOLECULAR STRUCTURES OF THE 'SUPER-ACID' SALTS

POTASSIUM TRI-HYDROGEN DI-SUCCINATE AND POTASSIUM TRI-HYDROGEN DI-GLUTARATE

4.1. Introduction

The acid salts of carboxylic acids

Many monobasic carboxylic acids readily form crystalline acid salts of composition \underline{MHX}_2 , where \underline{M} is a univalent cation, and \underline{HX} is the free acid (R.COOH). It has been shown, as a result of x-ray and neutron diffraction studies of a number of these acid salts, that they can be classified into two structural types, \underline{A} and \underline{B} .¹ In type \underline{A} the two acidic residues are equivalent, linked by a very short $0\cdots H\cdots 0$ bond across a crystallographic element of symmetry, and the structure may be formulated as $\underline{M}^+(\underline{XHX})^-$. Crystals of this type of acid salt have anomalous infra-red spectra,² the most notable features being the absence of an 0-H stretching band above 1700 cm⁻¹, and a broad band of absorption below 1600 cm⁻¹.

Type <u>B</u> acid salts have crystal structures in which the crystallographically distinct anion \underline{X}^{-} and free acid <u>HX</u> can be recognised, so that the structure may be formulated as $\underline{M}^{+} \cdot \underline{X}^{-} \cdot \underline{HX}$. The acid residues are joined by a short hydrogen bond, but in this case the oxygen atoms involved arc not symmetry-related. The infra-red spectra of Type <u>B</u> acid salts approximate to a superposition of the spectra of the free acid and its anion.

Dicarboxylic acids $(H_2\underline{Y})$ form acid salts $(MH\underline{Y})$ which can also be classified into two structural types. Type \underline{A}_2 acid salts, in which the two carboxyl groups are crystallographically equivalent, each being effectively half-ionised, are analogous to Type \underline{A} acid salts of monobasic carboxylic acids and have the same type of anomalous infra-red spectra. In Type \underline{B}_2 salts, the carboxyl groups are differentiated, one being ionised, the other not; this type is thus analogous to Type \underline{B} acid salts of monobasic carboxylic acids, and has a similar infra-red spectrum.

In addition to the normal Type \underline{A}_2 and \underline{B}_2 acid salts, dicarboxylic acids form 'super-acid' salts of stoichiometric formula $\underline{M}\underline{H}_2\underline{Y}_2$. The crystal structures of the first two members of the series of super-acid salts $\underline{K}\underline{H}_2\underline{Y}_2$, potassium tetroxalate³ and potassium trihydrogen dimalonate have been investigated by neutron diffraction; as expected (on the basis of their infra-red spectra), both structures contain the unionised acid molecule $\underline{H}_2\underline{Y}$ and the \underline{B}_2 Type acid anion $\underline{H}\underline{Y}$. Their structures can thus be more correctly formulated as $\underline{K}^+ \cdot \underline{H}\underline{Y}^- \cdot \underline{H}_2\underline{Y}$. The structure analyses by neutron diffraction of the next two members of the series, potassium tri-hydrogen di-succinate and potassium tri-hydrogen di-glutarate are now described in parts two and three respectively of this chapter.

4.2. The Crystal Structure of Potassium tri-hydrogen di-succinate

4.2.1. Introduction

Potassium tri-hydrogen di-succinate (KH_3Succ_2) was first described by Marshall and Cameron in 1907⁵ who studied its morphology during an investigation into crystals with curved boundaries.

Its preparation is simple: equimolar quantities of succinic acid

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and potassium hydroxide are dissolved in warm water, and crystals of KH3Succ2 separate out on cooling or evaporation. However, although large crystals suitable for neutron diffraction were relatively easy to grow, considerable difficulty was encountered in obtaining small crystals suitable for x-ray analysis - they tended to be split or bent. A full set of neutron diffraction data were therefore collected in the hope that the structure might be solved directly from neutron data. Since potassium is no longer a 'heavy atom' for neutron scattering, an attempt was made to solve the structure by the symbolic addition method, in spite of theoretical objections that the presence of a large number of negativelyscattering hydrogen nuclei make its application invalid. However, the anticipated difficulties were not encountered, and the structure was solved at the first attempt.

4.2.2. Experimental

Crystal Data

The unit-cell parameters were determined from x-ray photographs: $C_8H_{11}O_8K, \underline{M} = 2743$, monoclinic, <u>a</u> = 7.434(5), <u>b</u> = 18.437(10), <u>c</u> = 9.006(5)Å, = 109.51(0.1)^o; <u>U</u> = 1163.5Å³, <u>D</u>_m (Marshall and Cameron, 1907) = 1.559, <u>z</u> = 4, <u>D</u>_c = 1.56. Space group, P₂₁/c (No. 14).

The goniometric parameters given by Marshall and Cameron correspond to a different choice of axes: $\underline{a}_{G} = -\underline{a}-2\underline{c}$; $\underline{c}_{G} = \underline{a}$. These lead to the ratios 0.923:1:0.403, 94.7° compared with 0.936:1:0.407, 94.4° cited by Groth.

Data Collection

Diffracted neutron intensities were measured on a Ferranti Mark II automatic diffractometer attached to the Dido reactor at A.E.R.E. (Harwell), using a monochromated neutron beam with $\lambda = 1.172$ Å. The crystal used had dimensions 5.5(parallel to <u>c</u>) x 5 x 3.5 mm³ and was mounted along <u>c</u>. Integrated intensities were measured for all 1890 independent reflections out to $\theta = 45^{\circ}$ using w/20 scans; of these, 1213 with $|F| \ge 36(|F|)$ were used in the structure analysis. Absorption corrections were applied to all the data using a calculated μ (effective) of 1.40 cm⁻¹; the incoherent scattering cross-section of hydrogen was taken to be 37.0 x 10⁻²⁴ cm.

Normalised structure amplitudes (E 's) were calculated from the observed structure amplitudes according to the equation

$$E^{2} = k^{2} F^{2}_{obs} / e^{-2B(\sin\theta/\lambda)^{2}} \sum_{j=1}^{N} b_{j}^{2}$$

where b_j is the scattering length of the jth atom, and N is the number of atoms in the unit cell. The values of the scale factor k and overall temperature factor B were obtained as follows: the summation of $(E^2-1)^2$ over all reflections was calculated for various physically reasonable values of B, the value of k being adjusted so that the average value of E^2 was forced to be 1.0. The best value of B, and hence k, was taken to be that which minimised the summation $(E^2-1)^2$. These calculations were carried out using the X-RAY SYSTEM program DATFIX; all subsequent programs used in the structure analysis were also from the X-RAY SYSTEM.

4.2.3 Solution of the phase problem.

The phase problem was solved by an application of the symbolic addition method using the programs SIGMAZ and PHASE, 1,801 Σ_2 relationships were generated by SIGMA2 between the 224 reflections with |E| values greater The reflections 621, 517, and 438 were allocated positive signs than 1.5. in order to define an origin before proceeding with the phase determination using the program PHASE. This program finds an initial solution in terms of the top 30-40 percent E 's - in this case 80 were used - which are known as 'generators'. The subset of Σ_2 relationships used in this solution - known as the 'defining' subset - are then tested against the full set of relationships and a count is made of the number of times each relationship in the subset appears 'accordant' or 'discrepant' in terms of all the known relationships. Any relationship in the defining subset which appears discrepant more often than accordant can then be removed from the The program thus finds the most internally self-consistent solution. solution. and this is usually, though not always, the correct one. In the present case, the defining subset contained 77 relationships, of which 1 was subsequently removed to yield a consistent solution. The phases of 206 reflections were determined from this solution, and an E-map computed using these phased E's as coefficients revealed every atom in the structure. including the negatively-scattering hydrogens. Structure factors calculated using the atomic coordinates determined from the E-map gave an R-value of 29

per cent.

It was pointed out in Chapter I that application of the symbolic addition method to diffraction data yields phases for the 'squared structure' - that is, the structure which scatters with the square of the scattering factor for each atom in the original structure. Symbolic addition will thus be successful with neutron data from a structure containing a proportion of negatively-scattering nuclei only if the largest structure factors of the original structure have the same phases as the corresponding structure factors of the squared structure (or of the original structure in which all the nuclei are considered positive scatters), and it was argued that this was likely to be the case when only a moderate proportion of the nuclei were negative scatterers.

Having successfully solved the structure by the symbolic addition method, it was decided to investigate the extent of the agreement between the phases of the original structure and that of the same structure with positively scattering hydrogen nuclei. Structure factors were calculated from the final least-squares parameters using a positive sign for the hydrogen scattering length, and Table 4.2.11. lists these structure factors (F_b^+) for the 80 reflections used in the initial symbolic addition solution along with their structure factors calculated using the correct (negative) hydrogen scattering length (F_b^-) . Although the amplitudes of each pair of F_b^+ and F_b^- sometimes differ by a large amount, their phases are, without exception, the same, and of the 206 reflections used in the final solution, only 2 have different signs for F_b^+ and F_b^- . Any errors in the phases determined by the symbolic addition procedure are thus most likely to be the result of differences in the amplitudes of F_b^- and F_b^+ ; not all of the large F_b^- 's correspond to a large F_b^+ , and since only reflections with a large F_b^+ should theoretically be used in the symbolic addition procedure, the reflections for which $F_b^+ << F_b^-$ have been wrongly (but unavoidably) included. Phases determined for such reflections have a low probability of being correct, and in 8 of the ll phases which were incorrectly determined in the present analysis (Table 4.2.12), F_b^+ is much smaller than F_b^- (by 50 per cent or more). This 'amplitude error' effect was not, however, important in this case, since only one of these 'invalid' reflections was among the set of 80 largest reflections from which the initial solution was found.

The proportion of hydrogen scattering power in potassium tri-hydrogen di-succinate is 20 per cent; obviously, neutron data derived from crystals containing increasing proportions of negative scattering nuclei will suffer to an increasing extent from the 'amplitude error' effect amongst the largest structure factors, and the point at which the symbolic addition procedure becomes unworkable is reached, according to Sikka⁷ when negativescattering nuclei account for more than 1/3 of the total scattering power in the unit cell.

4.2.4 Refinement.

The structure was refined by least-squares using the program CRYLSQ.

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Nuclear scattering lengths were taken to be 0.35, 0.661, 0.579 and -0.378×10^{-12} cm. for K, C, O and H respectively. Two cycles of fullmatrix isotropic least-squares refinement were followed by three cycles of block-diagonal anisotropic least-squares refinement, and convergence was reached with R = QO86. The weighting scheme used in the last two cycles is defined by the equation $W^{-1} = 1 + [(F_0 - 5.0)/3.0].^2$ Seven reflections which seemed to be badly affected by extinction were omitted from the final stages of refinement, and these are listed in Table 4.2.5.

The final positional and vibrational parameters are listed in Tables 4.2.1 and 4.2.2 respectively; the observed structure amplitudes and calculated structure factors are listed in Table 4.2.3 and an analysis of their agreement is given in Table 4.2.4.

4.2.5 Discussion of the structure

The numbering scheme of the crystal-chemical unit (C.C.U.) is shown in Figure 4.2.1; other symmetry-related units needed in the description of the structure are as follows :-

I	-l+ <u>x</u> , <u>y</u> , <u>z</u>	IV	1+x, y, $1+z$
II .	- <u>x</u> , - <u>y</u> , - <u>z</u>	¥	<u>x, y</u> , l+ <u>z</u>
III	-x, -y, 1-z	VI	1- <u>x</u> , - <u>y</u> , 1- <u>z</u>

The principle bond-lengths and angles in the succinate residues are given

in Table 4.2.6. Figures 4.2.2 and 4.2.3 show the crystal structure projected along the <u>b</u> and <u>c</u> axes respectively.

The two independent succinate residues are clearly differentiated, residue R_1 being the acid anion $H\underline{Y}^-$ and residue R_2 the neutral acid molecule $H_2\underline{Y}$. The location of the hydroxylic protons identifies the carboxyl based on C(4) as the carboxylate anion and this is confirmed by a comparison of the differences in C-O bond length and C-C-O angle in the four carboxyl groups (Table 4.2.7). The unionised carboxyls have larger differences in both C-O distance and C-C-O angle than the carboxylate anion.

The main features of the structure are most clearly observed in Figure 4.2.2. The structure consists of infinite chains of the <u>B</u>₂ type residues (R₁) linked head-to-tail along the x-direction by short asymmetric hydrogen bonds, with the neutral acid molecules R₂ attached as festoons: each O(3) atom of the main chain forms a short asymmetric hydrogen bond with O(5)-H of one R₂ residue, and with O(7)-H of the next.

The R_1 residue is in an extended form and its four carbon atoms are coplanar, their mean plane being represented by the equation :

0.2471X' + 0.8461Y + 0.4723Z' = 1.843 Å;

the root mean square distance of the four atoms from the plane is 0.017 Å. Whereas the R_1 residues fit seven atoms into a primitive translation of 7.43 Å, the R_2 residues have to fit nine atoms into this distance, and in order to allow this, one carboxyl group is in a gauche conformation, with a dihedral angle of 57.3° about C(6) - C(7). A list of the other important torsion angles in the succinate residues is given in Table 4.2.9.

The interatomic distances and angles in the three hydrogen bonds are given in Table 4.2.10. The $O(1) - H \cdots O(4^{I})$ and $O(5) - H \cdots O(3^{I})$ bonds are of similar length, but consideration of their $0 - H \cdots O$ angles and $H \cdots O$ distances suggests that the former is the stronger bond. The other hydrogen bond is significantly longer, and its $0 \cdots 0$ distance of 2.63 Å is similar to those found in carboxylic acid dimers.

Figure 4.2.4 shows the Nakamoto-Margoshes-Rundle relationship⁸ between 0 - H and $0 \cdot \cdot \cdot 0$ distances in hydrogen bonds; the curve is that of Hamilton and Ibers⁹ representing the best least-squares fit to the 0 - H and $0 \cdot \cdot \cdot 0$ distances of all the $0 - H^{\bullet \cdot \cdot \cdot 0}$ hydrogen bonds studied by neutron diffraction up to 1967, and shows how the 0 - H distance tends to increase with decreasing $0 \cdot \cdot \cdot 0$ distance. The six points representing the hydrogen bonds in the present analysis and those in potassium tri-hydrogen di-glutarate (Chapter IV, part 3) are plotted in Figure 4.2.4 and fit the Hamilton-Ibers curve very well, considering the average standard deviation in the 0 - Hdistances of about 0.016 Å.

The C - H distances have a mean value of 1.089 Å, with an internal standard deviation of 0.025 Å, which suggests that their least-squares standard deviations in Table 4.2.6 are underestimated.

The environment of the potassium ion is shown in Figure 4.2.5. Eight oxygen atoms surround the ion and the six $K^+ \cdots 0$ distances less than 2.84 Å

must be genuine ionic contacts; the two $K^+ \cdots 0$ distances of 3.19 Å and 3.28 Å are, however, questionable contacts, although they appear to fill gaps in the environment provided by the other six oxygen atoms. The $K^+ \cdots 0$ distances are listed in Table 4.2.10 along with the 28 $0 \cdots K^+ \cdots 0$ angles.

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TABLES AND DIAGRAMS

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Fractional coordinates $(\underline{x}, \underline{y}, \underline{z})$ and absolute orthogonal coordinates (in $\overset{0}{A}$ with $X' = \underline{ax}\sin\beta$, $\underline{Y} = \underline{by}$, $\underline{Z}' = \underline{ax}\cos\beta + \underline{cz}$, and with standard deviations in parentheses).

	<u>x</u>	<u> </u>	Z	<u>x</u> '	<u>¥</u>	<u>Z</u>
K+	0.2696	0.0047	0.6076	1.889(9)	0.087(9)	4.802(9)
0(1)	-0.0790	0.0813	0.0640	-0.554(6)	1.498(7)	0.772(6)
0(2)	0.0391	0.0442	0.3126	0.274(6)	0.815(9)	2.718(7)
0(3)	0.4650	0.1209	-0.1248	3.258(6)	2.229(9)	-2.287(7)
0(4)	0.6083	0.0750	0.1123	4.263(6)	1.323(7)	-0.499(6)
0(5)	-0.3209	0.1740	-0.2709	-2.248(8)	3.207(7)	-1.643(7)
0(6)	-0.4503	0.0887	-0.4507	-3.156(7)	1.634(6)	-2.941(6)
0(7)	0.1977	0.2120	-0.2836	1.385(8)	3.908(9)	-3.045(9)
0(8)	0.0225	0.1157	-0.3843	0.158(8)	2.133(7)	-3.517(10)
C(1)	0.0628	0.0626	0.1912	0.440(5)	1.155(5)	1.566(5)
C(2)	0.2547	0.0632	0.1722	1.785(5)	1.165(5)	0.919(5)
C(3)	0.2653	0.1022	0.0276	1.859(5)	1.884(6)	-0.410(6)
C(4)	0.4574	0.0987	0.0073	3.205(4)	1.819(5)	-1.070(5)
C(5)	-0.3664	0.1466	-0.4131	-2.568(5)	2.702(5)	-2.811(5)
C(6)	-0.3051	0.1927	-0.5241	- 2.138(5)	3.552(6)	-3.963(5)
C(7)	-0.1172	0.2328	-0.4480	-0.821(5)	4.292(5)	-3.743(6)
C(8)	0.0401	0.1805	-0.3702	0.281(6)	3.328(6)	-3.433(6)
H(1)	-0.2047	0.0798	0.0840	-1. 434(9)	1.471(11)	1.264(10)
H(2)	-0.3841	0.1466	-0.2073	-2.691(12)	2.702(12)	-0.913(12)

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Table 4.2.1 (cont'd)

	x	<u>y</u>	<u>Z</u>	<u>x</u> '	<u>¥</u>	<u>z</u> '
H(3)	0.2931	0.1743	-0.2297	2.054(12)	3.213(15)	-2.797(13)
H(4)	0.2997	0.0063	0.1705	2.086(15)	0.115(15)	0.796(18)
H(5)	0.3549	0.0854	0.2799	2.486(12)	1.572(20)	1.641(11)
H(6)	0.1647	0.0807	-0.0725	1.154(12)	1.488(21)	-1.062(12)
H(7)	0.2349	0.1603	0.0349	1.646(17)	2.955(15)	-0.269(19)
H(8)	-0.4191	0.2314	-0.5777	-2.937(13)	4.266(15)	-4.162(14)
H(9)	-0.3031	0.1589	-0.6233	-2.124(18)	2.924(17)	-4.861(13)
H(10)	-0.0818	0.2646	-0.5346	-0.573(16)	4.878(17)	-4.612(17)
H(11)	-0.1311	0.2714	-0.3555	-0.918(16)	5.004(13)	-2.876(17)

11.5

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Vibrational parameters $(\overset{o2}{A} \times 10^4)$

	<u>U</u> 11	<u>U</u> 22	<u>U</u> 33	<u>U</u> 12	<u>U</u> 13	<u>U</u> 23
К +	168(37)	252(44)	119(40)	98(32)	67(34)	106(32)
0(1)	134(25)	566(38)	238(29)	46(24)	121(24)	138(27)
0(2)	156(28)	910(57)	267(32)	- 42(30)	104(26)	221(35)
0(3)	168(26)	799(50)	3 35(34)	50(28)	167(27)	264(34)
0(4)	106(23)	507(37)	247(29)	73(22)	62(23)	67(26)
0(5)	464(37)	339(31)	354(33)	-216(27)	261(30)	-121(27)
0(6)	385(32)	31 9(30)	221(29)	-144(27)	1107(26)	-53(26)
0(7)	308(35)	578(49)	533(45)	-81(33)	-40(34)	162(39)
0(8)	371(36)	342(36)	750(56)	132(28)	148(38)	- 34(36)
C(1)	104(19)	369(25)	179(22)	-29(18)	89(19)	9(20)
C(2)	92(20)	410(27)	213(24)	6(19)	77(19)	105(21)
C(3)	145(21)	446(29)	292(26)	92(20)	123(21)	181(23)
C(4)	107(19)	316(24)	282(25)	20 (1 8)	120(19)	54(21)
C(5)	190(21)	277(23)	159(22)	-40(18)	65(19)	-43(19)
C(6)	260(26)	352(27)	238(26)	-58(21)	57(23)	78(21)
C(7)	218(24)	265(25)	377(28)	-20(19)	71(23)	130(22)
C(8)	274(26)	387(29)	301(28)	17(21)	124(24)	93(24)
H(1)	217(43)	489(56)	259(45)	66(38)	92(40)	47(42)
H(2)	391 (53)	567(66)	446(60)	-197(50)	214(48)	-60(54)
H(3)	303(54)	807(87)	459(64)	100(54)	89(51)	273(64)

Table 4.2.2 (cont'd)

	<u>U</u> 11	<u>U</u> 22	<u>U</u> 33	<u>U</u> 12	<u>U</u> 13	<u>U</u> 23
H(4)	589(78)	650(85)	978(110)	249(66)	497(83)	436(81)
H(5)	234(51)	1528(142)	136(47)	- 256(70)	5(43)	-17(66)
н(6)	277(51)	1699(167)	218(56)	-194(78)	82 (46)	186(76)
H(7)	807(97)	571(77)	1082(112)	365(73)	714(95)	387(79)
H(8)	394(63)	659(82)	597(75)	113(58)	43(57)	329(68)
Н(9)	849(102)	808(96)	391(68)	-207(82)	331(71)	- 5(64)
H(10)	567(80)	822(102)	767(90)	-188(71)	199(72)	472(84)
H(11)	679(85)	412(66)	771(90)	3(62)	214(74)	-104(66)

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Observed structure amplitudes and final calculated structure factors. $(\times 0)$

0,2,L	3 57 55	1.0.L	-3 58 -52	5 20 -13	3 42 37
	7 21 19	-1- 10 10	-2 17 -12	1.1.	4 57 -57
/ 84 - 77	0 38 11	-8 34 -35	2 56 57	1+14,L	• 21 12
0.5.L	0,8,L	-6 38 35	3 30 28	-8 37 -37	2.2.L
		-4 56 -61	4 59 - 60	-6 30 32	
5 78 - 40	1 27 -26	4 26 25	7 57 -58	-4 21 23	-7 54 -53
0,4.L	2 53 52	6 29 -24		3 39 -38	-6 27 21
• •	3 55 51	8 76 - 76	1.7.L	5 31 -25	-5 37 35
Ŭ 68 −78	4 32 -21	1.1.1	-10 18 19	1.15.1	-9 77 86
0.7.6	7 19 -19		-9 47 45		-1 63 64
	_	-9 62 -66	-8 50 46	-6 35 33	0 57 61
4 84 99	3,9.L	-8 17 20	-7 38 -40	-4 36 -41	1 75 81
6 60 72	2 42 38	-6 59 -61	-4 67 66	-1 28 23	6 24 -20
1.3.L	3 53 56	-5 38 34	-3 34 -31	1 66 74	
-7 66 1.4	4 55 -54	•4 54 59 •1 12 12	0 54 51	2 74 79	2,316
-6 90 -101	5 10 N	-2 51 55	2 39 42		-10 23 -25
	3,10,1	-1 16 -15	4 56 55	1.16.1	-9 24 -21
1,10+L		1 52 -53	5 42 -40	-7 19 5	-6 39 40
4 83 -100	1 57 56	4 29 27		-6 29 30	-4 50 49
5 75 84	3 46 41	6 37 -29	1,8,L	-5 25 30	-1 61 62
6 66 -72	4 53 52	7 79 -86	-9 17 -6	•3 42 40 •2 50 50	0 19 -17
6.2.L	0 10 27	0 32 -30	-7 32 29	0 42 39	2 33 24
····	€, Ji.L	1.2.L	-6 64 -66	3 41 +42	3 33 -29
1 110 131	3 43 43	-0 -47 -47	-4 40 39 -3 43 30	1.17.1	4 19 8 5 56 -55
4.4.1	3 45 42	-8 51 -49	-1 68 70		6 21 20
	4 19 -12	-7 38 34	0 39 -34	-6 29 2B	7 48 48
3 95 110	5 37 32	-6 38 38	1 32 31	-5 56 55	3 4
0.0.1	2.12.1	-> Z5 -22 -4 55 5#	∠ 8∠ 83 3 43 18	-2 42 39	2.7+L
		-1 25 -23	5 46 47	-1 29 -28	-9 54 -57
2 59 59	1 47. 44	1 63 -71	7 46 45	0 32 24	-8 25 -21
4 20 -9	2 34 33	2 67 -70 '	1.9.1	1 /J =01 2 20 10	-0 31 26 -3 58 55
	5 77 +80	5 60 -84		3 29 35	-2 80 -90
OsteL	6 23 -17	6 20 23	-9 23 2ú	5 40 37	-1 21 19
4 22 -24	a 11 i		-7 35 43 -3 40 39	1.1.4	3 33 25
5 38 44	J	1.315	2 19 12		4 69 72
6 56 -59	1 20 -22	-10 27 -32	3 56 -55	-5 20 -15	6 22 2z
7 47 47	3 35 -36	-9 17 13	4 33 - 30	-3 17 -22	
0 1 13	• 52 -51	-3 43 -30	5 55 - 32	0 30 35	*,375
0,2,L	0,14,6	-3 40 -36	1,10.L	1 16 13	-10 19 -12
		-2 19 -19		3 50 52	-9 21 9
0 42 54	0 23 -21	0 27 -23	-2 35 28	4 14 -10	-7 29 30
3 49 50	2 19 -19	2 27 -22	-1 33 -26	1,19,L	-4 54 -51
4 34 -34	3 27 23	6 25 -27	0 46 -44		-5 68 62
6 41 37 8 31 - 30	4 21 -21	8 24 19	2 55 -56	•5 29 •25	-3 53 48
6 21 - 25	5 40 4/	1.416	5 50 51	-2 19 20	-2 57 55
0,3,L	0,15,L	•••	1.11	0 22 -21	1 62 66
		-8 44 -43	-9 24 -27	2 42 -43	2 47 52
2 43 -71	4 30 -34	-/ 47 58	-8 25 -30	• • •	4 40 -34
5 17 35		-5 20 -23	-7 48 -41	1.20.1	6 53 -54
6 34 -34	2,16,L	-3 42 36	-5 35 31	-1 14 1	7 61 -64
7 34 -34 8 19 -18	• 40 #J	-2 60 01 ∞1 59 63	0 33 -29	-2 33 -34	2.6.1
,	1 21 -23	0 54 56	1 43 43	-1 31 31	••
0,4.L	2 36 -35	1 60 -66	2 47 -49	0 35 -28	-9 22 -19
2 44 -71	3 18 +14	2 23 22	5 23 +23	3 28 30	-5 32 25
3 43 -42		4 33 28	6 74 82		+2 20 -17
4 32 35	0,17,L .	5 45 -44		1,21,6	-1 19 -14
> 37 38	·	6 43 34	. 1,12,L	0 25 -24	1 43
~ 20 •27	4 26 29	6 31 26	-7 31 -28		2 38 -37
0,5,L			-6 27 -29	1+22+6	4 17 -14
	C,18,L	1,516	-4 20 -20	_1 10 _2#	5 22 22
2 20 -15	2 39 -17	-10 21 -33	-2 19 -21	-1 30 -14	2.7.L
4 39 -39		-9 39 43	-1 25 -19	2.0.L	
4 47 -46	2,19,L	-6 51 51	0 21 -25	-10 -1 -1	-6 38 41
/ 34 -27	1 31 11	-5 18 -10 -3 42 -39	3 40 -41	-10 27 -1	-4 20 -14
	3 IA 17	J 56 -59	5 22 -26	-6 72 -76	-1 17 -14
0.4.L	4 28 27	1 24 22	4 19 17	2 74 -85	+3 41 -55
1 36 - 34		2 45 44	1.13.0	4 42 -38 4 41 42	-2 30 -26
2 30 -25	0,40,L	4 35 -31	111415	- 10 16	0 70 -76
3 31 +32	ەد دە 2	5 22 23	-8 40 -37	2+1+6	1 33 27
4 34 -34	3 21 -15	6 66 -65	-6 42 -43	-9 10 14	3 28 25
5 43 37 6 66 -18	5.91.1	/ 75 /8	-2 62 +40	-5 57 -57	
8 28 29	u g a l o L	1.6.L	•1 30 28	-5 42 41	2,8,6
- - .	1 30 -30		0 38 39	•2 65 67	-10 - 22 - 1-
0.7.L	3 26 17	-8 45 47	3 57 -5#	0 59 +57	-10 22 91
1 32 -28		-4 34 33	4 20 5	2 31 24	-0 41 36

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Table 4.2.3 (cont'd)

2.8.L	2,17,L	2 19 -17	3,12,1	1 , 21 -22	-7 '34 -36
-6 37 34	-3 42 40	4 22 14	-8 24 24	4 66 94	-4 19 16
-5 18 -18	-2 24 -11	6 36 36	-7 21 -17	5 66 67	-3 27 -29
-4 21 10	0 28 -35	3.516	-5 29 33	4.2.1	2 27 25
-1 40 38	1 23 -19		-4 67 -66		3 54 -53
3 44 -46	2 33 -31	-10 36 -37	-3 32 31	-10 17 14	• • 2• •2•.
6 30 34		-7 40 39	1 65 67	-7 80 79	4.7.L
	2,18,1	-6 20 -23	4 32 35	-5 28 -24	
2,412	-6 28 24	-3 63 59	3,13,6	-1 46 34	-6 37 -36
-9 33 34	-4 26 -2	-2 56 -53		0 46 42	-5 24 21
-6 25 22	1 29 -27	-1 32 28	-4 29 -24	3 33 29	-3 64 69
-4 28 -27		1 74 -77	-3 31 30	4 46 39	-2 41 -41
-3 38 -40	2,14,1	2 64 64	-2 19 12	5 5/ -55	-1 18 -18
U 48 48	-3 21 -19	5 27 -23	1 44 47	4,3,6	1 71 76
2 31 24	-2 37 36	• • • •	2 19 10	-10 20 -7	3 26 29
4 45 47	2 33 33	3.010	4 17 20	-9 21 -22	
	2,20,1	-8 66 70		-8 95 107	4,10,L
2,10,1	-4 27 33	-2 88 102	3,14,6	-6 34 32	-9 33 27
-9 41 43	-2 20 -22	0 37 31	-7 18 -20	-4 23 21	-8 49 50
-8 32 26 -7 41 41	3 18 10	2 45 -90	-4 27 -28	-2 23 23	-5 52 52
-5 26 -23	2,21,1	5 36 - 35	-1 51 -52	-1 41 -58	-4 40 34
-4 30 -30	-2 29 -30	6 18 -14	0 18 -7	0 56 +52 2 40 39	-2 80 67
-1 42 -42		3.7.L	2 65 72	3 31 -25	0 58 58
1 39 -35	3,0,L	-15 17 14	3 31 -32	4 23 -20 5 28 32	2 53 50
2 14 17	-10 35 37	-8 24 21	3,15,6	J 10 JL	4 23 -17
2,11,L	-8 18 -17	-7 38 37		4.4.1	
-6 21 23	-6 80 -84 -2 75 -81	-6 27 23	-6 25 -25	-7 29 27	4,11,0
-7 33 -36	0 53 53	-4 24 -22	-3 37 -39	-6 43 -43	-6 61 61
-6 37 -33	4 29 29	-3 85 95	-1 27 -22	-3 20 20	-5 44 41
-2 21 -16		0 57 -55	1 21 -22	-1 63 63	-3 18 -14
0 25 16	3,1,6	1 52 -50	2 26 25	0 33 -30	-2 41 41
5 22 23	-9 62 -59	- 35 - 30 5 44 42	4 40 442	4 56 -58	0 42 41
	-8 84 -88		3,16+L	5 53 52	1 17 -15
2.12.L	-6 88 -95	3,81L	-6 32 36	415.6	3 66 69
-9 30 -32	-2 75 81	-10 22 -19	-4 18 18		
-3 24 -21	-1 41 -39	-9 21 -21	-3 22 10	-10 35 -41	4,12,L
-1 32 30	2 45 -37	-7 34 37	0 39 38	-8 25 23	-6 22 22
0 31 30	3 50 44	-6 26 -23	3 21 25	-7 40 -37	-5 29 34
2 19 16	6 I/ IS	-4 31 -26	1 63 61	-5 45 45	0 29 -29
3 44 42	3,216	-3 39 -39	3,17,16	-4 54 -53	1 63 67
5 38 36	-10 23 17	-1 58 -54	-5 22 15	-2 51 44	4,13,6
2,13,L	-9 24 -17	3 43 42	-3 22 23	-1 19 -12	
-7 -7 -23	-8 42 -42	5 55 56	C 21 20 3 17 20	1 43 -37	-7 18 -22
-5 61 -61	-6 33 31	3,916		2 35 35	-4 52 54
-3 33 -37	-5 33 -29		3,18,6	3 18 16	-3 31 -27
-1 53 19	-2 53 -47	-7 72 -74	-4 19 9	5 69 -73	0 24 23
0 22 17	1 17 15	-6 23 21	1 23 29	8.4.1	2 36 -31
5 19 -12	4 22 •11 5 32 •32	-1 38 37	2 34 -37		4,14,6
2,14,L	6 59 -63	0 54 -51	3,19+6	-9 29 -27	
	3.3.4	1 36 - 36 2 23 - 10	•2 22 22	-6 48 -41	-6 25 20
•7 42 •40	34516	4 35 -34	0 24 -14	-5 +4 +42	-5 34 35
-4 38 36	-9 39 39		.1 23 -22	-4 18 17	-3 32 31
-2 59 57	-7 33 -32	3,10,1	3.20.L	0 49 -43	-1 31 34
U 29 +25	-6 44 -39	-7 38 -39	0 21 010	1 78 -81	0 42 -34
1 50 +51	-5 54 -52	-5 27 27	0 21 -10		
3 20 -15	-3 25 -20	-4 31 -32	4.0.L	4.7.L	4,15,L
	-2 89 103	-1 24 -21	-8 59 54	-10 40 -39	-5 19 -18
211910	C 69 69	1 71 -73	-6 54 50	-9 47 50	-4 38 -34
-6 41 45	2 21 17	3 29 27		-7 52 -53	-3 23 -23
-4 24 23	5 17 13		2 60 -56	-6 55 -57	-: 21 -27
-1 55 51	6 32 = 33	3,11,1		•5 24 24	1 31 -31
1 IA IS	3.4.1	-7 21 -27	1116	-3 48 48	3 38 -34
2,16,L		-4 32 -31	-10 24 23	-1 25 -20	.
•7 •6	-9 36 -35	-5 44 -47 -4 68 59	-7 38 -34 -8 54 50	3 01 -02,	7,14,6
-4 42 -46	-7 46 -43	-2 37 -41	-6 59 -61	4 50 47	-7 51 -57
-3 51 54	-6 36 37	-1 48 -45	-4 17 15 -3 47 -44	> 48 -76	-4 52 -52
-1 54 57		4 32 24	-2 38 -36	4+++L	-1 18 -13
1 22 14	0 21 -14		-1 36 35	-9 20 -14	0 17 1.
- 11 -13	1 23 20				

Table 4.2.3 (cont'd)

4,10,6	3 29 28	5.15.1	-1 44 40	4+14+L	7,10,6
2 37 -36	5,4,L	-6 33 30	1 63 64	-2 46 48	-7 21 -25
3 18 22		-4 38 -41	2 34 37	-1 32 -40	-5 27 23
9.17.L	-8 78 -90 -7 17 2ú	-3 18 -15	6.6.L	7.0.1	-2 22 23
	-6 36 -38	1 20 -16			-1 10 15
-6 20 4	-4 27 28	e . 14.1	-7 44 -42	-8 25 29	0 37 34
-1 23 -18	-2 66 63	311010	-5 33 32	-2 72 73	7,11,6
1 72 -20	0 38 32	-6 24 12	-2 17 -8	2 18 20	-5 -60 -7
2 27 31	1 17 11	-3 22 20	1 23 19	7.1.L	+3 29 32
4,10,1	5,7.L	-2 42 43		-6 -2 -23	-2 42 44
-4 29 -37	-6 61 67	5,13,6	6;/sL	•1 71 72	1 30 -40
-3 44 -39	-7 38 -40		-8 40 -38	-3 23 21	7,12,1
0 32 35	-6 42 42	-3 51 -53	-6 35 -35	0 35 -36	-6 20 -19
4,19,L	-4 78 84		-2 24 20	1 17 -14	-3 34 -31
-1 26 21	•3 45 •40 •2 45 45	5,14,L	0 68 -68	7.2.1	0 17 14
-1 22 23	-1 80 -84	-7 19 -9	1 34 33		
E 0.1	1 31 32	5.14.1	6.8.1	-7 31 -30	7,13,6
3,012		311-10		-6 55 -60	-5 29 -27
-10 19 20	5,8.L	2 35 +32	-4 30 -33 -3 20 -18	-5 29 28	-1 23 17
-4 89 -98	-8 28 -34	5.17.6	-1 63 -64	-2 54 -53	
0 41 -39	-6 35 29	-1 -14 -010	0 51 48	0 18 13	8,0+L
4 19 -21	-4 87 94	-4 36 37	3 31 -33	2 27 25	-6 27 -30
	-3 18 15	-2 33 33	4	7.3.1	-2 65 72
5,1,6	1 31 28	1 34 52	••••		8,1,L
-10 18 -15	3 40 34	5.18.6	-8 18 19	-8 19 -20	-7 65 54
-8 34 -30	5.9.L	-3 37 42	-5 31 -25	-4 48 45	-6 21 12
-6 48 -46		-2 19 26	-3 56 -59	-3 71 70	-5 36 33
	0 19 7	-1 36 34	0 26 25	1 47 -45	-3 30 -32
1 43 -64	2 22 -23	4.0.L	3 20 -19	• • •	-2 21 13
2 39 -37	3 16 -13	-8 34 40	6.10.L	/ • 4 • L	-1 19 10
3 38 34	5,10,L	-6 47 -47		-6 23 21	#,2.L
5,2,L		-2 18 20	-6 19 -16 -7 26 -23	-/ 40 -34	-5 59 -54
-9 23 28	-7 20 20	2 28 -28	+6 21 21	-5 36 32	-3 52 -51
-8 27 20	-5 39 35		-4 36 -36	-1 51 -48	-2 30 -29
-3 71 -06	-1 27 23		-1 41 44		1 41 44
-2 25 19	1 19 13	-10 32 32	1 19 -23	7,5,6	6.3.1
-1 37 -38	3 24 -22	-7 21 22		-8 17 10	-,
2 24 27		-5 58 -55	6,11+L	-7 51 -56	-6 40 -39
• 28 20	5,11+6	-3 27 26	-6 17 15	-5 31 -25	-2 33 37
5,3,6	-8 34 -37	-1 53 -55	-4 17 -10	-3 49 -49	8.9.1
-10 37 -37	-5 61 61	1 70 -69	-2 35 38		
-8 28 -26	-4 29 -25	2 49 49	-1 34 -36	7,6,L	-7 19 23
	-2 22 -20	4.2.L	1 1/ 30	-8 28 28	-2 25 -23
-4 19 12	0 18 -4		6,12,6	-5 19 7	1 25 29
-2 36 35	2 48 -46 3 47 -49	-9 19 17	-7 29 31	-2 17 -14	8,5.L
0 89 -94	• • • • • •	-7 69 77	-6 34 40	0 25 -28	-4 27 - 29
1 44 -41	5,12,L	-5 24 24	-2 20 -22	7.7.L	-5 25 28
3 48 -16	-4 45 -50	-2 26 -22	-1 62 67	-4 25 -18	-4 37 -31
	-3 81 -92	5 42 -100	1 26 26	-5 21 15	-1 17 +13
31-15	0 22 -23	4.3.L	2 16 -21	-3 28 -27	
-9 20 22	1 32 -32	-9 29 33	6.13.L	0 25 22	•,•·L
-6 17 13	5 10 -12	-8 53 48		1 20 20	-6 91 -96
-5 46 -41	5,1316	-5 27 -25	-3 25 33	4 20 27	8,7,⊾
-2 27 -27	-8 23 -28	-1 74 74	-2 25 14	7.8.6	
-1 77 -79	-5 51 -52	C 52 50	4 17 -16	-6 40 39	-1 17 20
4 20 23	-3 50 +53	2 75 76	6,14,L	-5 20 12	-3 19 12
	-2 36 -37	6.4.1	-6 54 60	-3 27 19	-1 34 -37 D 19 -13
5.201	-1 27 21		-3 27 35	-2 34 -35	
-10 20 15	5,14,6	-8 18 -6	U 43 -43	1 27 . 26	4,8 ,1
-v 38 -37 -8 48 50	-5 22 -21	-6 62 60	6,15,L		-4 34 31
-7 53 -49	-3 37 -40	-4 57 54	-4 34 -17	7.9.L	-3 30 -31
-6 87 -08 -4 59 -56	-2 17 18 -1 20 17	-2 17 12	-3 48 50	+6 31 24	-1 26 -22
-3 37 32	30 -25		•1 23 18 0 32 14	•5 24 27 •4 35 -33	á. • • •
-1 43 44	3 22 -27		- /•	-3 19 19	
1 96 149		-3 27 26		-1 37 -37 1 22 27	-5 19 13

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Analysis of structure-amplitude agreement. (N is the number of reflections in each group.)

(a) As a function of $(\sin\theta)/\lambda$

Range	ΣF_0	$\Sigma\Delta$	<u>N</u>	<u>R</u>	(ΣΔ)/ <u>N</u>
0.0 - 0.1	13.64	1.76	5	0.129	0.352
0.1 - 0.2	203.44	16.15	42	0.079	0.384
0.2 - 0.3	614.40	4 7. 62	136	0.078	0.350
0.3 - 0.4	1057.04	85.26	247	0.081	0.345
0.4 - 0.5	1706.77	130.50	407	0.076	0.320
0.5 - 0.6	1077.05	122.06	359	0.113	0.340
0.6 - 0.7	28.29	3.62	10	0,128	0.362
(b) As a	function of	<u>F</u> o			
0.0 - 3.0	1066.16	177.96	470	0.167	0.379
3.0 - 5.0	1684.95	116.59	435	0.069	0.278
5.0 - 7.0	1269,99	54.06	217	0.043	0.249
7.0 - 9.0	590.48	.47.05	75	0.080	0.626
9.0 -11.0	89.06	11.32	9	0.127	1.255
ALL	4700 064	406.98	1206	0.086	0.337

Low-order reflections affected by extinction which were removed from the final stages of refinement.

h	k	1
0	1	2
0	4	0
0	4	1
0	5	1
1	0	2
1	0	-2
1	9	-1
2	0	0
2	0	-2
2	0	-4
3	0	-4

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Interatomic distances (A) and angles (degrees) within the succinate residues (standard deviations in parentheses).

C(1) - O(1)	1.317(6)	C(5)-O(5)	1.312(8)
C(1)-O(2)	1.212(9)	C(5)-O(6)	1.226(8)
C(1)-C(2)	1.493(7)	c(5)-c(6)	1.495(8)
C(2)-H(4)	1.099(16)	С(6)-Н(8)	1.090(14)
C(2)-H(5)	1.087(12)	C(6)-H(9)	1.093(16)
C(2)-C(3)	1.513(8)	C(6)-C(7)	1.526(7)
C(3)-H(6)	1.038(13)	C(7)-H(10)	1.077(19)
C(3)-H(7)	1.101(16)	C(7)-H(11)	1.126(17)
C(3)-C(4)	1.501(7)	c(7)-c(8)	1.497(7)
C(4)-0(3)	1.277(9)	C(8)-0(7)	1.306(9)
C(4)-0(4)	1.233(6)	C(8)-0(8)	1。204(9)
0(1)-C(1)-O(2)	122.9(0.6)	0(5)-c(5)-0(6)	123.1(0.6)
0(1)-C(1)-C(2)	114.6(0.5)	0(5)-C(5)-C(6)	113.4(0.5)
0(2)-C(1)-C(2)	122.5(0.4)	0(6)-C(5)-C(6)	123.5(0.5)
C(1)-C(2)-C(3)	115.4(0.4)	C(5)-C(6)-C(7)	114.4(0.4)
H(4)-C(2)-H(5)	104.9(1.3)	H(8)-C(6)-H(9)	103.4(1.1)
C(2)-C(3)-C(4)	114.2(0.4)	C(6)_C(7)_C(8)	110.7(0.4)
H(6)-C(3)-H(7)	108.7(1.4)	H(10)-C(7)-H(11)	107.3(1.3)
C(3)-C(4)-O(3)	116.1(0.4)	C(7)-C(8)-O(7)	113.5(0.5)
C(3)-C(4)-O(4)	121.4(0.6)	C(7)_C(8)_O(8)	123.3(0.5)
0(3)-C(4)-O(4)	122.5(0.6)	0(7)-C(8)-0(8)	123.2(0.7)

Sums of, and differences between, C = 0 distances, and differences between C = C = 0 angles in the carboxyl groups.

Unit		R ₁	R ₂	
Carboxyl group	C(5)	C(8)	C(4)	C(1)
∑(C - 0),(Å)	2.528	2.510	2.510	2.529
$\Delta(C - O), (Å)$	0.044	0.105	0.086	0.102
$\Delta(C - C - 0)$, (deg.)	10.1	9.8	5.3	7•9

Torsion angles (degrees) in the succinate residues, with standard deviations in parentheses.

Atom <u>A</u>	Atom \underline{B}	Atom C	Atom \underline{D}	Angle
0(1)	C(1)	C(2)	C(3)	14.7(0.5)
0(2)	C(2)	C(2)	C(3)	-167.6(0.4)
C(1)	C(2)	C(3)	C(4)	-177.1(0.3)
C(2)	C(3)	C(4)	C(3)	169.6(0.4)
C(2)	C(3)	C(4)	C(4)	-10.2(0.4)
C(5)	C(5)	C(6)	C(7)	34.5(0.5)
0(6)	C(5)	C(6)	C(7)	-145.1(0.5)
C(5)	C(6)	C(7)	C(8)	57.3(0.4)
C(6)	C(7)	C(8)	0(7)	-170.6(0.3)
C(6)	C(7)	C(8)	0(8)	8.5(0.4)

The angle A-B-C-D is defined as positive if when viewed along the B-C bond atom A has to be rotated clockwise to eclipse atom D.

Interatomic distances (A) and angles (degrees) in the hydrogen bonds, with standard deviations in parentheses.

$$0(1) \dots 0(4)^{\perp} 2.579(9) 0(1) - H(1) \dots 0(4)^{\perp} 178.1(1.0)$$

$$0(1) - H(1)$$
 1.009(12) $C(1) - 0(1) - H(1)$ 110.9(0.8)
 $H(1) \dots 0(4)^{I}$ 1.571(12) $C(1) - 0(1) \dots 0(4)^{I}$ 111.1(0.5)

$$0(5) \dots 0(3)^{I}$$
 $2.573(11)$ $0(5) - H(2) \dots 0(3)^{I}$ $162.6(1.2)$ $0(5) - H(2)$ $0.991(16)$ $C(5) - 0(5) - H(2)$ $110.5(0.9)$ $H(2) \dots 0(3)^{I}$ $1.610(16)$ $C(5) - 0(5) \dots 0(3)^{I}$ $110.6(0.5)$ $0(7) \dots 0(3)$ $2.630(10)$ $0(7) - H(3) \dots 0(3)$ $172.3(1.3)$ $0(7) - H(3)$ $0.996(15)$ $C(8) - 0(7) - H(3)$ $109.4(1.1)$

 $H(3) \dots O(3) \quad 1.639(14) \quad C(8) - O(5) \dots O(3) \quad 113.9(0.6)$

Environment of the potassium ion: $K^+ \cdots 0$ distance $\begin{pmatrix} 0 \\ A \end{pmatrix}$ and $0 \cdots K^+ \cdots 0$ angles (degrees); standard deviations of angles $\sim 0.4^{\circ}$.

	K(1)•••0(2) K(1)•••0(2 ^{III})		2•736(9) 2•775(12)		K(1)•••0(6 ¹¹)		2.834(12)		
					K(1)•••	K(1) • • • 0(6 ^{IV})		2.781(12)	
	K(1)•	•••0(3)	3.189(11)		K(1)•••	K(1)•••0(8 ^{II})		1)	
	$K(1) \cdots O(4^{VI})$		2.797(10)		K(1)	K(1) ····0(8 [♥])		2.767(12)	
	0(2)	0(2 ^{III})	0(3)	0(4 ^{VI})	$0(6^{II})$	0(6 ^{IV})	0(8 ^{II})	0(8 ^V)	
0(2)	0	91.97	122.34	157.72	85 .7 0	86.23	60.88	67.85	
0(2 ^{III})		0	103.29	69.05	120,15	165.00	60.24	67.66	
0(3)		•	0	75.07	127.78	65.69	163.46	67.80	
0(4 ^{VI})				0	93•74	115.14	98. 39	112.53	
0(6 ^{II})					0	74.60	67.07	153.10	
0(6 ^{IV})						0	130.14	98.00	
0(8 ^{II})							0	101.96	
(8 ^V)								0	

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Subset of reflections used in the initial $\frac{\Sigma_2}{2}$ solution and their F_b - and F_b + values (as defined in the text). The reflections are listed in order of decreasing E.

h	k	1	F _b -	^F ь+	h	k	ו	F _b -	F_+ b
6	2	1	13.07	1 4,28	5	1	7	11.67	12.87
4	3	-8	10.33	7.36	5	3	- 6	15.89	11.07
6	2	0	-10. 05	- 5.04	· 5	6	-8	-9.04	-6.52
5	5	1	5.96	4.72	6	6	0	9.03	7.36
6	8	1	-7.49	-6.04	5	1	0	-1.1.01	-10. 08
5	12	-3	-9.19	-12.90	5	5	- 6	-8.76	- 8 . 95
3	1	-8	-8.82	-8.35	4	1	4	9.43	6.96
6	5	-2	-9.42	-2,68	6	3	2	7.65	12.54
5	8	-4	9.35	12.43	6	9	-7	-7.02	-7.96
1	11	6	8,22	9.13	1	1	7	-8.57	-1 3.03
4	7	5	-7.58	-5.79	5	2	-7	- 8 . 18	-7.76
5	8	-1	9.06	5.85	5	3	0	9.43	6,96
6	•7	-1	7.99	5.86	4	5	5	-7.32	-5.68
4	10	3	-7.93	-3.85	1	5	7	7.76	8,90
1	17	1	- 8.06	-5.74	0	2	7	-9. 88	-7.90
7	1	-4	7.23	3.45	6	2	-7	7.67	1.72
4	2	-7	7. 88	9.24	4	11	- 1	-9.20	-6.29
7	3	-3	6.98	6.01	0	12	5	-8.02	9. 20

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Table 4.2.11 (cont'd)

I.

h	k	l	F _b -	F _b +	h	k	1	F	F _b +
8	1	-7	5.46	7.37	6	14	- 6	5.98	5.60
5	4	1	- 8,66	-6.12	3	1	- 6	-9.54	-9.69
3	9	-7	-7.44	-3.69	6	12	-1	6.67	7.84
1	1 5	2	7.87	5.28	5	7	-1	-8,45	-7.88
0	7	6	9.20	4.77	4	1	5	6.69	6.04
6	1	1	-6.89	-7.41	4	16	-7	-5.70	-5.30
4	11	3	6.90	3.84	5	7	-4	8,38	5.91
5	7	- 8	6.75	7.81	6	7	0	-6.77	-5.70
3	15	0	7.04	7.31	1	1	-9	-6.55	-4.43
1	10	5	8.44	11.68	6	3	-1	7.38	3.09
4	10	-2	8.71	7.12	1	12	-3	-8.92	-4.00
3	6	8	6.99	3.82	2	18	1	-6,21	-3.42
4	6	4	-6. 98	-3.32	3	1	-9	-5.90	-8.27
4	1	3	8.07	4.42	1	10	6	-7.23	-5.84
8	2	- 5	-5.45	-2.72	3	14	2	7.22	5.82
1	6	-8	6.70	5.11	2	5	7	-6.45	-5.01
1	17	- 5	5.54	5.62	8	3	-4	-5.98	-2.87
6	5	1	6.39	4.80	5	A.	-1	-7.90	-4.11
4	12	-3	-6.78	-6.95	1	2	5	-8.38	-5.50
3	7	3	9.55	4.73	4	6	1	-8.12	-4 .24
4	3	-7	7,11	6.46	1	4	7	-6.43	-8,26
6	. 8	-1	-6.37	-6.37	3	6	- 2	10.15	11,21

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Reflections whose phases were incorrectly determined by the symbolic addition procedure, along with their F_o , F_{b-} and F_{b+} values (as defined in the text).

h	k	1	Fo	^F b -	^F b+
8	2	-5	5•45	- 5•45	-2.72
8	3	-4	5.42	-5.98	-2.87
0	8	6	6.65	-7.38	-3.33
8	2	-3	5.15	-5.14	-5.28
5	l	3	5.76	5•94	3.14
1	13	3	5•75	-5.80	-1.37
7	13	-3	3.90	4.04	1.57
3	2	6	5.86	6.30	-0.88
6	6	-6	5.85	5.91	-0.13
4	10	-8	4.89	4•97	4.05
l	13	-2	6.17	-5.98	-4.88



Figure 4.2.1 : KH₃Succ₂ - the crystal-chemical-unit (C.C.U) and numbering scheme.



Figure 4.2.2 : The crystal structure of KH_3Succ_2 projected along the <u>b</u> axis from y = 0 to $y = \frac{1}{4}$.



Figure 4.2.3 : The crystal structure of KH3 Succ2 projected

along the <u>c</u> axis.



Figure 4.2.4 : Graph showing the Nakamoto-Margoshes-Rundle relationship between 0...0 and 0-H distances in hydrogen bonds. The graph is that given by Hamilton and Ibers⁹. The diagonal broken line corresponds to hypothetical centrosymmetric bonds. The values obtained from the analyses of KH₃Succ₂ and KH₃Glut₂ are indicated by crosses and stars respectively.



Figure 4.2.5 : The environment of the potassium ion. The two questionable K⁺... O contacts are represented by dot-dash lines.

4.3. The Crystal Structure of potassium tri-hydrogen di-glutarate

4.3.1. Introduction

Unlike potassium tri-hydrogen di-succinate, small crystals of potassium tri-hydrogen di-glutarate suitable for x-ray analysis are relatively easily grown, and its structure has been solved from x-ray diffraction data by Dr. A.L. Macdonald.¹⁰ However, the x-ray analysis revealed nothing about the positions of the hydrogen atoms in the structure, and a full set of neutron diffraction data were therefore collected in order to locate the hydrogen atoms accurately, in particular, the three hydroxylic protons involved in hydrogen bonding.

4.3.2. Experimental

Crystal Data

The $\underline{a}\sin\beta$ and \underline{b} dimensions of the potassium salt were derived from a least-squares treatment of some high-order reflexions on an hko Weissenberg photograph. The other cell dimensions were obtained from precession and rotation photographs.

 $KC_{10}H_{15}O_8$, <u>M</u> = 302.10. Monoclinic, <u>a</u> = 11.182(3), <u>b</u> = 12.727(4), <u>c</u> = 9.423(8) $\stackrel{\circ}{\Lambda}$, <u>β</u> = 92.75(25)^o; <u>U</u> = 1339.5 $\stackrel{\circ}{\Lambda}^3$, <u>D</u>_m = 1.46, <u>z</u> = 4, <u>D</u>_c = 1.495. Space group P_{2_1}/c (No. 14). Diffracted neutron intensities were measured on a Ferranti Mk 11 four-circle diffractometer mounted in the Dido reactor at A.E.R.E. Harwell using a neutron beam monochromated to 1.172 Å. A crystal of dimensions 6.0 (parallel to <u>c</u>) x 6.5 x 2.0 m.m.³ mounted along <u>c</u> was used, and integrated intensities were measured for some 2,000 reflections out to $\theta = 45^{\circ}$. Of these, only 1009 with $|F| \ge 3\sigma(|F|)$ were used in the analysis, and absorption corrections were applied to these observed data using a calculated $\mu(\text{effective})$ of 1.66 cm⁻¹. The incoherent scattering cross-section of hydrogen was taken as 3 7 x 10⁻²⁴ cms.

4.3.3 Structure analysis and refinement.

The observed structure amplitudes were combined with phases calculated from the set of fractional coordinates determined for the nonhydrogen atoms in the x-ray analysis to compute a map of neutron-scattering density in which all fifteen hydrogen atoms were found in their expected positions. The atomic coordinates thus determined were refined by leastsquares analysis using the program CRYLSQ; two cycles of full-matrix isotropic least-squares refinement followed by four cycles of blockdiagonal anisotropic least-squares refinement reduced R to 0.87. Unit weights were used throughout, and the relative constancy of $(\Sigma \Delta^2/N)$ when analysed at the end of refinement in terms of $F_{\rm obs}$ and $\sin\theta/\lambda$ indicated that a non-unit weighting scheme was not required. The nuclear scatteringlengths used were 0.350, 0.661, 0.577 and -0.378 x 10^{-12} cm for K, C, 0 and The final positional and vibrational parameters are given in Tables 4.3.1 and 4.3.2 respectively. The observed structure amplitudes and calculated structure factors are listed in Table 4.3.3 and an analysis of their agreement is given in Table 4.3.4.

4.3.4 Discussion of the structure.

The crystal-chemical unit (C.C.U.) and atomic numbering system is shown in Figure 4.3.1; other symmetry-related units required to describe the structure are given in Table 4.3.5. The crystal structure is represented in Figures 4.3.2 and 4.3.3 and the principal interatomic distances and angles in the glutarate residues are listed in Tables 4.3.6 and 4.3.7 respectively.

The results of the x-ray analysis suggested that R_2 is the glutaric acid molecule and R_1 the acid anion, the carboxyl group centred on C(1) being the ionised carboxylate. The neutron analysis provides confirmation of the x-ray results by locating the hydroxylic protons and also from the dimensions of the four carboxyl groups; the unionised carboxyls have larger differences in their C-O lengths and C-C-O angles (Table 4.3.8).

The crystal structure is based on infinite chains of B_2 type acid anion residues linked head-to-tail by short asymmetric hydrogen bonds, and in this respect is similar to the crystal structure of potassium trihydrogen disuccinate. In this case, however, the chains form two antiparallel helices which spiral around the two-fold screw axes at $\frac{1}{2}$, \underline{Y} , $\frac{1}{4}$ and $\frac{1}{2}$, \underline{Y} , $\frac{3}{4}$. The helices of different cells are linked together by hydrogen bonding to the unionised glutaric acid molecules; the O(5) carboxyl oxygen of an R₁ residue is linked via an R₂ residue to the O(2) carboxylate oxygen of the equivalent R₁ residue in the cell (101). There is no hydrogen-bonding between helices in the same cell.

The glutaric acid molecule is in an extended form, and the five glutarate chain atoms C(6), C(7), C(8), C(9) and C(10) appear to be coplanar, their mean plane being represented by the equation -0.2078X + 0.9449Y - 0.2529Z' = 2.5891 Å; the root mean square distance of the atoms from this plane is 0.006 A. However, examination of the thermal parameters in Table 4.3.2 shows atoms C(7) and C(9) to have U_{22} values of 0.18 and 0.21 $^{\circ}A^2$ respectively, while atoms C(6), C(8) and C(10) have U₂₂ values of 0.06, 0.05 and 0.04 \mathbb{A}^2 respectively. The anomalously large U_{22} values for atoms C(7) and C(9) are in a direction (along b) which is approximately normal to the plane of the glutarate chain, and can be explained if the glutarate chain is considered to be slightly disordered, adopting the two conformations (a) and (b) in Figure 4.3.3 : atoms C(6), C(8) and C(10) have the same positions in both conformations, while atoms C(7) and C(9) are alternatively above and below the plane of the glutarate chain.

The acid anion (R_1) is non-planar, with a dihedral angle about C(2) - C(3) of about 55°. However, atoms C(2), C(3), C(4) and C(5) approach coplanarity with a dihedral angle about C(3) - C(4) of 176.1°. Details of the other conformations in the glutarate residues are given in

Table 4.3.9.

The interatomic distances and angles of the three hydrogen bonds are set out in Tables 4.3.10a and 4.3.10b respectively. The bond between The R, residues $O(4) \cdots O(3^{II})$ is the strongest, although its 0 ••••• H ••••• O angle is the least favourable of the three. Its length (2.49 Å) is not significantly different from that found for a similar bond in ammonium hydrogen diacetate.¹¹ The bond between O(1) and O(2) which joins the anion and the acid molecule is in a similar environment and its 0 H 0 angle is 177.5°; however it is significantly weaker, with an 0 · · · · · 0 distance of 2.57 Å. The third bond $\{0(5) \cdots 0(6)\}$ is between the unionised carbonyl group of the acid anion and the other carbonyl group of the acid molecule and its length of 2.64 Å is similar to those found in carboxylic acid dimers. The O-H distances in the three bonds - 1.08, 1.06 and 0.96 A show the expected increase with decreasing 0 0 distance and points representing these O-H distances and the corresponding O O distances show a good fit to the Hamilton-Ibers version of the Nakamoto-Margoshes-Rundle curve (Figure 4.2.4). The two shorter hydrogen bonds make angles with both the donor and acceptor bonds which are close to tetrahedral (110-117°), whereas the angle of the longest hydrogen bond with the acceptor groups differs appreciably from this value (136.8°).

The environment of the potassium ion is represented in Figure 4.3.4; the ion is co-ordinated to 8 oxygen atoms at distances of less than 3.04 $\stackrel{o}{A}$ and the K⁺ 0 distances and 0 K⁺ 0 angles

are given in Tables 4.3.11 and 4.3.12.

As a further test of the applicability of the symbolic addition method to neutron data, an attempt was made to solve the structure of potassium tri-hydrogen di-glutarate directly from neutron data, and with hydrogen accounting for 22 per cent of the total scattering power of the crystal, compared with 20 per cent in potassium tri-hydrogen disuccinate, this was a slightly stiffer test of the method. However, the results were equally successful; phases were found for 191 reflections with $E \ge 1.5$ and an E-map calculated with these phased E's as coefficients revealed every atom in the structure, although a few of the methylenic hydrogens were poorly resolved.

TABLES AND DIAGRAMS

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Table 4.3.1

Fractional coordinates $(\underline{x}, \underline{y}, \underline{z})$ and absolute orthogonal coordinates (in A, with $\underline{X}' = \underline{axsin}\beta$, $\underline{Y} = \underline{by}$, $\underline{Z}' = \underline{cz} + \underline{axcos}\beta$, and with standard deviations in parentheses).

(a) Neutron analysis.

	<u>x</u>	<u>y</u>	<u>z</u>	<u>x</u> '	<u>Y</u>	<u>Z</u> '
к+	0.1208	0.4205	0.4307	1.350(11)	5.352(12)	3.993(12)
0(1)	0.0718	0.3022	0.8282	0.802(8)	3.847(11)	7.766(8)
0(2)	0.2308	0.2957	0.6404	2.578(9)	3.764(10)	5.911(9)
0(3)	0.2592	0.1317	0,7095	2.895(8)	1.676(8)	6.546(9)
0(4)	0.6017	0.4786	0 .7 891	6.721(9)	6.091(9)	7.113(9)
0(5)	0.6617	0.4508	0.5716	7.391(9)	5•734(9)	5.031(8)
0(6)	0.6769	0.3967	0.3026	7.561(9)	5.049(13)	2.488(9)
0(7)	0.8712	0.4295	0.3192	9•731(10)	5.467(13)	2.541(10)
0(8)	0.9671	0.3873	-0.3413	10.800(11)	4.931(11)	-3.740(10)
C(1)	0 . 2859	0.2103	0.6374	3.193(7)	2.676(7)	5.853(6)
C(2)	0,3858	0,2026	0.5367	4.309(7)	2.578(8)	4.850(7)
C(3)	0.4631	0.3006	0.5263	5•172(8)	3.826(8)	4.711(6)
C(4)	0.5135	0.3342	0.6673	5.736(7)	4.253(7)	6.012(7)
C(5)	0.5991	0.4272	0.6700	6.691(7)	5.436(7)	5.991(7)
C(6)	0.7814	0 .407 2	0.2517	8.727(8)	5.183(9)	1.953(7)
C(7)	0.7793	0.3750	0.0941	8.704(9)	4.772(16)	0.469(8)

Table 4.3.1(a) (cont'd)

	<u>x</u>	ዾ	Z	<u>x</u> ,	Y	<u>Z</u> *
C(8)	0.8919	0.3819	0.0214	9.961(8)	4.861(7)	-0.277(8)
C(9)	0 .87 45	0.3490	-0.1304	9.767(9)	4.442(17)	-1.698(9)
C(10)	0•9754	0.3476	- 0 . 2242	10.895(7)	4.423(8)	-2.636(8)
H(1)	0.6619	0•5441	0.7822	7.393(17)	6.924(14)	7.015(14)
H(2)	0.1376	0.2025	0,2517	1.537(11)	3.786(16)	7:009(13)
H(3)	0.6733	0.4150	0.4013	7.521(18)	5.281(20)	3.421(17)
H(4)	0.4483	0.3624	0.0658	5.007(13)	1.729(15)	5.091(25)
H(5)	0.6584	0.6818	0.0639	3.815(23)	2.313(27)	3.926(17)
H(6)	0.5924	0.8602	0.0217	4.552(19	4.584(18)	4.289(18)
H(7)	0.4630	0.7800	0.0444	5.998(20)	3.562(19)	4.006(19)
H(8)	0.4450	0 . 1453	0.2438	4.970(25)	4.514(34)	6.770(21)
H(9)	0.5693	0.2316	0.2180	6.358(26)	3.416(22)	6.461(25)
H(10)	0.7001	0.3944	0.0407	7.820(21)	5.019(36)	0.008(15)
H(11)	0.7551	0,2919	0.1036	8.434(26)	3.715(30)	0.571(31)
H(12)	0.9678	0.3531	0.0775	10.807(23)	4.494(40)	0,212(21)
H(13)	0.9121	0.4567	0.0246	10.187(59)	5.812(42)	-0.257(45)
H(14)	0.7974	0.1239	0.3213	8.906(34)	4.786(57)	-2.112(24)
H(15)	0.8370	0.2245	0.3668	9.349(39)	3.504(45)	-1.704(35)
Table 4.3.1 (cont'd)

(b) X-ray analysis.

	x	X	<u>Z</u>	<u>X</u> ,	<u>Y</u>	<u>Z'</u>
к+	0.1221	0.4180	0•4337	1.368(2)	5.305(2)	4.027(2)
0(1)	0.0721	0.3000	0.8237	0.808(8)	3.808(10)	7. 734(9)
0(2)	0.2291	0.2937	0.6373	2.567(8)	3.728(8)	5.871(8)
0(3)	0.2623	0.1316	0.7103	2.940(7)	1.670(8)	6 . 562(8)
0(4)	0.5984	0•4774	0.7844	6.706(8)	6.058(8)	7.081(8)
0(5)	0.6607	0. 4480	0.5718	7.403(8)	5.685(8)	5.040(8)
0(6)	0.6782	0.3968	0.3024	7.599(10)	5.035(12)	2.489(10)
0(7)	0.8719	0.4291	0.3218	9.770(10)	5.446(12)	2.568(11)
0(8)	0.9684	0.3864	-0.3411	10,852(9)	4. 904(9)	-3.740(9)
C(1)	0.2862	0.2079	0.6350	3.207(9)	2.639(9)	5.838(10)
C(2)	0.3857	0.1996	0₀5341	4.322(13)	2.533(12)	4.833(14)
C(3)	0.4618	0.2986	0.5240	5.175(11)	3.790(12)	4.696(13)
C(4)	0.5138	0.3312	0.6676	5•757(10)	4.202(12)	6.024(12)
C(5)	0.5955	0.4259	0.6666	6.674(10)	5.406(11)	5.970(11)
C(6)	0.7844	0.4050	0.2488	8.490(13)	5.140(15)	1.925(13)
C(7)	0.7781	0.3786	0.0971	8.720(14)	4.804(20)	0.497(13)
C(8)	0.8957	0.3791	0.0242	10.036(13)	4.811(15)	=0.254(14)
C(9)	0.8737	0.3559	-0.1293	9.791(14)	4.517(28)	-1.691(16)
C(10)	0.9762	0.3505	-0.2244	10.939(11)	4.448(11)	-2.643(12)

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Table 4.3.2 (a) (Neutron analysis)

Vibrational parameters ($^{02}_{\Lambda} \times 10^4$), with standard deviations in parentheses.

	<u>U</u> 11	<u>U</u> 22	<u>U</u> 33	<u>U</u> 12	<u>U</u> 13	<u>U</u> 23
к+	164(47)	219(57)	298(63)	37(47)	70(46)	11(49)
0(1)	294(38)	822(69)	252(40)	27(46)	123(34)	230(45)
0(2)	358(42)	402(45)	472(52)	70(39)	147(39)	228(41)
0(3)	311(37)	223(34)	452(47)	125(34	193(36)	101(34)
0(4)	416(47)	440(51)	407(48)	- 251(42)	273(40)	-231(41)
0(5)	414(43)	442(48)	204(36)	-99(40)	128(34)	-8(36)
0(6)	366(44)	955(83)	290(45)	-103(53)	127(37)	-225(51)
0(7)	424(48)	904(80)	336(46)	-123(58)	56(4 0)	-150(54)
0(8)	531(55)	550(60)	448(54)	144(52)	25(46)	121(47)
C(1)	326(31)	277(31)	212(32)	-73(30)	-11(27)	42(28)
C(2)	417(39)	316(36)	364(38)	-4(33)	209(34)	-81(32)
C(3)	396(36)	406(40)	196(32)	-1 8(35)	133(28)	26(30)
C(4)	411(39)	322(36)	233(34)	-102(33)	66(31)	47(28)
C(5)	299(31)	220(31)	295(33)	2(29)	49(27)	40(29)
C(6)	463(40)	615(52)	212(34)	-36(42)	99(31)	-97(36)
C(7)	360(43)	1,767(123)	251(41)	213(63)	123(35)	-15(57)
C(8)	454(42)	544(49)	3 34(39)	-208(38)	189(34)	-126(36)
C(9)	252(38)	2,097(147)	316(43)	219(63)	96(34)	-213(66)
C(10)	252(34)	446(44)	379(39)	55(33)	150(30)	-84(34)
H(1)	7 40(98)	364(71)	402(75)	-86(73)	359(75)	-143(62)

	<u>U</u> 11	<u>U</u> 22	<u>U</u> 33	<u>U</u> 12	<u>U</u> 13	<u>U</u> 23
H(2)	412(68)	516(76)	285(64)	-164(65)	136(56)	2(58)
H(3)	557(90)	812(12)	552(93)	-271(97)	140(77)	-202(91)
H(4)	688(114)	165(65)	1,477(179)	-89(72)	582(124)	170(86)
H(5)	911(142)	1,472(209)	257(77)	427(146)	29(85)	534 (112)
H(6)	644(102)	497(96)	604(99)	-7(85)	-216(83)	-213(81)
H(7)	751(117)	614(111)	747(110)	221(100)	444(98)	167(94)
H(8)	906(144)	1,779(269)	561(115)	477(167)	489(118)	136(147)
H(9)	1,070(169)	617(131)	966(158)	-50(125)	-285(134)	-444(12C)
H(10)	596(109)	2,472(331)	128(69)	116(162)	-81(71)	- 185(123)
H(11)	881(150)	977(175)	1,354(212)	-329(147)	400(147)	-410(171)
H(12)	607(114)	2,566(372)	546(116)	842(179)	-67(93)	302 (165)
H(13)	3,326(611)	1,505(312)	1,914(346)	-1432(373)	1624(396)	-13 82(292)
H(14)	1,114(217)	3,454(630)	531(129)	-1295(325)	-40(134)	-1 09(232)
H(15)	1,830(321)	2,591(428)	1,487(266)	1802(339)	1144(259)	1817(316)

.

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Table 4.3.2 (b)(x-ray analysis)

	<u>U</u> 11	<u>U</u> 22	<u>U</u> 33	<u>20</u> 23	<u>2U</u> 13	<u>20</u> 12
K(1)	498(11)	502(10)	504(15)	-46(19)	330(19)	-141(19)
0(1)	594(46)	959(63)	632(59)	-415(89)	322(78)	-286(83)
0(2)	570(42)	645(45)	622(54)	- 429(73)	451(73)	-126(67)
0(3)	536(40)	605(43)	634(52)	-472(70)	485(70)	-110(63)
0(4)	635(46)	697(48)	588(54)	271(75)	471(76)	224 (74)
0(5)	583(42)	617(43)	567(52)	94(69)	4 58(70)	285(65)
0(6)	747(59)	1,441(90)	634(67)	299(111)	481(94)	450(113)
0(7)	787(61)	1,180(80)	789(71)	211(112)	66(96)	407(108)
0(8)	727(54)	689(49)	738(63)	-372(83)	360(86)	-439(79)
C(1)	455(50)	446(47)	444(65)	- 58(78)	181(81)	1C6(74)
C(2)	802(78)	597(63)	723(89)	103(110)	960(135)	423(109)
C(3)	448(53)	780(74)	666(84)	-59(113)	494(102)	549(98)
C(4)	508(58)	698(66)	557(78)	-54(108)	16(96)	277(94)
C(5)	395(46)	619(57)	461(69)	64(90)	156(80)	-78(81)
C(6)	764(75)	940(93)	533(86)	232(124)	459(113)	292(129)
C(7)	683(79)	1,739(155)	397(87)	330(161)	543(118)	97(167)
C(8)	645(69)	1,034(96)	5 22(85)	67(129)	540(114)	226(125)
C(9)	596(76)	2,356(246)	515(104)	503(239)	465(134)	-91(214)
C(10)	567(60)	545(56)	537(74)	30(92)	370(97)	-48(88)

Observed structure amplitudes and final calculated structure factors. ($\star \omega$)

0.0.L		0,11,L	0 92 -100	1.11.1	-4 63 65	2,12,1
			1 76 73	•	-3 59 -54	
2 89 -	6 2	28 -24	2 60 -55	-7 27 -29	-2 23 -21	0 46 47
4 50 -	3	24 -23	4 69 -62	-4 24 -18	-1 41 -33	2 38 - 36
e 111 11	3 7	44 -41	6 44 45	0 42 -41	3 21 20	
0.1.1	2	33 92	8 43 445	3 40 -41	5 75 -77	2,13,6
31115		0.12.1	1 130	3 37 27	, 52 50	-5 24 -10
1 45 4	19		1.5.1	4 73 76	2.5.1	-4 37 -39
2 66 -	8 2	42 -42		5 25 -17		-2 41 43
3 46 -	2 5	29 28	-10 32 34	-	-8 43 -37	2 33 -30
4 51 -4	8		-8 67 -67	1.12.1	-7 60 54	
5 23 2	23	0,13,L	-5 44 -41.		-6 43 47	2.14.L
6 78 -1	12 .		-4 25 -17	-5 37 -34	-3 72 79	
9 90 - 9	1 2	30 33	-3 41 41	-4 43 33	0 60 -49	3 24 19
			-2 64 -64	-3 42 43	- 1 35 - 34	4 37 42
0.2.1		0,19,1	1 38 36	+2 23 -16	3 22 16	2.15.1
2 43 -	44 D	10 27	4 73 73	£ 03 37 6 47 - 36	8 46 43	211-11
3 76 -	10 0	50 27	5 59 53	· · · · · · · · · · · · · · · · · · ·	0 .0 .0	-1 24 23
4 35	30	1.0.L	-7 38 -38	1.13.4	2.6.1	•
5 64 4	6		, , , ,,	•••••		3.0.L
6 70 -	6 -10	63 66	1.6.L	-6 35 34	-9 66 65	
7 46 -	13 -8	60 59		-3 34 34	-8 30 -24	-10 28 28
8 46 -	15 -4	35 - 39	-5 53 -48	-2 21 -19	-6 28 -23	-8 67 -65
	2	63 -60	-4 30 23	0 32 38	-5 68 63	-6 21 22
0,3,L	4	52 54	-3 62 61	2 34 -29	-4 45 43	-4 76 70
	6	49 -46	-2 30 23	5 29 -24	-Z 55 -59	-Z 108 -123
1 40	0		0 27 -24		-1 40 -41	Z 27 -25
6 28		1,1,1	1 84 86	1.15.6	0 5/ 54	4 31 -26
9 35 1	12		2 48 -38	0 33 - 51	1 /4 /2	• 24 -22
a .	-10	Z4 21	4 45 -38	0 23 -21	3 30 -24	8 37 42
U.4.L	- 0	9/ -13		1 28 20	4 25 22 6 44 45	3.1.1
0		23 - 21	/ 20 2/	* . 0 . 1	7 43 - 34	27112
2 44	16 -4	29 12	. 7.1	21012	,	-11 34 32
5 24 -	27 -3	49 -47		-10 46 -43	21716	-8 26 33
7 31	23 -2	77 -98	-8 69 -72	-8 78 -80		-5 26 -23
	-1	12 -10	-7 28 21	-4 23 -23	-7 56 -55	-3 32 30
0,5,L	0	23 -25	-6 59 -56	4 38 39	-5 42 41	-2 60 -59
	1	17 -15	-5 31 25		-3 69 -69	-1 50 -50
3 73	70 2	58 55	-3 82 83	2+1,L	0 54 -50	0 66 68
4 54 -	47 3	70 60	-2 64 -74		-1 22 -20	1 87 92
5 44 -	34 4	71 62	-1 47 -42	-8 115 129	1 48 54	Z 45 -39
6 59	59 8	48 43	2 51 51	-7 59 65	5 74 -73	4 66 -63
			3 82 -82	-6 30 30		5 23 -23
0,6,L		1.2.1		-5 -1 -31	2101	3 67 63
		• • • • •	1.8+6	-7 68 65	- 0 10 12	A 13 11
1 42 -	4Z −]L	0 30 +27 10 10 −34	- 7 4 7 - 1 7	-1 67 72	• A 30 - 23	9 23 +15
5 28 -	14 -7		-/ -/ -//	0 36 35	-5 24 23	,
8 27	23 -4	35 -81	-1 35 42	1 42 - 34	-2 37 -27	3,2,6
0 27	- 5	AL A4	-1 25 -17	2 73 69	-1 27 23	
8.7.1	- 4	43 - 39	0 77 79	3 33 - 29	0 35 -41	-9 58 - 58
	- 3	79 -69	2 43 43	5 28 -34	2 3.6 31	-8 46 -41
1 41 -	36 - 2	32 - 35	3 45 45	♦ 37 = 38	4 51 -57	-5 33 31
3 30	28 0	24 -17	4 63 60	_	5 24 25	-4 70 -67
4 42 -)) 2	101 108	5 48 -53	2.2,L		-3 61 -55
5 39 -	35 3	21 -1/			2.9.1	-2 62 70
7 43	35 4	47 41	1,9+L	-10 35 -26		-1 20 21
8 37 -	28 5	94 95		-0 >> >>	-4 29 -34	1 44
	,	40 40 40 AD	-9 20 -21	-3 44 -42	-4 41 -49	4 22 23
UsbsL		ער בר י דר נו י	-8 27 28	-2 48 44	0 49 -34	5 66 -67
a . •	- 7	76 -3/		•1 73 B1	4 34 -34	6 49 49
J 60 -	37 81	1.3.4	-3 2, 20	2 71 -68	5 30 -30	7 57 50
2 60 -	42	19-396	-2 103 113	4 44 -35	<u>6</u> 67 62	0 31 -23
1 34	36 -10	30 25	- 30 29	7 38 -32		• 24 -25
41 17	35 -1	29 29	0 39 41		2.10.L	
5 18 -	37 -2	52 49	1 27 22	2,3,L		3,3,6
6 .7 -	47 -6	5 56 57	3 58 -++		-8 33 -34	
	- 9	5 56 64	4 44 -41	-8 76 76	-7 30 -27	-10 24 -18
0.9.L	- 3	3 48 -43		-7 41 -34	-6 40 -38	-8 26 -26
-	- 2	2 38 -39	1,10,L	•5 21 13	2 86 70	-7 37 -41
1 55 -	55 -1	50, 48		0 59 752	3 47 -44	
2 3A	41 1	27 25	-5 52 -50	1 30	2.11.1	
			-4 47 -42	3 37 32		
5 29 -	31 2	39 - 32				-2 41 14
5 29 - 7 28	31 2 16 3	28 - 27	-2 41 33	מנ מנ	-4 44 40	-2 41 34
5 29 -	31 2 16 3	28 -27 28 -27 23 -22	-2 41 33 -1 36 32 0 31 -33	6 30 30	-6 44 40 -4 46 45	-2 41 34 -1 29 24 0 81 80
5 29 - 7 28 0,10,L	31 2 16 3	2 39 -32 3 28 -27 4 23 -22 5 41 32	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 30 30 2+1+L	-6 44 40 -4 46 45 -2 27 19	-2 41 34 -1 29 24 0 81 80 3 36 -32
5 29 - 7 28 0,10,L	31 2 16 3 5	2 39 -32 3 28 -27 4 23 -22 5 41 32	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 30 30 2+4+L	-6 44 40 -4 46 45 -2 27 19 -1 31 24	-2 41 34 -1 29 24 0 81 80 3 36 -32 4 28 25
5 29 - 7 28 0:10:L 0 70	31 2 16 3 48 25	2 39 -32 3 28 -27 4 23 -22 4 1 32	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 30 30 2+4+L -10 23 29	-6 44 40 -4 46 45 -2 27 19 -1 31 24 0 43 45	-2 41 34 -1 29 24 0 81 80 3 36 -32 4 28 25 5 59 49
5 29 - 7 28 0,10,L 0 70 1 31 2 33	31 2 16 3 48 25 31 -10	2 39 -32 3 28 -27 4 23 -22 4 1 32 1,41L 3 24 19	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 30 30 2.4.L -10 23 29 -9 43 40	-6 44 40 -4 96 45 -2 27 19 -1 31 24 0 43 45 2 61 64	-2 41 34 -1 29 24 0 81 80 3 36 -32 4 28 25 5 59 49 6 97 98
5 29 - 7 28 0,10,L 0 70 1 31 2 33 5 14 -	31 2 16 3 48 25 31 -10 37 -1	2 39 -32 3 28 -27 4 23 -22 5 41 32 1,4,L 0 24 19 8 34 -34	-2 41 33 -1 36 32 0 31 -30 2 54 -43 4 65 -58 5 33 32	4 30 30 2+4+L -10 23 29 -9 43 40 -7 24 -25	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-2 41 34 -1 29 24 0 81 80 3 36 -32 4 28 25 5 59 49 6 97 98 7 34 44

Table 4.3.3 (cont'd)

3.4,L	3,10,L	2 48 -46	4 29 -30	5.4.L	5,14,6
- 26 23	-4 55 41	3 23 -23			
-8 27 20	-5 46 -49	7 44 -41	40110	-7 76 192	-4 24 21
-7 59 58	-3 32 32	, , -,,	-2 41 45	-1 44 66	5.13.6
-6 55 60	-2 52 -53	4,4.6	-1 31 29	-2 82 71	51111
-4 47 -44	-1 26 -30		3 30 -24	-1 34 38	0 34 38
• 3 72 70	1 30 -23	-8 64 68	4 34 31	0 41 41	. .
=1 80 B5	4 32 -41	-/ 0/ -00	a 32 32	22 - 23	4 8 ⁴ 8 L
0 53 44	5 32 -34	-3 38 33	4.12.L	3 38 34	-4 34 -38
1 63 -63		-1 76 -82		4 27 31	-4 26 -30
2 71 64	3,11,1	0 20 -24	-2 26 35	5 46 43	-2 69 66
3 105 -105		1 37 37	3 35 -34	6 60 61	0 20 -12
6 84 -84 7 38 -33	-7 99 -40	2 88 81		7 59 -54	3 72 -74
, ,,	1 30 26	4 42 -59	111316	5.5.1	5 85 -85
3,5,6		5 36 37	-5 35 -33	31316	7 31 37
	3,12,L	6 63 67	-3 24 19	-8 25 29	
-10 33 -33		7 37 -29	1 31 -27	-7 45 57	6.5.L
-7 68 -64	-2 24 21	_		-6 54 54	
-6 31 27	2 34 -25	4,5+6	4,14,6	-5 55 -54	-9 26 -25
-5 77 -00	- 33 -3	-1.0 15 12	2 24	-4 54 -50	-8 44 -40
-3 34 26	3.13.1	-9 32 -33	2 20 23	0 40 -55	-5 86 -90
-2 21 23		-8 22 -20	5,0,L	1 53 +53	-2 31 29
-1 27 -32	-4 29 22	-7 46 -39	• • •	5 33 -33	-1 34 34
0 60 -59	-1 22 -24	-5 46 47	-10 37 41	7 39 -34	0 40 40
1 79 -77	2 37 37	-3 49 -46	-8 26 -25	-	4 49 -45
2 56 -52 4 44 -45	3 14 1	-1 55 5/		51016	2 83 83
7 28 -26	3,14,1	2 7 91	-2 31 -28	-8 27 -20	6.6.1
•••	-2 41 -38	6 69 -73	2 29 -22	-7 45 -72	
3,6,L			6 94 -87	-5 84 -80	-7 45 -41
_	4,0.L	4.6.L	8 40 38	-3 34 -32	-6 35 40
-9 65 -76				0 23 -20	-5 40 37
-/ 21 -11	-10 30 -28	-9 20 26	51116	1 53 50	-4 62 +64
•5 18 37	-6 37 -39	-7 20 16	-10 24 -22	4 52 52	-3 /3 //
-4 53 52	-4 18 12	-6 37 36	-8 30 26	6 54 -48	1 53 48
-3 47 +53	-2 60 -56	-5 40 38	-7 45 45		2 23 -14
-2 21 18	2 100 -101	-4 23 16	-6 43 -44	5.7.L	3 36 35
-1 35 29	4 20 23	-3 41 32	-3 64 63		4 34 28
2 36 - 38	6 22 -16	-1 47 42	-2 27 25	-5 40 -43	-
3 35 35	8 75 70	0 50 52	•1 95 •92	-4 4/ 48	6./.L
5 40 45	4.1.1	47 41	0 00 -02	-2 35 -34	-7 49 57
6 57 -61	41.12	• • •	5,2,6	-1 49 -50	-6 26 34
	-7 89 89	4.7.6		0 48 -50	-4 30 20
3,7,L	-6 33 -25		-10 32 -32	1 40 35	-3 28 -25
-7 -7 75		-6 51 -58	-/ 48 51	5 28 30	-2 45 45
-/ 82 /3	-1 45 -11	-3 20 -22	-4 23 17	A 24 24	1 46 45
-5 24 18	-2 84 85	2 24 21			0 26 -20
-4 41 45	1 24 29	3 45 -49	5 . I . L	5+8+L	
-3 30 24	2 52 -48	4 43 42			6,10,L
-2 67 -65	4 95 101	6 39 -36	0 82 -62		0 60 60
-1 30 24	5 35 37	7 28 30	2 29 -23	-1 30 -70	0 30 -47
2 32 42	8 24 - 29	4.8.1.	5 50 -48	-2 38 -37	6,11,L
3 25 -18	-		6 30 -23	3 29 28	
4 55 -59	4,2.1	-8 46 -50	7 60 74	5 39 -44	1 32 -30
5 51 -55		-7 26 -23		6.0.	4.13.
é 49 -38	-8 55 57	-5 65 -66	21416	31716	o,i≮,L
	-7 67 66	-1 30 -27	-3 72 -73	-6 28 -32	-1 26 29
398 j.C	-1 49 46	2 22 -13	-2 48 -48	-3 56 -53	0 23 22
-6 13 -32	0 75 -73	3 44 49	0 53 50	-2 25 -24	1 35 27
2 35 -35	1 37 36	4 33 -33	2 44 -44	-1 36 34	2 31 +35
3 37\ 40	2 49 53		4 43 -45	0 26 27	
5 51 -46	3 37 -33	4.9.6	• 26 Z3	2 4/ 45	6,13,6
6 49 49	4 36 34	r F3 40	6.1.1	• • • • • •	-1 25 -15
1.0.1	5 47 44	-4 43 -50		5,10.2	-1 12 -10
	7 62 -62	-2 52 -44	-10 55 -58	-	7,0.L
-7 30 Zil		0 22 14	-9 -6 -50	-6 35 -41	
-6 26 -30	4.3.L	1 49 47	-8 57 55	-4 29 ,23	-6 66 61
-4 79 82	- 10	2 35 -31	-/ 29 -32 	-1 -10 -10 66- 00 -	-z 66 -69 0 50 -1-
-1 24 16	-7 63 62	J 20 17	+4 47 -47	3 32 -19	2 41 34
1 27 -20	-7 84 +8ú	4.10.L	-2 5. 60		4 59 -41
2 33 36	-6 61 54		0 51 47	5.11.L	
3 37 -30	-4 47 -47	-4 23 -29	2 54 -50	· · · · · ·	
4 65 59	-2 26 -23	-3 30 -27	3 02 01 4 23 34	0 45 44/	
5 44 44	-1 38 -37	3 46 -48	,,	2 23 16	
		- · · · · ·			

Table 4.3.3 (cont'd)

7.1.L	-4 24 21	8,516	0 50 +52	10.3.L	11+4+L
	-2 44 -43		1 58 58		
-7 29 27		-5 34 34	3 23 -16	-7 27 27	-6 29 23
-6 34 -29	7,10,L	-3 56 -51	4 (29 - 23	-2 41 -46	-4 38 -32
-5 28 -30	2 3/ 3/	-2 21 -11		-1 34 35	-3 25 -20
-4 36 -30	-2 35 31	0 21 12	9+5,L	0 36 34	0 2/ 29
-3 26 -21	2 28 34		-7 46 -0	2 32 = 35	1 33 -36
-2 90 -71	3 29 -30	H. C.L	-7 75 38	3 44 43	2 34 -33
-1 30 20			-2 23 23	9 20 17	
22 17	/.II.L	- 60 - 60	-1 55 54	10.4.1	111916
J 42 JO	-4 51) -55	2 32 -31	8.6.1	101415	
7.2.1	1 25 26	4 17 41		-7 51 51	-1 31 -10
	2 36 -28		-6 29 24	-3 54 -56	0 35 -39
-8 26 26	3 27 -25	8.7.L	-3 53 57	-1 47 49	1 36 30
-4 26 22	5 23 -18	•••	-2 28 21	3 73 -76	• • • • •
2 39 -37		-7 35 33	1 42 -42		11,6,6
3 35 - 34	7,12,L	-6 29 -20	3 25 -24	10,5,L	
5 61 -63		-5 42 -42	4 27 -32		-5 40 42
6 38 42	-3 31 -40	-4 38 40		-5 44 -43	
7 33 28	-2 41 49	-3 43 48	9+7,L	-4 31 -37	11+7+L
		-1 25 -16		-3 56 59	
7,3,6	8,0.L	2 28 -20	-7 39 -37	-1 31 -35	-1 31 32
	- 9 - 4 - 4 - 5	3 37 38	-5 28 30	4 26 22	
-3 8Z -83	-0 64 -62	4 Z> 19	-1 80 -74	10.4	11000
-4 65 -05		5 27 26	-1 74 -7"	101010	-))
-1 45 4/	-1 27 31	0.0.1	0 31 10		-3 37 48
U 24 -15	0 104 113	8.81	2 37 - 19	3 42 47	12.0.1
4 30 -30	2 55 +50	-1 29 -30	2 01 57	2 12 11	1-1-16
7 25 21	4 34 -29		9.8.1	10.7.6	0 34 -38
/ 25 -1		1 3 27	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	1-1-1-	4 34 34
7.4.6	1	8.9.L	-5 36 42	-2 30 28	,
			-3 27 -26	5 23 -17	12,2,6
-9 43 45	-9 56 -53	-4 34 32	-1 26 18		
-8 22 24	-8 28 25	-1 44 -40	3 33 22	10,8,L	-5 41 -36
-7 56 -58	-6 92 83		5 30 -22		-3 21 14
-6 67 -68	-3 35 3 0	8,10.L		-5 24 -27	1 29 -21
-3 47 41	-1 96 -102	•	9191L	-4 37 43	
-1 83 85	1 72 69	1 23 24		-1 32 38	12;],L
2 22 19	2 23 - 25	2 46 52	-3 29 -29	2 24 24	
3 86 88	3 34 -44		-2 35 24		-4 25 19
5 42 54	4 39 37	9,0,L		10.4.6	-2 54 55
6 25 17			V.10.1		0 11 +31
• • •	8,2,L	-8 33 32	-3 33 -33	-3 30 31	12.8.1
1+5+6	- 0 51	-4 30 -32			1
	-3 51 -10	-2 /2 //	3 24 -23	11.0.1	-1 28 28
		4 21 51	• • • • • •		2 24 14
	-7 37 20	e. 1.1	•••••	-4 23 19	
-1 42 -56	-1 89 92	*****		-4 38 40	12.5.1
•2 100 110	1 60 66	-7 42 -47	-2 23 19	-2 60 63 .	
-1 42 -45	4 29 -29	-2 78 -75		0 52 -59	-3 27 -32
0 35 -34	5 26 32	0 24 22	10.0.L	2 20 23	-] 28 24
1 33 -29		1 36 35		4 27 21	
2 44 46	8,3,L	2 24 -30	• • 23 -27		12,6,L
		4 53 -54	-4 74 -81	110106	
7161L	-9 51 53		0 54 54		-1 43 46
	-6 65 63	9,2,L	2 28 •32	•6 •7 51	1 23 -24
-6 54 -59	-5 26 20		• 51 57	•3 33 37	13.0.1
-4 43 50	-1 53 -18	-7 23 -22	10.1	-2 37 -60	134095
-3 71 -63	-3 57 62	-6 43 -32	10+1+6	-1 30 -34	
-i i 08 ₊117	-2 45 -44		-7 31 33	2 43 -50	2 24 22
	-1 78 78	-3 27 28	-4 31 29	5 20 -34	13.1.1
7.7.L'			-3 49 -53		
	4 12 -14	0 <u>3</u> 0 32	0 95 97	11,2.L	41 45 L44
	6 14 14	8.3.1	1 30 -29		1 28 24
-1 23 -10	- 27 20		2 34 +33	-5 28 28	
- 37 33	8.9.6	-4 51 49		-1 27 -27	13.2.L
7.8.1		-3 48 -48	10.2.L	0 31 -38	
	-7 25 24	-2 22 16		2 24 24	-2 24 -25
-5 25 -25	-5 56 SU	-1 72 76	-6 30 26	5 31 -24	0 27 -24
-4 35 36	-4 35 -30	1 79 -77	-4 24 19		2 22 -26
-3 30 28	-3 79 -80	2 39 35	+2 53 +53	11,3,6	
-1 23 24	-1 5e +52	4 34 -42	-1 36 -29		
	0 60 458	•	1 38 472	•6 76 93	
7.9.6	3 31 -22	9,91L	J 76 70 5 24 14		
	ч 32 30	21 -15	* **	1 27 -31	

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Table 4.3.4

Analysis of structure-amplitude agreement. (<u>N</u> is the number of reflections in each group).

(a) As a function of $(\sin\theta)/\lambda$

Range	ΣF_{O}	$\Sigma\Delta$	N	R	$(\Sigma \Delta)/N$
0.0 - 0.1	15•72	1.69	6	0.107	0,282
0.1 - 0.2	300.41	28,24	52	0.094	0.543
0.2 - 0.3	693.53	51.35	143	0.074	0.359
0.3 - 0.4	1092.65	83.24	233	0.076	0.357
0.4 - 0.5	1506.38	125.39	340	0.083	0.368
0.5 - 0.6	777•57	92.28	231	0.119	0.399
0.6 - 0.7	12.04	1.25	4	0.104	0.313
(b) As a func	tion of F _o				
0.0 - 4.0	1576.19	. 201.07	528	0,128	0.380
4.0 - 6.0	1434.85	109.26	295	0.076	0.370
6.0 - 8.0	916.39	49•73	134	0.054	0.372
8.0 -10.0	375.15	15.99	43	0.043	0.372
10.0 -12.0	95 •7 3	7.40	9	0.077	0,820
All	4398.31	383.45	1009	0.087	0,380

Table 4.3.5.

Equivalent positions

I	x, y, z = C.C.U
II	1-x, ½+y, 3/2-z
III	l+x, y, -l+z
IV	$1-x, -\frac{1}{2}+y, 3/2-z$
v	-l+x, y, l+z
VI	$x, \frac{1}{2}-y, -\frac{1}{2}+z$
VII	1-x, 1-y, -z
VIII	-l+x, y, z
IX	l-x, l-y, l-z

1.7

Table 4.3.6

Bond lengths (Å) in the glutarate residues: (a) neutron analysis, (b) x-ray analysis (Eacdonald, 1971). Standard deviations are im parentheses.

		(a)	(b)
C(1)	- 0(2)	1.250(12)	1.264(12)
C(1)	- 0(3)	1.254(11)	1.239(12)
C(5)	- 0(4)	1,299(11)	1,282(14)
C(5)	- 0(5)	1.224(11)	1.212(13)
C(6)	- 0(6)	1,290(12)	1.322(17)
C(6)	- 0(7)	1.197(12)	1.211(17)
C(10)	- 0(8)	1.214(12)	1.191(15)
C(10)	- 0(1 ^{III})	1.299(11)	1.314(14)
C(1)	- C(2)	1.503(10)	1.505(17)
C(2)	- C(3)	1.524(11)	1.525(17)
C(3)	- C(4)	1.481(9)	1.507(17)
C(4)	- C(5)	1.521(10)	1.513(15)
C(6)	- C(7)	1.540(12)	1.469(19)
C(7)	- C(8)	1.465(12)	1.515(19)
C(8)	- C(9)	1.494(12)	1.487(21)
C(9)	- C(10)	1.466(12)	1.493(19)

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Table 4.3.6 (cont'd)

C - H distances (neutron analysis only)

C(2) - H(4)	1.126(19)	C(7) - H(10)	1.027(22)
C(2) - H(5)	1.080(20)	C(7) - H(11)	1.096(34)
C(3) - H(6)	1.066(20)	C(8) - H(12)	1.045(26)
C(3) - H(7)	1.118(22)	C(8) - H(13)	0.978(44)
C(4) - H(8)	1.108(26)	C(9) - H(14)	1.015(37)
C(4) - H(9)	1.136(24)	C(9) - H(15)	1.025(46)

Bond angles (degrees) in the glutarate residues: (a) neutron analysis, (b) x-ray analysis. Standard deviations are in parentheses.

				(a)	(b)
0(2)	-	C(1)	- 0(3)	123.5(0.8)	122.7(0.9)
C(2)	-	C(1)	- 0(3)	119.6(0.7)	119.7(0.9)
C(2)	-	C(1)	- 0(2)	116.9(0.7)	117.6(0.9)
C(1)	-	C(2)	- C(3)	115.4(0.6)	114.6(0.9)
C(2)	-	C(3)	- C(4)	111.8(0.6)	111.3(1.0)
C(3)	-	C(4)	- C(5)	116.8(0.6)	114.9(0.9)
C(4)	-	C(5)	- 0(5)	124.0(0.7)	125.0(1.0)
C(4)	-	C(5)	- 0(4)	113.2(0.7)	112.4(0.9)
0(4)	-	C(5)	- 0(5)	122.8(0.8)	122.2(0.9)
0(6)	-	C(6)	- 0(7)	125.4(0.9)	121.5(1.2)
C(7)	-	C(6)	- 0(6)	111.0(0.7)	110.7(1.2)
C(7)	-	C(6)	-0(7)	123.3(0.8)	127.8(1.3)
C(6)	-	C(7)	-C(8)	117.5(0.8)	116.0(1.2)
C(7)	÷	C (8)	- C(9)	110.9(0.7)	109.6(1.1)
C(8)	-	C(9)	- C(10)	120.8(0.8)	119.9(1.2)
C(9)	-	C(10)	- 0(8)	121.0(0.9)	120.9(1.2)
C(9)	-	C(10)	- 0(1 ^{III})	115.2(0.8)	117.1(1.2)
0(8)	_	C(10)	- 0(1 ^{III})	123.8(0.9)	121.9(1.1)

Table 4.3.7 (cont'd)

H - C - H angles (neutron analysis only)

Table 4.3.8

Sums of, and differences between, C = 0 distances, and differences between C = C = 0 angles in the carboxyl groups.

Neutron analysis

	R	1	R ₂		
Carboxyl group	C(1)	C(5)	C(6)	C(10)	
Σ(C-O), Å	2.504	2.523	2.487	2.513	
∆(C-O), Å	0.004	0.075	0.093	0.085	
Δ (C-C-O), (deg.)	2.7	9.6	12.3	5.8	
	X-ray	analysis			
$\Sigma(C-O), \tilde{A}$	1.503	1.494	1.533	1.505	

 Δ (C-O), \breve{A} 0.025 0.070 Δ (C-C-O), (deg.) 2.1 12.6 0.111 0.123 17.1 3.8

•

Table 4.3.9

Torsion angles^{*} (degrees) in the glutarate residues : (a) Neutron analysis, (b) x-ray analysis, with standard deviations in parentheses.

Atom A Atom B Atom C Atom D

Angle

(a) (b)

C(1)	C(2)	C(3)	C(4)	55.0(0.6)	56.1(1.0)
C(2)	C(3)	C(4)	C(5)	176.1(0.6)	177.2(1.0)
C(6)	C(7)	C(8)	C(9)	-179.4(0.8)	-177.3(1.2)
C(7)	C(8)	C(9)	C(10)	-178.5(0.8)	-179.2(1.2)
0(2)	C(1)	C(2)	C(3)	39.4(0.7)	40.2(0.9)
0(3)	C(1)	C(2)	C(3)	-143.1(0.7)	-140.7(0.9)
C(3)	C(4)	C(5)	0(4)	153.6(0.7)	152.9(0.9)
C(3)	C(4)	C(5)	0(5)	-28.0(0.7)	-33.4(1.0)
0(6)	C(6)	C(7)	C(8)	-179.6(0.9)	-176.8(1.2)
0(7)	C(6)	C(7)	C(8)	5.9(0.8)	1.6(1.3)
C(8)	C(9)	C(10)	0(8)	-131.9(0.9)	-140.1(1.2)
C(8)	C(9)	C(10)	0(1)	44.8(0.9)	43.3(1.1)

The angle A-B-C-D is defined as positive if when viewed along the B-C bond atom A has to be rotated clockwise to eclipse atom D.

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Table 4.3.10(a)

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O Interatomic distances (A) in the hydrogen bonds : (a) neutron analysis, (b) x-ray analysis, with standard deviations in parentheses.

	(a)	(b)		
0(1)•••0(2)	2.569(13)	2.550(12)		
0(1) - H(2)	1.056(16)			
H(2)•••0(2)	1.514(16)	• .		
0(4)•••0(3 ^{II})	2.492(12)	2.513(11)		
O(4) - H(1)	1.075(18)			
H(1)0(3 ^{II})	1.421(17)			
0(6)•••0(5)	2.640(12)	2.640(14)		
0(6) – H(3)	0.962(20)			
H(3)•••0(5)	1.678(19)			

Table 4.3.10(b)

Interatomic angles (degrees) in the hydrogen bonds (neutron analysis only), with standard deviations in parentheses.

$$O(1) - H(2) \cdots O(2)$$
177.5(1.6) $C(10) - C(1) - H(2)$ 111.0(1.1) $C(10) - O(1) \cdots O(2)$ 110.0(0.6)

$$0(4) - H(1) \cdots O(3^{II})$$
 173.3(1.5)
 $C(5) - O(4) - H(1)$ 109.1(1.1)
 $C(5) - O(4) \cdots O(3^{II})$ 112.8(0.6)

$$0(6) - H(3) \cdots 0(5)$$
 $177.4(1.9)$ $C(6) - 0(6) - H(3)$ $114.5(1.4)$ $C(6) - 0(6) \cdots 0(5)$ $115.5(0.7)$

O Environment of the potassium ion : oxygen contacts (A) with standard deviations in parentheses.

	Neutron analysis	X-ray analysis
K ⁺ 0(2)	2.776(15)	2.720(8)
K ⁺ 0(3 ^{VI})	2.736(14)	2.763(8)
K ⁺ 0(8 ^{V11})	2.753(16)	2.806(8)
K ⁺ 0(8 ^V)	2.847(16)	2.828(8)
$K^+ \cdots O(7^{\vee \perp \perp \perp})$	2.938(14)	2.954(8)
$\mathbb{K}^+ \cdots O(5^{\perp X})$	2.934(14)	2.975(8)
$K^+ \cdots O(1^{\vee \perp})$	3.037(16)	2.999(8)
$\mathbb{K}^+ \cdots O(7^{\perp X})$	3.031(16)	3.013(8)

Table 4.3.12

Environment of the potassium ion : $0 \cdots K \cdots 0$ angles (degrees). The standard deviations on the angles from the neutron analysis are ~ 0.5 deg.; from the x-ray analysis ~ 0.7 deg.

Neutron analysis

 $0(2) 0(3^{VI}) 0(8^{VIII}) 0(8^{V}) 0(7^{VIII}) 0(5^{IX}) 0(1^{VI}) 0(7^{IX})$

0(2)	0	99.0	150.0	69.0	131.1	89.2	76.1	79.1
0(3 ^{VI}	99.1	0	100.9	157.3	107.4	68.4	68.4	138.5
o(8 ^{VII})	150.9	101.1	0	98.2	62.4	77.6	132.5	71.1
0(8 ^V)	69.6	158.6	97.8	0	71.2	128.3	89.7	60.2
$0(7^{VIII})$	131.3	107.7	61.5	70.9	0	138.5	76.6	104.2
0(5 ^{IX})	90.5	67.7	76.9	128.6	137.0	0	131.1	70.1
0(1 ^{VI})	77.2	68.3	130.5	91.1	76.2	131.4	0	146.4
0(7 ^{IX})	80.8	137.6	70.3	60.5	103.2	69.9	148.9	0

x-ray analysis

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Figure 4.3.1 : KH_3Glut_2 - the crystal-chemical-unit (C.C.U.) and atomic numbering system.



Figure 4.3.2 : The crystal structure of KH_3Glut_2 projected along the <u>c</u> axis. The methylenic hydrogen atoms have been omitted for clarity.



Figure 4.3.3 : The two disordered conformations proposed for the glutaric acid molecule (R_2)



Figure 4.3.4 : The environment of the potassium ion in KH₃Glut₂.

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CHAPTER 5

THE CRYSTAL AND MOLECULAR STRUCTURE OF a-PICOLINE_N_OXIDE

HYDROCHLORIDE MONOHYDRATE.

5.1. Introduction

The ability of many monobasic acids to form crystalline acid salts, $\underline{M}^{+}H\underline{X}_{2}^{-}$, which contain short, symmetrical hydrogen bonds (Type A acid salts) has been described in section 1 of Chapter 4; certain monoacidic bases are capable of forming analogous crystalline basic salts, $\underline{HB}_{2}^{+}\underline{X}^{-}$, where \underline{X}^{-} is the acid anion, and \underline{B} the neutral base.

In 1962 Hadzi¹ reported the preparation of such a basic salt, α -picoline N-oxide hemihydrobromide, a 2:1 adduct of the base α -picoline N-oxide with hydrogen bromide. It had an infra-red spectrum similar to those of Type A acid salts, and Hadzi thus predicted a structure containing a short symmetrical hydrogen bond with the proton bridging the two oxygen atoms. This prediction was subsequently verified in an x-ray diffraction study of the hemihydrobromide by Mills and Speakman,² who found a crystallographically symmetrical hydrogen bond,with $0 \cdots 0 = 2.3$ Å. Unfortunately, the quality of the x-ray data was poor, owing to the decomposition of the crystal in the x-ray beam during data collection, and the present work was initiated in the hope that α -picoline N-oxide hemihydrochloride, if it could be prepared, would prove more stable to x-rays than the hemihydrobromide.

Hadzi's method of preparing N-oxide hydrohalides, by bubbling hydrogen chloride gas into a solution of α -picoline N-oxide in ethanol under strictly anhydrous conditions, was tried, but with no success; only the normal 1:1 adduct could be isolated. Different solvents, such as acetone and methanol, and various mixtures of these solvents, were tried, but again with no success. As a last resort, some base was dissolved in concentrated hydrochloric acid in a base:acid molar ratic of 2:1. Two crystalline products were obtained: one was identified from its infra-red spectrum as the free base, but the other product had an infra-red spectrum which was almost identical to that of α -picoline N-oxide hemihydrobromide, except for an additional peak at 3,300 cm⁻¹ due to hydration. A density determination (by flotation) of the latter product implied that the stoichiometry corresponded to the hydrated neutral salt [<u>B</u>.HCl.H₂0], where <u>B</u> = α -picoline N-oxide. The evidence of the infra-red spectrum was, however, confirmed by the subsequent structure analysis, which revealed the presence of the centrosymmetric ions [B₂H]⁺ and [HCl₂]⁻.

5.2. Experimental

Preparation

 α -Picoline N-oxide hydrochloride monohydrate was prepared by dissolving some α -picoline N-oxide slowly in an equimolar quantity of concentrated hydrochloric acid. The resulting material was recrystallised from water, to give clear plate-shaped crystals of m.p. 41-43°C. The crystals have plate faces (100) and are elongated parallel to <u>b</u>.

Crystal Data

 $\begin{array}{l} \alpha - \text{Picoline N-oxide hydrochloride monohydrate, $C_{6}H_{10}NO_{2}Cl$,}\\ M = 163.6. \quad \text{Orthorhombic, }\underline{a} = 17.570(9), \quad \underline{b} = 6.793(5),\\ \underline{c} = 13.345(9) \stackrel{\text{O}}{\text{A}}, \quad \underline{U} = 1591.5 \stackrel{\text{O}}{\text{A}^{3}}. \quad \underline{D}_{m} = 1.35, \quad \underline{D}_{c} = 1.367,\\ z = 8. \quad \text{Space group (unambiguously from absences) }\underline{Pccn} (No. 56).\\ F(000) = 688, \quad \mu(MoK_{\alpha}) = 4.2 \text{ cm}^{-1}. \end{array}$

5.3.(a) Collection of x-ray data.

A crystal of dimensions 0.45 x 0.35 x 0.15 m.m³ was mounted along its <u>b</u> axis and dipped in a diluted solution of the mounting glue to form a protective coating, since exposure to x-rays caused rapid decomposition. Preliminary crystal data were determined photographically, and more accurate cell dimensions were derived by a least-squares treatment of high-order reflections whose θ values had been measured on a Hilger and Watts four-circle diffractometer, using Mo-K_{α} ($\lambda = 0.71069$ Å).

Intensity data were collected on the diffractometer using filtered No radiation, out to $\theta = 20^{\circ}$. The two standard reflections remained constant throughout the data collection, indicating that the protective coating had successfully prevented decomposition. It was not considered worthwhile collecting data beyond $\theta = 20^{\circ}$ because of the fairly rapid fall off in scattered intensity with increasing θ . A total of 753 independent intensities were measured, of which 498 with $|F| > 3\sigma(|F|)$ were used in the structure analysis and refinement. Lorentz and polarisation corrections were applied to the data, but no corrections for absorption were made ($\mu R \sim 1.3$).

5.3.(b) Structure Determination and Refinement (x-ray data)

The structure was solved by the symbolic addition method using versions of the X-RAY 70 programs DATFIX. SIGMA2 and PHASE adapted for use on the Glasgow KDF 9 computer. Normalised structure amplitudes (E 's) were calculated for all the observed structure amplitudes. and the 110 reflections with E > 1.4 were used to derive 1148 Σ_{2} relationships. An origin was defined by assigning as positive the signs of the reflections 15 2 2, 6 6 1, and 4 1 11; starting with this basic set of signs, the phase-determining procedure yielded the signs of 94 reflections, and an E-map calculated using these phased E's as coefficients revealed all the non-hydrogen atoms. Structure factors calculated using the atomic co-ordinates obtained from the E-map gave an R-factor of 39% which was reduced to 15.5% after four cycles of full-matrix least-squares refinement with isotropic vibrational parameters, and further to 10.1% after four cycles of block-diagonal refinement with anisotropic vibrational parameters. Hydrogen ators were not included at this stage of the refinement, but a further two cycles of refinement in which hydrogen atoms were included (but not refined) using the co-ordinates obtained from the refinement of the neutron data reduced R to a final value of 7.8%, with R' (= $W\Delta^2/WFo^2$) The weighting scheme applied in the final four cycles is at 0.62%.

represented by the equation $\sqrt{W} = [1 - \exp(-P_1(\sin/\lambda)^2)]/[1+P_2]$ Fo + P_3 Fo² + P_4 Fo³]^{$\frac{1}{2}$}; the final values of P_1 , P_2 , P_3 , and P_4 were 20, 0.0001, 0.0005 and 0.0 respectively. The atomic scattering factors were taken from reference (3). The final x-ray positional and vibrational parameters are given in Tables 5.1(a) and 5.2(a) while Table 5.3. lists the observed structure **a**mplitudes and structure factors calculated from the final least-squares parameters.

5.4.(a) Collection of the neutron data.

Crystals of a size suitable for neutron diffraction were obtained by crystallisation from a saturated solution of α -picoline N-oxide hydrochloride in water over a period of about 5 days. A crystal of dimensions 8 x 6 x 2 mm³ was selected and mounted along <u>b</u>. Integrated intensities for 1,273 independent reflections were measured on an automatic four-circle diffractometer in the DIDO reactor at A.E.R.E. Harwell, using a neutron beam monochromated to a wavelength of 1.172 A. The diffracted intensities suffered from a fall-off in magnitude with increasing Bragg angle similar to that found with the x-ray This was probably due to the high level of incoherent intensities. scattering (50% of the nuclei in the crystal are hydrogens) combined with large atomic vibrational effects resulting from a loosely bound lattice; the latter effect would also explain the fall-off in the x-ray intensities. As a result, only 599 reflections had structure amplitudes which were statistically significant $(|F| > 3\sigma(|F|))$. Absorption corrections

were applied to these observed data using a μ (effective) of 1.88 cm⁻¹, the incoherent scattering cross-section of hydrogen being taken as 37 x 10⁻²⁴ cms.

5.4.(b) Structure Analysis and Refinement (neutron data)

The starting point of the neutron structure analysis was the set of atomic co-ordinates determined for the non-hydrogen atoms during the x-ray analysis. A synthesis of neutron scattering density using the observed neutron structure amplitudes and phases calculated from the x-ray-determined co-ordinates revealed most of the negativelyscattering hydrogen nuclei in their expected positions. One of the two crystallographically distinct water molecules was found to be disordered; the proton which was expected to be at the centre of the bichloride ion also appeared to be disordered, and a difference synthesis with coefficients $[F_{obs} - F_c]$, where F_c was calculated for all atoms except the bichloride ion proton, also showed apparent disorder (Figure 5.1.). To accept this disorder as genuine would imply a Cl-H bond length of about 0.7 A; since the Cl-H bond length in hydrogen chloride is 1.275 Å a Cl-H bond length of 0.7 Å is clearly unacceptable and the 'disorder' must therefore be a diffraction effect. the neutron data being neither sufficiently accurate or numerous to resolve a small negative peak at a point between two large positive peaks.

The 599 'observed' reflections were used in the refinement of the structure. Two cycles of full-matrix isotropic least-squares analysis

were followed by five cycles of anisotropic, block-diagonal analysis, and the R-factor at convergence was 12.17%, with $R'(\Sigma V \Delta^2 / \Sigma F_o^2) = 1.76\%$.

The nuclear scattering-lengths used were 0.661, 0.577, 0.940, 0.990 and -0.378×10^{-12} cm for C, O, N, Cl, and H respectively. Unit weights were used throughout the refinement.

The final neutron positional and vibrational parameters are given in Tables 5.1(b) and 5.2(b), whilst the observed structure amplitudes and calculated structure factors are listed in Table 5.4.

5.5. Description and Discussion of the Structure

Although the x-ray and neutron diffraction analyses of α -picoline-N-oxide hydrochloride monohydrate have not provided particularly accurate bond lengths and angles, they have nevertheless proved worthwhile in revealing an unexpectedly interesting structure.

A density determination had indicated that the stoichiometry of the crystals corresponds to that of a normal hydrated neutral salt $[BH^+Cl^-H_2O]$. The crystal structure analysis, however, has revealed the presence of the two symmetric ions $[B_2H]^+$ (where $B = \alpha$ -picoline N-oxide), and $[HCl_2]^-$. This can be described as a disproportionation, in which a neutral salt has reverted in part to a basic salt $[B_2H]^+$ and in part to an acid salt $[HCl_2]^-$:

 $2[BH^+C1^-H_2O] \equiv [BHB]^+[C1HC1]^-.2H_2O$

A view of the structure along the <u>c</u>-axis is given in Figure 5.2. The $[B_2H]^+$ cations are situated on centres of symmetry and form relatively tightly-bound layers in the <u>bc</u> plane at $x \approx 0$ and $x \approx \frac{1}{2}$. The $[HCl_2]^-$ anions are situated on the two-fold axis parallel to <u>c</u>, and are linked together (<u>via</u> hydrogen bonding) by water molecules to form loosely-bound layers in the <u>bc</u> plane at $x \approx \frac{1}{4}$ and $x \approx \frac{3}{4}$ There is no hydrogen-bonding between these alternate layers of anions and cations.

The bond lengths and angles in the α -picoline N-oxide residue from both the x-ray and neutron analyses are listed in Table 5.5., and the numbering system adopted is shown in Figure 5.3. The dimensions determined by the x-ray and neutron analyses do not differ significantly from each other or from their expected values. A comparison of the α -picoline N-oxide bond lengths with those of some other pyridine N-oxides is given in Table 5.6.

The pyridine ring of the α -picoline N-oxide residue is planar within the limits of experimental error. The mean plane through the ring is defined by the equation (based on the x-ray co-ordinates) -0.1395X +0.2124Y -0.9673Z = -4.698 Å, and the root mean square deviation of the atoms from the plane is 0.008 Å. Atoms 0(1) and C(6) are displaced from the plane of the ring by +0.02 Å and +0.03 Å respectively.

The anisotropic temperature factors (neutron analysis) of the methyl group suggest that, although the group is not rotating freely,

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it is oscillating about the C(1)-C(6) bond with a root mean square amplitude of about 28°. The orientation of the group with respect to the pyridine ring can be defined by the angles which the three methyl C-H bonds subtend with the plane of the pyridine ring. They are, for C(6)-H(5), C(6)-H(6) and C(6)-H(7) respectively, 55.1°, 1.4° and 62.3°.

The oxygen atom O(1) is involved in a short, crystallographicallysymmetric hydrogen bond across the centre of symmetry at 0. $\frac{1}{2}$.0; the $0 \cdots 0$ distance of 2.421(9) A compares with a value of 2.418(11) A for a similar 0 ••• H ••• 0 bond in acetamide hemihydrochloride.⁴ The proton, H(1), was located by the neutron analysis at the centre of symmetry, as expected, but this is not, in itself, evidence that the proton is situated exactly mid-way between the two centrosymmetricallyrelated oxygen atoms; two potential-energy minima less than 0.1 Å on either side of the centre would give the same result in a diffraction experiment as a single potential-energy minimum. The arguments as to whether the proton in a very short, crystallographically symmetric hydrogen bond is truly centred have been widely discussed, and the most favoured interpretation of the accumulated spectroscopic and crystallographic evidence is that the proton is situated in a "broad. flat unharmonic potential. possibly with a bump in the middle no more than 200 cm⁻¹ in height, but also possibly completely flat."⁵

The bond lengths and angles between the bichloride ion and the (two crystallographically distinct) water molecules are listed in Table

Figure 5.4. shows the hydrogen-bonded system involving the 5.7. bichloride ion and water molecules projected along a; the α -picoline N-oxide residues have been omitted for clarity. The oxygen atoms of the water molecules are situated on the two-fold axis at $\frac{1}{4}$, $\frac{1}{4}$, z, while the bichloride ion is situated about the two-fold axis at $\frac{1}{4}$. The water molecules act as hydrogen-bonding bridges between the 1/2. Z. bichloride ions, with the water molecule based on O(3) utilising both of its (crystallographically equivalent) hydrogen atoms for this The water molecule based on O(2) is disordered about the twopurpose. fold axis. using only one of its hydrogen atoms in forming O-H...Cl bonds (effectively ¹/₂H in each bond), the other hydrogen atom being used in forming an O-H...O hydrogen bond along the two-fold axis between adjacent water molecules, with an 0 \cdots 0 distance of 2.723(8) $\stackrel{o}{A}$ (as determined from the x-ray analysis). The $O(2) \cdots Cl$ and $O(3) \cdots Cl$ distances of 2.982(7) Å and 3.062(8) Å respectively (x-ray analysis) are comparable with the average length of O-H...Cl bonds quoted by Pimentel and McClellan⁶ of 3.12(13) A. The standard deviations of the water molecule hydrogen positions (from the neutron analysis) are too large for any meaningful comment to be made about the geometry of the water molecules and their hydrogen bonds.

The most interesting part of the structure is undoubtedly the bichloride ion, $[C1 \cdots H \cdots C1]^{-}$. The bichloride ion was first detected in 1958 by Waddington⁷ during an infra-red study of $N(CH_3)_4^+HCl_2^-$, and since then has been extensively studied, mainly by infra-red

spectroscopy, by Waddington and Salthouse, ⁸ Evans and Lo⁹ and McDaniel and Vallée.¹⁰ Evans and Lo identified two different types of spectra which they dassified as Type I and Type II. Type I spectra they attributed to salts containing a linear but noncentrosymmetric HCl_2^{-} ion (point group C_{ov}) while Type II spectra were attributed to salts containing a linear, centrosymmetric HCl_2^{-} ion (point group D_{oh}). Later work by Stirling, Ludman and Waddington¹¹ on the inelastic neutron scattering spectra and Raman spectra of the Type I salts CsHCl₂ and $CsDCl_2$ showed that the bichloride ion was bent in these salts, having the point group C_{2v} or C_s , and nuclear quadrupole resonance studies by Smith et al¹² of a series of salts containing HCl_2^{-} and DCl_2^{-} ions confirmed Evans and Lo's classification of bichloride ions into two types.

The crystal structures of only two salts containing bichloride ions have been reported; the Type II salt CsCl $(H_3^{0+HCl_2})$ has a Cl \cdots Cl distance of 3.14(2) Å,¹³ and has a mirror plane perpendicular to the Cl \cdots Cl axis, while the Type I salt $Me_4^{N+HCl_2}$ has a Cl \cdots Cl distance of 3.22(2) Å and has no mirror plane perpendicular to the Cl \cdots Cl axis.¹⁴ The bichloride ion in the present structure has a Cl \cdots Cl distance of 2.891(5) Å and a two-fold axis perpendicular to the Cl \cdots Cl axis, thus suggesting a Type II structure. The bending and asymmetric stretching modes, v_2 and v_3 , of the HCl₂ ion cannot be identified in the infra-red spectrum of α -picoline N-oxide hydrochloride monohydrate because of interference from the cation absorptions. How-
ever, a weak, fairly broad peak which can be assigned to the symmetric stretching frequency, v_1 , is observed centred at 278 cm⁻¹ (Figure The symmetric stretching of the cation $[B \cdots H \cdots B]^+$ would also be expected around this region of the spectrum, but since the ion is centrosymmetric, it is infra-red inactive. The value of 278 cm⁻¹ for v_1 can be compared with values of 266 cm⁻¹ and 240 cm⁻¹ for v_1 in the Type II salts $(C_{3}H_{7})_{4}N^{+}HCl_{2}^{-}$ and $(C_{5}H_{11})_{4}N^{+}HCl_{2}^{-}$ respectively.⁹ The higher frequency of v_1 in the present structure suggests a stronger Cl ••• H ••• Cl bond; the bond length of 2.891(5) A is significantly shorter than those of the other two bichloride ions whose dimensions are known, but it is likely that the large thermal vibrations (root mean square amplitude about $0.1 \stackrel{o}{A}$ of the chlorine atoms normal to the Cl ··· Cl axis have caused an apparent shortening of the Cl ··· Cl An estimate of the magnitude of this apparent shortening, distance. calculated using Cruickshank's method, ¹⁵ is 0.13 ⁰. This gives a corrected Cl ••• Cl distance of 3.02 Å, still significantly shorter than the Cl ··· Cl distances in $CsCl_{z}^{1}(H_{3}O^{+}HCl_{2}^{-})$ and $(C_{2}H_{5})_{4}N^{+}HCl_{2}^{-}$.

The shortest intermolecular contacts (those significantly less than the normal van der Waals contact distances for the atoms involved) are listed in Table 5.8.

The methyl groups are related by the two-fold axis, the contact o distance being 3.60 Å (x-ray analysis). This is significantly less than twice the accepted van der Waals radius of the methyl group (4.0 Å), but the groups are not rotating freely and are staggered with respect to each other; the hydrogen atoms of one methyl group are thus able to fit into the spaces between the hydrogen atoms of the symmetricallyrelated methyl group without involving any very short H ••• H contacts, all of the H ••• H contacts between the methyl groups being greater than twice the van der Waals radius of hydrogen (2.4 Å). The shortest such contact is, in fact, 2.74 Å.

A similar argument applies to the two methyl-chlorine contacts of o o 3.68 A and 3.74 A (x-ray analysis).

More interesting are the contacts involving C(5), H(4) and the bichloride ion. The C(5) \cdots Cl distance of 3.50 Å (x-ray analysis) is approximately 0.3 Å shorter than the sum of the carbon and chlorine van der Waals radii, and, more important, the Cl \cdots H(4) distance of 2.40 Å is 0.5 Å less than the sum of the hydrogen and chlorine van der Waals radii (using Pauling's value for hydrogen of 1.2 Å). The C - H \cdots Cl angle is 155°, and it therefore seems reasonable to conclude that C(5) - H(4) \cdots Cl represents a genuine C - H \cdots Cl hydrogen bond.

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TABLES AND DIAGRAMS

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Fractional co-ordinates $(\underline{x}, \underline{y}, \underline{z})$ and absolute co-ordinates (in \underline{X} , with $\underline{X} = \underline{a}\underline{x}$, $\underline{Y} = \underline{b}\underline{y}$, $\underline{Z} = \underline{c}\underline{z}$, and with standard deviations in parentheses.)

(a) X-ray analysis

	x	¥	<u>z</u> ,	<u>X</u>	<u>¥</u>	<u>Z</u>
Cl	0.2073	0,5681	0.3399	3.642(4)	3.857(4)	4.534(4)
N	-0.0122	0.2737	0,3972	-0.215(5)	1.859(7)	5 . 299(6)
0(1)	-0.0286	0.4632	0.4196	-0 . 502(6)	3.145(5)	5.597(6)
0(2)	0.2500	0.2500	0.1965	4.393	1.698	2.621(9)
0(3)	0.2500	0.2500	0.4924	4.393	1.698	6.569(10)
C(1)	-0.0696	0.1409	0.3928	-1.223(8)	0.957(8)	5.240(7)
C(2)	-0.0519	-0.0452	0,3682	-0.911(9)	-0.307(9)	4.91 2(8)
C(3)	0.0234	-0,1023	0.3492	0.410(9)	-0. 695(10)	4.659(8)
<u>c(4)</u>	0.0793	0.0375	0.3524	1.393(8)	0.255(9)	4.702(9)
C(5)	0.0618	0.2230	0.3775	1.086(8)	1.514(10)	5.036(s)
C(6)	- 0 .1 485	0.2170	0.4138	-2.609(8)	1.474(12)	5.520(10)

(b) Neutron analysis

Cl	0.2074	0,5628	0.3421	3.645(15)	3.821(13)	4.562(11)
N ·	-0,0123	0.2736	0.3969	-0.217(7)	1.858(8)	5.294(6)

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Table 5.1 (cont'd)

	<u>x</u>	X	Z	<u>x</u>	<u>Y</u>	<u>Z</u>
0(1)	-0.0306	0.4601	0.4212	-0.538(20)	3 . 124(16)	5.616(19)
0(2)	-0.2500	0.2500	0.1955	-4.393	1.698	2.606(20)
0(3)	- 0 . 2500	0.2500	0.4871	-4.393	1.698	6,499(21)
C(1)	-0.0693	0 .1 463	0,3935	-1,217(9)	0.994(12)	5.249(9)
C(2)	-0.0500	-0.0466	0,3680	-0.877(12)	-0.317(13)	4.910(10)
C(3)	0.0243	-0,1020	0.3488	0,427(12)	-0.693(12)	4.653(1C)
C(4)	0,0811	0.0402	0.3522	1.424(9)	0.273(14)	4.699(12)
C(5)	0.0605	0.2263	0.3758	1.064(11)	1.537(13)	5.015(11)
C(6)	-0.1477	0,2136	0.4139	-2.595(11)	1.451(16)	5.520(12)
H(1)	-0.0973	-0,1590	0,3656	-1.710(3)	-1.08(3)	·4 . 88(4)
H(2)	0.0335	-0,2548	0.3311	0.59(3)	-1.73(3)	4.41(3)
H(3)	0.1365	-0.0022	0.3351	2.40(3)	-0.02(4)	4.47(3)
H(4)	0.1002	0,3596	0.3847	1.76(2)	2.44(3)	5 .1 3(3)
H(5)	-0 .1 529	0.2847	0.4828	- 2.69(3)	1.93(7)	6.44(4)
H(6)	-0,1815	0.0943	0.4071	-3.26(4)	0.64(5)	5.43(6)
H(7)	-0 . 1666	0.3196	0,3619	-2.93(3)	2.17(5)	4.82(4)
H(8)	0.2403	0,3610	0.2424	4.22(6)	2.45(6)	3.23(5)
н(9)	0.2500	0.2500	0.1203	4.39	1.70	1.60(10)
H(10)	0.2377	0.3495	0.4584	4.18(5)	2.37(4)	6.11(3)
H(11)	0.2319	0,6442	0,3518	4.08(3)	4.38(4)	4.69(3)
H(12)	0.0000	0,5000	0,5000	0.00	3.40	6.67

Vibrational parameters (A^2) with standard deviations in parentheses.

(a) X-ray analysis

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	^U 11	U ₂₂	U ₃₃	²⁰ 23	²⁰ 31	²⁰ 12
Cl	0 .1 05(2)	0.096(2)	0.114(3)	-0.018(4)	0.005(4)	0.0 ⁰ 1(4)
N	0.059(4)	0.041(4)	0.038(3)	-0.015(7)	-0.011(7)	0.003(7)
0(1)	0.084(4)	0.038(3)	0.075(4)	-0.024(6)	~ 0,036(7)	-0.014(6)
0(2)	0.153(10)	0.112(9)	0.048(5)	0.000	0.000	-0.094(17)
0(3)	0.167(11)	0.102(8)	0.063(6)	0,000	0.000	-0.029(18)
C(1)	0.054(5)	0.038(4)	0.035(4)	-0.015(8)	-0.005(8)	-0.031(8)
C(2)	0.057(6)	0.050(5)	0.051(5)	-0.019(9)	0.005(9)	-0.045(9)
C(3)	0.074(6)	0.059(6)	0.042(5)	-0.002(10)	-0.005(9)	0.019(11)
C(4)	0.045(5)	0.058(6)	0.065(6)	-0.021(10)	-0.001(9)	0.005(9)
C(5)	0.041(5)	0.066(6)	0.052(5)	0.029(10)	-0.001(9)	-0. 039(10)
C(6)	0.032(4)	0.098(8)	0.075(6)	-0.021(12)	0.021(9)	0.016(11)
(ъ)	Neutron anal;	ysis				
Cl	0.156(12)	0.070(8)	0.077(6)	-0.015(12)	0.063(14)	0.041(16)
N	0.054(4)	0.024(4)	0.043(3)	-0.016(7)	-0.004(6)	-0.005(7)
0(1)	0.113(15)	0.039(9)	0.088(11)	-0.004(17)	-0.063(21)	-0.006(20)
0(2)	0 .1 56(30)	0.057(18)	0,051(10)	0.000	0.000	0.107(41)

0(3) 0.148(26) 0.063(18) 0.045(9) 0.000 0.000 -0.023(39) C(1) 0.039(5) 0.038(6) 0.038(4) 0.001(10) 0.004(8) -0.012(10)

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Table 5.2(b) (cont'd)

	^บ 11	U ₂₂	U ₃₃	^{2U} 23	20 ₃₁	^{2U} 12
C(2)	0.073(7)	0.034(7)	0.038(4)	-0.007(11)	-0.001(10)	-0.089(13)
C(3)	0,056(6)	0.041(7)	0.050(5)	-0.008(11)	0.005(11)	0.007(12)
C(4)	0.026	0.058(8)	0.060(6)	0.010(12)	-0.017(8)	0.002(11)
C(5)	0.056(6)	0.029(7)	0.060(6)	-0.015(12)	0.011(11)	-0.048(11)
C(6)	0 .042 (5)	0.087(11)	0.061(17)	-0.021(15)	0.019(10)	-0.018(13)
H(1)	0.089(18)	0.094(25)	0.137(26)	-0.058(45)	0.056(37)	-0.144(39)
H(2)	0.102(19)	0.067(18)	0.104(18)	-0.037(36)	0.009(32)	0.026(33)
H(3)	0.085(19)	0 . 181(33)	0.027(9)	-0.039(30)	-0.048(22)	0.027(39)
H(4)	0.056(12)	0.098(22)	0.135(21)	-0.034(40)	0.034(29)	-0.1 63(30)
H(5)	0.087(21)	0.254(58)	0.130(26)	-0.166(74)	-0.006(42)	0.137(65)
H(6)	0.112(25)	0.113(39)	0.255(51)	-0.006(81)	0.002(65)	-0.111(56)
H(7)	0.111(23)	0.238(57)	0.118(26)	0.166(67)	0.049(42)	0.216(65)
H(8)	0.115(40)	0.067(38)	0.071(24)	0.011(58)	- 0.095(55)	-0.058(73)
H(9)	0.121(29)	0.039(22)	0.296(96)	0.000	0.000	0.048(48)
H(10)	0.174(33)	0.108(28)	0.078(17)	-0.085(35)	0.073(45)	-0.096(61)
H(11)	0.039(21)	0.050(28)	0.061(19)	-0.147(42)	0.000(29)	-0.120(42)
H(12)	0.098(30)	0.031(20)	0.082(20)	0.000(33)	-0.020(43)	-0.011(36)

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Observed structure amplitudes and final calculated structure factors

(x-ray analysis).

I K L FOESFLALD	4 K L FOPSFLALC	H K L FUESFCALC	H K L F'CES F LALC	H K L F UPS F CALC	P K L F USS F CALC
16 2 0 10.7 -10.2	10 3 1 12 3	• • • • • •			
	10 3 1 12.2 8.7	6 U 5 20.9 -15.5	5 5 1 13.3 13.5	3 6 3 18.4 19.9	2 1 3 9.1 11.1
16 2 3 6.4 -11 3		· U 4 56.4 54.8	5 5 0 16-2 -17-2	3 6 1 14+3 14+8	2 1 2 103.2 203.4
	10 2 / 12.2 -10.6	0 2 24.0 23.4	5 4 8 6.5 -4.7	3 5 6 8.9 -10.1	2 1 1 25.2 32.3
16 2 1 14 6 16 1		e u c 37.1 -37.2	5 4 6 5.8 -9.4	3 5 5 12+2 -12+8	2 0 12 16.4 -8.9
		7 5 3 21.0 -19.1	5 4 5 16.5 17.4	3 5 4 29.9 29.7	2 0 10 7.2 6.3
	10 2 1 12.1 11.2	7 5 1 14.6 13.8	5 4 4 6.7 3.9	3 5 3 18.7 -16.5	2 0 1 37.1 35.3
15 1 4 10.1 -17.5	10 2 0 29.7 28.9	7 5 0 16.3 16.7	5 4 1 17+2 -18+*	3 5 2 10+8 11+5	2 0 6 24.5 -89.8
15 1 2 26.8 30.5	10 1 9 9.6 11.9	7 4 7 20.5 18.3	5 3 10 6.0 7.4	3 5 1 23.9 24.0	2 0 4 143.3 -125.5
15 0 4 25.7 -20.5	10 1 7 13.9 13.6	7 4 5 11.5 -9.9	5 3 9 13.0 -14.7	3 5 0 21+4 -22+8	1 6 5 4.2 9.9
14 3 2 12.6 -11.9	10 1 5 15+8 -17+0	* 7 4 4 7.3 -7.9	5 3 8 5.7 -4.5	3 4 9 9.0 9.0	1 6 4 7.3 5.6
14 3 1 7.3 -7.7	10 1 3 21.4 -20.5	7 4 2 16.2 -15.3	5 3 7 6.0 7.*	3 4 7 10+5 11+0	3+51 1+51 C & L
14 2 6 15.1 19.7	10 1 2 19.6 -19.8	7 4 1 13+6 15+0	5 3 5 7.6 5.2	3 4 6 6.8 -6.8	1 6 7 10+9 -10+4
	10 0 10 9.8 -8.9	7 3 10 13.8 -13.3	5 3 4 5.9 -8.4	3 4 5 23+9 -21+0	1 5 7 7.2 -7.4
	10 0 0 0 0.5 -6.9	7 3 9 8.5 -10.2	5 3 3 14+6 -13+3	3 4 4 14+9 -12+1	1 5 5 11.2 -9.8
14 1 6 12.2 -11.7	10 0 6 22.5 21.7	7 3 5 9.1 8.5	5 3 2 13+7 11+9	3 4 3 10+8 11+6	1 5 7 6+2 -5+5
14 1 5 16+0 17+6	10 0 4 6.2 -4.5	7 3 4 16.8 -16.0	5 3 1 13+0 11+1	3 4 2 16+9 16+0	1 5 1 11+4 10+8
	10 0 2 24.4 -23.8	7 3 0 11.5 11.3	5 3 3 53.8 61.5	3 4 1 31+3 31+0	1 4 10 7.6 7.5
	10 0 0 18.3 -13.9	/ 2 / 6.1 6.3	5 2 11 9+0 5+3	3 3 4 5+7 2+2	1 4 7 10.7 -10.5
	10.0 -11.1	7 2 5 40.2 -41.6	5 2 8 6.8 9.	3 3 7 5.7 -7.9	146 9.3 -8.7
	* 3 / *** ***	7 2 3 25+5 24+8	5 2 / 25.9 -65.5	3 3 6 39.4 -40.0	1 4 4 7.6 8.0
	¥ 3 1 6.6 /./	7 2 7 24.6 -23.2	5 2 6 14+1 13+4	3 3 3 10.2 9.2	1 4 3 20.8 25.6
10 0 0 1968 0040	9 9 0 11-0 12-0	7 2 1 55.7 61.5	5 2 5 8.2 12.5	3 3 2 17.5 20.2	1 4 1 15+8 11+8
13 4 2 13.5 -14.3	9 4 / /.4 6./	7 1 9 24.8 24.1	5 2 4 47.9 +45.5	3 3 0 55+8 -58+3	1 3 11 7.6 5.4
13 3 5 6.9 -6.5	9 4 5 11.4 11.1	7 1 6 7.8 7.2	5 2 3 30.0 27.3	3 2 11 13+3 -12+8	1 3 8 6.7 -3.5
13 3 4 12.9 11.7	9 4 5 1443 1444	7 1 5 37.4 -36.7	5 2 2 41.6 -34.3	7 2 7 7+0 9+0	1 3 7 16.6 -17.2
13 3 0 15+0 -11+5	9 4 4 7.8 -8.8	7 1 4 6.6 -6.4	5 2 1 5+6 -6+9	3 2 5 32.2 -34.2	1 3 4 38.9 37.6
13 2 7 6.7 7.4	9 4 3 18+3 -18+5	7 1 3 14.0 19.1	5 1 10 6.8 -7.9	3 2 4 25.5 24.0	1 3 5 20.7 -21.0
13 2 6 10.9 -12.9	9 4 2 29.8 -31.3	7 1 2 5.9 5.6	5 1 9 9.1 -9.5	3 2 3 39.9 37.1	1 3 2 16.5 -20.6
13 2 4 6+9 -1+2	9 4 1 24+0 -22+7	7 1 1 14•4 8•5	5 1 7 15+3 15+5	3 2 2 50.8 -53.7	1 3 1 30.9 28.5
13 2 3 13+4 -15+0	9 3 9 8.8 -8.2	7 0 8 22+1 22+9	5 1 6 10+0 -***	3 2 1 70+6 76+3	1 3 6 64.5 75.9
13 2 1 11+3 -12+2	9 3 7 7.8 9.4	7 0 6 9.4 10.8	5 1 5 13+8 +10+7	3 1 11 10+2 13+8	1 2 11 7.9 -8.1
13 1 4 11+5 -13+6	9 3 5 10+1 9+3	7 0 4 76.3 -66.0	5 1 4 10+7 -13+0	3 1 10 25+2 24+8	1 2 10 13+1 -13+9
13 1 3 9.3 10.0	9 3 4 14+4 15+5	7 0 2 29+2 -25+2	5 1 3 72.8 -76.9	3 1 9 16+9 14+8	1 2 9 6.1 4.1
13 1 1 15.0 -16.2	9 3 3 6.6 -4.7	6 6 1 21.9 23.7	5 1 2 14.8 -15.9	3 1 7 9.6 -9.1	1 2 * 7.1 8.3
13 0 4 6.4 4.5	9 3 0 9.8 -9.1	6 6 0 9.1 -8.1	5 1 1 85+5 +5+*	3 1 7 57+0 -56+1	1 2 7 5.1 3.3
13 0 2 21+2 -19+5	9 2 7 18+4 +16+2	6 5 5 5.5 1.7	5 0 12 10+0 -11+9	3 1 6 13+4 -15+9	1 2 4 48.4 -48.0
12 4 3 1.5 4.9	9 2 7 15.0 -16.9	6 5 4 12.0 12.0	5 C C 36+2 36+5	3 1 5 32+6 +32+1	1 2 3 10+6 8+8
12 3 6 7.7 -7.5	9 2 5 8+5 8+1	6 5 3 11+3 -12+1	5 0 6 10+5 -10+3	3 4 42+1 4 +7	1 2 7 76.6 76.3
12 3 4 20+3 +21+3	9 2 4 8+2 7+8	6 5 2 14+8 16+1	5 0 4 17.7 -22.3	3 1 3 94+4 94+9	1 1 12 10.0 9.5
12 3 2 20+4 19+5	9 2 3 15+0 13+9	6 5 1 15+0 -14+4	5 E Z E+9 10+5	3 1 2 32+5 35+6	1 1 11 18+5 19+6
12 2 7 12+4 -13+5	9 2 2 15+6 -15+5	6 4 9 11.5 -8.0	4 c 4 11+0 P+7	3 0 12 8.6 -7.5	1 1 10 5+3 +10+1
17 2 5 6+6 -9+3	9 1 7 19.3 16.8	6 4 7 6.0 -1.7	4 6 3 11+6 -11+5	3 0 10 7.4 7.5	0.9- 3.8 * 1 1
12 2 4 13.9 12.0	9 1 6 19.7 -21.7	6 4 7 7.3 6.1	4 6 1 21+4 23+3	3 0 8 8.0 6.7	1 1 7 56+6 -53+3
12 2 3 7.3 5.5	9 1 5 12+5 -11+6	6 4 6 27.5 -27.8	4 u C Z1+3 -16+6	3 0 6 13+9 14+3	1 1 0 25.1 -18.6
12 2 1 7.3 6.9	9 1 4 25+3 -23+6	6 4 4 10+2 -1C+0	4 5 7 14+5 15+4	2 6 3 13.9 -15.5	1 1 4 54+0 +56+6
12 2 0 33.6 -32.4	9 1 3 41.0 -42.3	6 4 3 23.5 -23.9	4 5 5 0+1 -7+5	2 6 1 13+9 16+5	1 1 3 44.6 70.9
12 1 7 9.0 10.2	9 1 2 13+0 12+3	6 4 2 13.3 12.3	4 5 4 22+4 21+=	2 5 5 8.7 6.8	1 1 2 5.5 -5.4
12 1 6 12.5 -13.0	9 1 1 39.4 38.7	6 4 1 73.3 24.4	4 5 3 14.3 -14.2	2 5 2 32+5 31+4	1 1 25.3 -20.1
12 1 3 19.8 -21.3	9 1 0 19-8 13-5	6 3 9 9.4 11.2		2 5 1 9.5 -9.3	1 0 12 10.0 -10.0
12 1 2 25.6 4.9	0 10 14.4 12.6	6 3 6 7.9 7.4		2 4 9 7.3 -5.7	1 0 10 5+0 -1+1
12 1 1 14.9 -14.9	• 0 6 /.1 6.8	6 3 24.2 -23.4		2 4 7 6+5 4+3	1 0 * 55+1 64+9
12 0 6 9+1 3+5	9 0 2 /6.9 -78.2	6 3 4 8.5 7.7	4 4 3 1/10 1010	2 4 6 20.2 -19.4	1 0 + 22.1 -22.5
12 0 6 12.7 -12.4	8 5 - 0.4 -9.0	6 3 2 3/41 -3443		2 4 3 8+3 -6+3	1 0 4 73.3 -56.5
12 0 2 10.4 9.4	8 5 7 18+5 17+6	6 3 1 17.0 16.5		2 4 24.9 -22.8	0 6 4 11.3 7.9
12 0 0 8.6 47.5	8 5 1 10.0 9.1	6 2 1 0 6 4 2 4		2 3 23.7 -24.4	6 6 6 17.6 -22.6
11 4 3 10.0 -11.4	8 4 / 1/.3 -1/.9	6 2 4 11.1 -4.4		2 4 2 8+7 6+1	C 5 8 15+1 -12+4
11 4 6 6446 46342		0 2 F 0.7 -4.8	4 3 3 15.3 -14.4		0 5 4 50 5 29 6
			4 3 2 32.9 -35.5	2 3 10 18.7 -17.5	0 10 1310 1212
1 3 4 10-1 -10 4	0 4 J 2445 2447	0 2 0 14+0 11+0	4 3 1 22.4 -19-1	2 3 9 8.6 0.0	0 4 4 13.1 15.1
			4 2 10 14.9 -15.3	2 3 4 15-3 14-3	
11 3 4 640 4943	- · · J 7 · · · · · · · · · · · · · · · ·		4 2 9 6.2 6.3	2 3 7 10.1 9.4	
11 3 5 19.7 18.3	8 3 5 1440 -124	6 1 10 9.9 -11.9	4 2 8 11+1 +11+2	2 3 6 21.0 17.9	6 4 5 43.4 45.6
11 2 B 10.7 10.1	8 3 4 2348 -22-3	A 1 9 1646 17-5	4 2 7 14+1 +15+5	2 3 5 9.0 -9.6	0 3 6 23.3 -22.0
	R 2 0 17.0 14.4	6 6 24.3 -24.0	4 2 6 15.9 -15.1	2 3 3 23.6 -23.1	0 3 6 46.4 45.1
11 2 4 14.5 -13.2	B 2 7 20ab - 20a5	6 7 12 4 12 9	4 2 5 11+0 -12+1	2 3 2 12.5 4.3	0 3 4 20.5 25.4
1 2 3 .5 +2.7	8 2 6 13+8 -17+6	6 1 6 14.6 14.0	4 2 4 24.7 -23.7	2 3 1 13+5 -11+1	0 3 7 75.6
11 2 2 13.0 13.4	8 2 5 15.7 -15-5	6 1 5 53+1 -53-0	4 2 3 34.9 39.°	2 2 11 8.2 -7.1	0 2 12 . 4.7 A.5
11 1 9 6.4 6.9	8 2 4 12.4 12.4	6 1 4 13.7 11.9	4 2 2 V+6 7+)	2 2 9 13.8 -13.7	0 2 10 44.5 -45.9
11 1 8 741 5-7	1 2 3 32.0 34.3	6 1 3 11.0 -10.9	4] lá 0+6 9+?	2 2 * 12+5 -11+5	5 2 h 13.3 -13.5
11 1 6 17.5 17.3	B 2 1 6.2 -R.7	6 1 2 13.7 12.6	4 1 11 26.7 25.1	7 2 7 18.2 18.5	6 2 6 36.7 IN.P
	8 2 3 K4.8 -64-1	6 1 4 41 4 5 9	4 1 11 7+9 9+1	2 2 5 15+5 16+7	0 2 4 38.5 -40.9
	B 10.2 10.5	6 0 12 13-6 14-8	4 1 7 13+3 -13+4	2 2 4 42+8 41+9	9 2 2 40.6 _42.1
11 1 9 34.2 37 1	B 1 10 B-1	6 0 8 1946 -19-7	4 1 7 33.0 -32.7	2 2 3 29.7 -32.8	0 1 12 17-9 20-4
	8 1 7 H.A .A.S	6 0 6 41-2 -40-5	4 1 6 11+2 -8+4	2 2 2 24.8 31.2	0 1 10 In-4 14 4
L1 0 4 51-5 -51 #	R I 6 R_1 4-8	6 0 4. 7-9 af-R	4 1 4 4t+3 45+4	2 2 1 10.0 11.4	0 1 8 62-1 -62-5
		6 0 7 74-K J2-4	4 1 3 22+3 -23+2	2 1 12 14.9 16.6	0 1 6 49-2 -34-4
		4 0 0 3ALL 224-0	4 1 2 40.3 -39.4	2 1 1 0.9 5.8	0 1 4 137-1 135 3
	0 1 0 1002 1409	E L J A.E 4.1	4 1 1 79.0 -05.4	2 1 30.0 .20.4	0 0 12 13 5 1/1
10 1 8 13.2 -11.9	B J J 20+4 -25+5		4 0 12 4.2 5.*	2 7 6.1 -4.2	
10 3 6 15 5 11 1			4 0 10 6.4 1.9	2 1 4 20.1 -23.1	0 0 0 11. 17 1
10 3 7 13.3 412.1	0 1 1 4J45 #4345	5 5 5 14-0 -13-6	4 U N 21+3 26+3	2 1 17.8 -19.9	0 0 4 242.9
10 3 4 14.3 13.4	a 17 5 12-8 - 18-3 a 17 10 10 10 10 10 10 10 10 10 10 10 10 10	5 5 4 11.9 12.5	4 0 6 144.0 169.4	2 4 6.0 -11.0	1 6 7 1540 ALC

Observed structure amplitudes and final calculated structure factors (neutron analysis).

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Teble 5.4 (cont'd),

H	ĸ	L	Fo	Fc	н	к	L	Fo	Fc	H	κL	Fo	Fc	н	КL	Fo	Fc
777778888888888888888888888888888888888	55555000001111111100000000000000000111111	013460246801145689101346793458356712452600101234567347814568912356703402588	6595371556889749409396570173711350110787898973936316158351048716158716959719744 3464452476654441143123444354434444444444454543445454754754754754356551048716158716158716919744	6789199251514437576615915454545961749305692704654961430172646007310372796902422 32613227665222411300343334343434325245545545569270465496143017264600731037279690422	100000000000000000000000000000000000000	112222222333333344444501111122222333333333445001111111122222333334440001111111222223	792345791235613452404568125681234671202412345678013571230132480134568123674	62121781149530722879254756850762272529309944864704062274725297099448647040622571571755080000557504 5232345462245522257228792547424525475685076227252952994486470406224572454045572454	986793910889804906419665986110176717105776379866038607499006334540445404	334444444000000011111111111110000000111111	52046123466428424500011240112200001222454334504732254545472732462642442246266533245	3307967494541061139021099575963559063559060354220854440851121425756952260547	444498778368948058465210373378357476414724193780486125254787512321447170725 231104793312262531013011243624024221302132211241937803211202231311447170725	111112222355555555555555555555555555555	14435234000001111111100065210006212008400962105121092848421016241083275109762091 11211111112-1076542065210006212084009621051210928484210162410832275109762091 1338234000000111111-112208333344400000111122096210512109284842101624108324400200334441120011	00322139271166377273172013255492417452821846738124037921014621143017122415 222222487325729539222222222223222222222222222222	

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o Bond lengths (A) and angles (degrees) in the α -picoline N-oxide residue (standard deviations in parentheses).

(a) X-ray analysis

N-O(1)	1.352(9)	C(1)-C(6)	1.506(12)
N-C(1)	1.354(10)	C(2)-C(3)	1.400(13)
N-C(5)	1.371(10)	C(3)-C(4)	1.367(13)
C(1)-C(2)	1.343(12)	C(4)-C(5)	1.339(13)
	0(1)····0(1) ^I	2,432(8)	

	N -0(1)···	•0(1) ^I 107.7(0.7)	
C(2)-C(3)-C(4)	118.7(0.9)	C(6)-C(1)-N	116.6(0.7)
C(1)-C(2)-C(3)	121.6(0.8)	C(2)-C(1)-C(6)	125.6(0.8)
N-C(1)-C(2)	117.8(0.8)	C(5) - N - C(1)	122.0(0.7)
0(1) - N -C(5)	118.9(0.7)	C(4)-C(5)-N	120.2(0.8)
O(1) - N - C(1)	119.1(0.6)	C(3)-C(4)-C(5)	119.8(0.8)

(b) Neutron analysis

N-0(1)	1,345(18)	C(1)-C(6)	1.477(15)
N-C(1)	1.322(13)	C(2)-C(3)	1,381(17)
N-C(5)	1,350(13)	C(3)-C(4)	1.389(16)
C(1)-C(2)	1,396(17)	C(4)-C(5)	1.352(18)
	0(1)·····0(1) ^I	2,428(27)	

- C(2)-H(1)1.13(4)C(5)-H(4)1.15(3)C(3)-H(2)1.08(4)C(6)-H(5)1.04(5)C(4)-H(3)1.04(3)C(6)-H(6)1.05(5)C(6)-H(7)1.06(5)
- O(1) N C(1)116.3(1.1) C(3)-C(4)-C(5)117.8(1.0) 120.0(1.1) 121.6(1.0) O(1) - N - C(5)C(4)-C(5)-NN-C(1)-C(2)116.0(0.9) C(5) - N - C(1)123.7(0.9) C(1)-C(2)-C(5)122.1(1.1)124.2(1.1) C(2)-C(1)-C(6)C(2)-C(3)-C(4)118.8(1.1) C(6)-C(1)-N119.8(1.1) $\mathbb{N} = O(1) \cdots O(1)^{\mathbb{I}}$ 108.2(1.4)

C(1)-C(2)-H(1)	117.5(2.0)	N-C(5)-H(4)	111.6(1.7)
C(3)-C(2)-H(1)	120.4(2.0)	C(1)-C(6)-H(5)	112.8(2.3)
C(2)-C(3)-H(2)	116.4(1.9)	C(1)-C(6)-H(6)	109.4(2.9)
C(4)-C(3)-H(2)	124.8(1.9)	C(1)-C(6)-H(7)	112,5(2,2)
C(3)-C(4)-H(3)	118.1(2.4)	H(5)-C(6)-H(6)	112.0(4.4)
C(5)-C(4)-H(3)	124.1(2.4)	H(5)-C(6)-H(7)	104.1(4.3)
С(4)-С(5)-Н(4)	126.8(1.7)	H(6)-C(6)-H(7)	105.8(3.9)

Comparison of the bond lengths of a-picoline-N-oxide determined from the present analysis with those published recently for some other pyridine N-oxides.

Molecule	Ref. Av.	ring C-C(Å)	Av. ring $C_N(A)$	N-0(Å)
a-picoline-N-oxide	X-ray anal.	1.36	1.36	1.35
a-picoline-N-oxide	Neutron anal.	1.38	1.34	1.35
γ -picoline-N-oxide	16	1.379	1.343	1.349
γ -picoline-N-oxide	16	1.396	1.347	1.349
Pyridine-N-oxide	17	1.396	1.345	1.361
Pyridine-N-oxide	18	1.39	1.34	1.35

Bond lengths $\begin{pmatrix} 0 \\ A \end{pmatrix}$ and angles (degrees) in the hydrogen-bonded system involving the water molecules and hichloride ion. Standard deviations are in parentheses.

(a) X-ray analysis

Cl	2.891(5)	Cl0(3)	3.062(8)
Cl 0(2)	2.982(7)	0(2)0(3)	2•723(8)
ClCl0(2)	119 . 2(0 . 2)	0(2)ClC	9(3) 81.6(0.2)
C1 ^T C10(3)	118.4(0.2)	0(2)0(3)	Cl 131.7(0.2)
0(3)0(2)Cl	129.9(0.2)		

(b) Neutron analysis

ClClI	2.950(19)	0(2) - H(8)	0.989(58)	
Cl0(2)	2 . 984(18)	0(2) – H(9)	1.001(99)	
Cl0(3)	2 . 969(19)	0(3) - H(10)	0.807(38)	
0(2)0(3)	2.777(19)	Cl - H(11)	0.714(42)	
Cl ^I (2)	119 . 1(0 . 5)	0(2)0(3)	••••Cl	130.7(0.6)
C1 ^I 0(3)	119.3(0.5)	H(8) - 0(2)	н(9)	129.1(3.2)
0(3)0(2)01	131.0(0.6)	H(8) - O(2)	- H(8) ^T	101.8(3.2)
0(2)Cl0(3)	81.7(0.6)	H(10) - 0(3)	— H(10) ^I	123.0(3.5)

Position I is at $\frac{1}{2}$ - x, $\frac{1}{2}$ - y, z.

Table 5.8.

Intermolecular contacts which are less than the sum of the van der Waals radii of the atoms involved.

Symmetry-related positions other than x, y, z required to describe these contacts are :

I $-\frac{1}{2}-x$, $\frac{1}{2}-y$, z II -x, $-\frac{1}{2}+y$, $\frac{1}{2}-z$ III -x, 1-y, 1-z

Atom A Atom B		Distance (A)		van der Waals distance	
		x-ray anal.	neutron anal.	·	
C(6)	C(6) ^I	3.60	3.63	4 . 0	
C(6)	ClII	3.68	3.72	3.8	
C(6)	ClIII	3.74	3.74	3.8	
C(5)	Cl	3.50	3.48	3.8	
H(4)	Cl		2.40	3.0	



Figure 5.1 : The double minima of the bichloride ion proton, as shown in the difference map (section 5.4).



Figure 5.2 : The crystal structure of a-picoline N-oxide hydrochloride monohydrate projected along the <u>c</u> axis.



Figure 5.3 : The numbering system applied to the a-picoline molecule.



Figure 5.4 : The crystal structure of a-piceline N-oxide monohydrate projected along the <u>a</u> axis, showing the hydrogen bonding between the bichloride ions and the water molecules. The a-piceline N-oxide molecules have been omitted for clarity.



Figure 5.5 : The infra-red spectrum of a-picoline N-oxide hydrochloride

monohydrate.(CaBr disc)

CHAPTER 6

THE CRYSTAL AND MOLECULAR STRUCTURES OF 9-NITROSOJULOLIDINE

AND N, N-DIETHYL p-NITROSOANILINE.

6.1. Introduction

C-nitroso compounds

Although the chemistry of C-nitroso compounds has received considerable attention in recent years, there exists little detailed structural information about the C-nitroso group, especially the aromatic C-nitroso group. The main reason for this lack of structural knowledge of the nitroso group is that most C-nitroso compounds (which are blue if aliphatic and green if aromatic) exist in the solid state as colourless <u>cis</u> and/or <u>trans</u> dimers :



The only x-ray study of a monomeric nitroso compound which has been published is that of p-iodonitrosobenzene.¹ However, the analysis was carried out in projection, and this, combined with the presence of the strongly-scattering iodine atom, led to very high standard deviations in the bond lengths and angles.

Reasonably accurate structural parameters have been obtained for the simple aliphatic nitroso compounds CF_3NO^2 and CH_3NO^3 from gas-phase studies by electron diffraction and microwave spectroscopy respectively, but a microwave study of nitrosobenzene proved to be inconclusive because in order to obtain the C-N bond length and C-N-O angle, a value for the N-O bond length had to be assumed. One group of aromatic nitroso compounds which are monomeric and form crystals eminently suitable for x-ray analysis are the p-nitrosoanilines (I). Since these were among the first nitroso compounds to be identified,⁴ their physical and spectroscopic properties are well-known,⁵ and have been interpreted in terms of a large contribution to the resonance hybrid of the quinonoid structure (II) :



(I)

(II)

An x-ray study of p-nitrosoanilines would thus provide information not only about the aromatic nitroso group, but also on the conformation of the amino group, and the extent to which structure (II) contributes to the resonance hybrid. A large contribution from (II) would be expected to result in the following structural features :

- (1) C-N bond lengths considerably shorter than the C-N single bond
 o
 length of 1.47 Å.
- (2) A planar or almost planar amino group.
- (3) The amino and nitroso groups essentially coplanar with the aromatic ring.

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(4) The bonds between the ortho and meta positions of the aromatic ring shorter than the other ring bond lengths. 6.2. The Crystal and Molecular Structure of 9-nitrosojulolidine

6.2.1. Introduction

9-Nitrosojulolidine (III) was first synthesised in 1971 by MacNicol et al.⁶ Crystals of the compound are well-formed prisms with a steel-blue lustre, although they are green to transmitted light, as expected of an aromatic nitroso monomer. An n.m.r. study⁶ of the internal rotation in 9-nitrosojulolidine showed an appreciable barrier to rotation of the nitroso group about the C-N bond ($AH^{\ddagger} = 17.1 \text{ kcal.mole}^{-1}$), indicating a substantial contribution by the quinonoid structure (IV) to the resonance hybrid :



An x-ray analysis of 9-nitrosojulolidine was undertaken for the reasons discussed at the end of section 6.1., and in addition, to ascertain the conformation of the quinolizidine skeleton and the extent to which,

if at all, it prevents the amino group from achieving coplanarity with the aromatic ring.

6.2.2. Experimental

Crystal Data

 $C_{12}H_{14}N_{2}O, M = 202.17.$ Monoclinic, <u>a</u> = 7.448 (4), <u>b</u> = 8.717 (5), <u>c</u> = 15.890 (9), <u>b</u> = 100.3 (0.1)^O. <u>U</u> = 1015.0 $\stackrel{O3}{A}$, <u>D</u>_m = 1.31, <u>z</u> = 4, <u>D</u>_c = 1.323. <u> $\mu(M_{o}K_{\alpha})$ = 1.0 cm⁻¹</u>. Space group P₂₄/C (No. 14).

Data Collection

A cubic crystal of dimensions 0.6 x 0.6 x 0.6 mm³ was mounted along its <u>b</u>-axis and the space-group and initial cell dimensions were obtained from rotation, Weissenberg and precession photographs taken using CuK_{α} radiation. More accurate cell dimensions were obtained by a least-squares treatment of a number of high-order reflections for which θ values had been measured on a four-circle diffractometer using MoK_{α} radiation.

Integrated intensities were measured automatically on a P.D.P. 8 controlled Hilger and Watts four-circle diffractometer for reflections out to $\theta = 25^{\circ}$. Lorentz and polarisation corrections were applied to the data, but absorption corrections were not considered necessary. The 847 reflections for which $|F| > 3\sigma(|F|)$ were used in the subsequent analysis.

The structure was solved by the symbolic addition method, but only after some difficulty. Normalised structure factors were calculated for the 847 observed reflections, and an origin was defined by assigning positive signs to the reflections 612, 357, and 457. Using the XRAY 70 programm PHASE, a unique solution was obtained without having to assign any symbolic phases. Of the 110 reflections with $|E| \ge 1.5$ used in the solution, phases were obtained for 104, and the E-map which was calculated using these 104 phased E's as coefficients is shown in Figure 6.2.1. It can be seen that there are too many peaks, and this is a common feature of E-maps. Fortunately, it was possible to select only two, equally plausible, sets of peaks corresponding to 9-nitrosojulolidine from the E-map. Each set of co-ordinates gave an R-value of about 60 per cent, which least squares refinement could not lower below 45 per cent; clearly, neither set of co-ordinates was the correct Symbolic addition calculations were then carried out using solution. different origin-defining reflections, but the result was merely to reproduce the same set of E-map peaks at different locations in the unit cell, and R-values for sets of plausible peaks ranged from 65 to 80 per Suspect reflections - one and two dimensional reflections which cent. entered into a large number of Σ_2 relationships - were removed from the solution, but again with no success. However, on closer inspection of the initial solution, it was noticed 6 peaks were common to both the sets of

peaks selected from the E-map, and that these six peaks were, on average, about twice the height of the others. This could be explained by two overlapping half-weight images of 9-nitrosojulolidine separated by an aromatic C-C bond length, as shown in Figure 6.2.2. A similar effect has been reported by Burgi and Dunitz⁷ in the structure analysis of p-methyl benzylidene-p-nitroaniline; the correct solution was an average of two molecular images which were separated by a multiply-occurring interatomic vector. The two sets of 9-nitrosojulolidine co-ordinates were thus averaged, and the co-ordinates thus obtained gave an R-value of 45 per cent, which reduced to 19 per cent after three cycles of full-matrix, isotropic, least-squares.

This 'double-image' effect is an unavoidable result of the limitations of the symbolic addition method when applied to structures containing translational regularities such as six-membered rings. In these circumstances symbolic addition is unable to distinguish between various pseudo-homometric structures because only the strongest |E|values can be used. (The Patterson functions of these pseudo-homometric structures, although different, would be almost identical if computed exclusively with the largest values of E^2). However, this limitation should not be a threat to the application of symbolic addition methods to symmetrical structures, especially those with centrosymmetric space groups, since the detection of a 'double image' effect should lead in a straightforward manner to the correct solution (providing of course, that the images are at the correct location in the unit cell).

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At the end of the isotropic least-squares refinement, a difference map was calculated, which revealed all the hydrogen atoms in their expected positions, as well as disorder in the nitroso group and in one of the trimethylene chains. These features are shown in Figure 6.2.3. along with the atomic numbering system. Refinement was completed with four cycles of anisotropic least squares, in which the block-diagonal approximation was used for all but six of the atoms; because of the high correlations involved, atoms O(1), O(1'), N(1), C(11), C(11') and C(2) were refined by full-matrix least-squares. (N(1')) was considered too close to N(1) to be refined - its coordinates were fixed at the values obtained from the difference map, but it was accorded the same population and isotropic thermal parameters as N(1)). The disordered atoms O(1), O(1'), N(1), C(11) and C(11')had isotropic temperature factors (U) and population parameters (P) refined. as well as their positional parameters. The following constraints were applied during refinement to these thermal and population parameters :

 $P[O(1)] + P[O(1')] = 1 \qquad U[O(1)] = U[O(1')]$ $P[N(1)] = P[O(1)] \qquad U[N(1)] = U[N(1')]$ P[N(1')] = P[O(1')] P[C(11)] + P[C(11')] = 1

The R-value at the end of the refinement was 8.3 per cent. The following weighting scheme was applied during the final cycles of least-

squares refinement :

 $W = X \times Y$ If A x F_{obs} > $|F_{calc}|$ w = 0.000000001If sin θ > B, x = 1, else x = sin θ /B If C > F_{obs} y = 1, else y = C/F(obs)

and the final values of A, B and C were 0.3, 0.5 and 12.0 respectively.

The final atomic co-ordinates and vibrational parameters are listed in Tables 6.2.1. and 6.2.2. respectively. The observed structure amplitudes and corresponding calculated structure factors are listed in Table 6.2.3.

6.2.4. Description and Discussion of the Structure

The bond lengths and angles in 9-nitrosojulolidine are listed in Tables 6.2.4. and 6.2.5. respectively, and confirm the expected large contribution of the quinonoid structure (IV). In particular, the two C-N bond lengths of 1.350(6) $\stackrel{\circ}{A}$ and 1.434(9) $\stackrel{\circ}{A}$ (C(5)-N(2) and C(2)-N(1) respectively) are significantly shorter than the accepted C-N single bond length of 1.47 $\stackrel{\circ}{A}$. The C(5)-N(2) distance of 1.350 $\stackrel{\circ}{A}$ can be compared with similar very short C-N bonds of 1.35(2) $\stackrel{\circ}{A}$ in N,N-dimethylp-nitroaniline, $\stackrel{8}{a}$ and 1.37(1) $\stackrel{\circ}{A}$ in p-nitroaniline, $\stackrel{9}{A}$

The dimensions of the aromatic ring suggest a quinonoid-type structure, but the differences between bonds C(6)-C(1), C(1)-C(2), C(2)-C(3) and C(3)-C(4) are not statistically significant. However,

the bonds at the amino end of the ring - C(4)-C(5) and C(5)-C(6) are significantly longer than the other ring bonds, and this is a feature found also in both p-nitroaniline and N,N-dimethyl-p-nitroaniline. The aromatic ring is planar within the limits of experimental error, and the equation of the mean plane through the ring is given in Table 6.2.7. along with the displacements of the atoms from the plane. The displacements of C(9), N(2) and C(10) from the plane by +0.14 Å, +0.03 Å and +0.09 Å respectively, indicate that the amino group.is nonplanar. However, the deviation from planarity is small, and is probably the result of crystal packing forces, rather than any residual

The nitroso group dimensions, which have been less accurately determined than had been hoped because of the disorder described in section 6.2.3, also reflect a large contribution from structure (IV). The C-N and N-O bond lengths of 1.434(9) $\stackrel{\circ}{A}$ and 1.245(11) $\stackrel{\circ}{A}$ respectively can be compared with those in nitrosomethane of 1.48 $\stackrel{\circ}{A}$ and 1.21 $\stackrel{\circ}{A}$. Since the C-N-O angle in structures III and IV is of the type X=N-Y in both cases, a large contribution of IV to the electronic structure of III would not be expected to have much effect on the C-N-O angle; the value determined for the angle C(2)-N(1)-O(1) of 112.8° agrees well with the normal value for an X=N-Y angle¹⁰ of 113°.

sp² character in the nitrogen bonding orbitals.

To enable efficient overlap of the C(2) and $N(1) p\pi$ orbitals, the nitroso group has to be more or less coplanar with the aromatic ring. It makes an angle of only 2.8° with the plane of the ring, and in order to relieve what would otherwise be a very short intramolecular contact between O(1) and H(2) of about 2.4 $\stackrel{o}{A}$, angle C(3)-C(2)-N(1) has opened to 128°. The resulting 0 ···· H distance of 2.63(6) $\stackrel{o}{A}$ corresponds to a normal van der Waals contact (2.6 $\stackrel{o}{A}$).

The trimethylene chains of the quinolizidine adopt the expected conformations, with C(11) above, and C(9) below, the plane of the The resulting torsion angles are given in Table 6.2.8. molecule. The conformations of the two fused six-membered rings of the quinolizidine skeleton can be likened to the 'envelope' conformation of cyclopentane with only one atom markedly out of plane with the others; in one ring the envelope flap is pointing upwards, in the other ring, downwards. This 'up-down' conformation is, however, adopted by only 63 per cent of the julolidine molecules; in the other 37 per cent, both rings have their envelope flaps pointing downwards, and it is this disorder (of C(11)) which determines the amount of disorder in the nitroso group. Figure 6.2.4. shows the packing of the nitrosojulolidine molecules in the unit cell as viewed down a. It can be seen that the molecules pack in centrosymmetric head-to-tail pairs, in which the nitroso group of one molecule fits neatly into the amino end of the centrosymmetrically-The orientation which the nitroso group adopts is related molecule. therefore greatly influenced by the conformation of the quinolizidine skeleton. In the case of the predominant conformation, in which one flap is up and the other down, the nitroso group points in the direction of the downward flap, (the alternative orientation, 180° away,

would involve a very short $0 \cdots CH_2$ contact of 3.41 Å). In the case of the minor conformation, in which both flaps point downwards, there is little difference energetically between the two orientations, and the nitroso group adopts each orientation to an equal extent. The resulting populations of the two orientations should thus be in the ratio $63 + \frac{1}{2} \times 37 : \frac{1}{2} \times 37 = 81.5 : 18.5$. The ratio of the population parameters obtained from the least-squares refinement is 83:17.

The disorder of the trimethylene chain involving atoms C(10), C(11) and C(12) has resulted in unsatisfactory bond lengths and angles between these atoms, and the large vibrational amplitudes (about 0.1 $\stackrel{\circ}{A}$) of the other trimethylene chain involving atoms C(7), C(8) and C(9) has caused an apparent shortening in the bond lengths of C(7)-C(8) and C(8)-C(9) from the normal C-C bond length of 1.54 $\stackrel{\circ}{A}$ to 1.48 $\stackrel{\circ}{A}$ and 1.50 $\stackrel{\circ}{A}$ respectively.

All the intermolecular distances in the structure correspond to normal van der Waals contacts, but the shortest contacts involving the nitroso group are listed in Table 6.2.8. The aromatic rings of the centrosymmetrically-related head-to-tail pairs of nitrosojulolidine molecules are 3.70 Å apart. This is 0.3 Å more than the normal van der Waals contact distance between aromatic rings, the increase being due to the bulky trimethylene chains in the quinolizidine end of the molecules.

TABLES AND DIAGRAMS

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Table 6.2.1

Final fractional co-ordinates $(\underline{x}, \underline{y}, \underline{z})$ with population parameters (\underline{p}) other than unity. Standard deviations are in parentheses.

	x	У	<u>Z</u>	p
N(1)	-0.3292(12)	0.7968(9)	0,3888(6)	0.83(2)
N(1')	- 0 , 365	0.817	0.405	0.17(2)
N(2)	0.2256(6)	0.8124(5)	0.6744(3)	
0(1)	-0.4721(8)	0.8682(7)	0.3922(4)	0 。 83(2)
0(18)	-0.3715(40)	0.7830(34)	0.3482(21)	0.17(2)
C(1)	-0.0404(8)	0.7313(7)	0.4662(3)	
C(2)	-0.2019(8)	0.8058(7)	0.4686(3)	
C(3)	-0.2202(7)	0.8831(7)	0.5433(4)	
C(4)	-0.0823(8)	0.8847(7)	0.6135(4)	
C(5)	0.0846(7)	0.8099(6)	0.6082(3)	
C(6)	0.1006(7)	0.7317(6)	0.5316(3)	
C(7)	0,2992(9)	0,6560(8)	0.5238(4)	
C(8)	0.3844(10)	0.6111(9)	0.6078(5)	
C(9)	0,4019(8)	0.7449(9)	0.6680(4)	
C(10)	0.2176(9)	0.8971(9)	0.7535(4)	
C(11)	0.0793(16)	1.0072(14)	0.7471(6)	0.63(3)
C(11')	0.0196(40)	0.9536(34)	0.7575(16)	0.37(3)
C(12)	-0.0977(11)	0.9607(11)	0.6971(6)	
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Table 6.2.1. (cont'd)

	<u>x</u>	Y	<u>Z</u>
H(1)	-0 _• 029(8)	0.683(7)	0.413(4)
H(2)	-0.319(8)	0,931(7)	0.551(4)
H(3)	0.245(8)	0.562(7)	0.483(4)
H(4)	0 . 339(8)	0.716(7)	0.490(4)
H(5)	0.505(8)	0.580(7)	0.595(4)
H(6)	0.324(8)	0.521(7)	0.639(4)
н(7)	0.502(8)	0.830(7)	0.644(4)
H(8)	0.459(8)	0.728(7)	0.715(4)
H(9)	0.340(8)	0.934(7)	0.767(4)
H(10)	0,226(8)	0,826(7)	0.806(4)
H(11)	0.062(8)	0.045(7)	0.815(4)
H(12)	0.107(8)	0.082(7)	0.715(4)
H(13)	-0 . 154(8)	0.900(7)	0.720(4)
H(14)	-0 .1 95(8)	1.026(7)	0.687(4)

Table 6.2.2.

	Vibrational	parameter	(\mathbb{A}^{2}) with	n standard	deviations	in parentheses.
	U ₁₁ or U _{iso}	U ₂₂	⁰ 33	^U 12	^U 13	^U 23
N(1)	0.082(2)					
N(2)	0.058(3)	0.057(3)	0.053(2)	-0.005(2)	0.005(2)	0.001(2)
0(1)	0.088(3)					
C(1)	0.065(4)	0.073(4)	0.050(3)	0.002(3)	0.009(3)	0.005(3)
C(2)	0.066(4)	0.058(3)	0.057(3)	-0.009(3)	0.004(3)	0.012(3)
C(3)	0.045(3)	0.054(3)	0.098(4)	0.007(3)	0.013(3)	0,016(3)
C(4)	0.060(4)	0.061(4)	0.071(4)	0.003(3)	0.015(3)	-0.009(3)
C(5)	0.050(3)	0.038(3)	0.055(3)	-0.005(2)	0.009(2)	0.004(2)
C(6)	0.056(3)	0.046(3)	0.055(3)	-0.051(2)	0.007(2)	0.001(2)
C(7)	0.073(4)	0.083(5)	0.070(4)	0.014(4)	0.017(3)	-0.005(3)
C(8)	0.075(4)	0.094(5)	0.092(5)	0.030(4)	0.015(4)	0.003(4)
C(9)	0.050(4)	0.104(5)	0.080(4)	0.006(3)	-0.007(3)	0.007(4)
C(1 0)) 0.082(4)	0.095(5)	0.061(4)	-0.014(4)	0.004(3)	-0.015(4)
C(11)) 0.064(4)					
C(12) 0.083(5)	0.130(7)	0.123(6)	0.020(5)	0.026(4)	-0.044(6)
H(1)	0.06					
H(2)	0.07					
H(3)	0,08					
H(4)	0.08					
H(5)	0.09					

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Table 6.2.2. (cont'd)

	iso
H(6)	0.09
H(7)	0.08
H(8)	0.08
H(9)	0.08
H(10)	0.08
H(11)	0.06
H(12)	0.06
H(13)	0.11
H(14)	0.11

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Table 6.2.3

Observed structure amplitudes and final calculated structure factors. (xw)

7.5.1	6 61 92	5 49 +92	4.5.1	2 97 9	3.4.1
	-1 70 -154	3 98 132		1 89 - 38	31-10
4 52 +58		2 124 155	10 29 +6	P 50 -161	14 47 +00
5 47 -62	6,1,L	8 46 22	8 63 -115	•1 30 11	13 41 -64
-1 46 62		-1 38 63	7 162 -187	-2 329 274	12 35 -19
+2 33 =49	•4 79 •95	-2 55 82	6 106 +136	-3 58 177	10 38 +55
•1r 48 65	-6 45 -114	•3 24 •49	5 124 +104	-4 208 195	9 128 122
	-7 48 -55	-5 63 92	4 24 15	-6 34 -63	8 48 135
7,4,L	•8 28 19	-6 139 -180	2 41 -43	-9 31 36	6 51 =154
	-10 88 99	-7 83 84	1 86 178	-18 80 13A	5 37 -56
5 39 61	-12 146 210	-8 30 23	0 72 •78	-11 42 -3	3 52 30
4 35 +73	-13 43 -23	•9 68 121	•1 27 •66	•15 54 •93	2 47 -124
3 38 36	4.0.1	-1r 28 40	42 20 441	•16 JJ •50	1 45 43
1 36 -44	0,0,1	-12 54 -129	- 18 - 132	4.2.1	8 135 103
-1 16 78	19 45 79	-12 56 -129		•,•,(-3 -34 48
•9 51 •5H	8 .34 .45	5.1.1	•7 194 225	19 114 -168	-3 51 116
	6 45 -11	51112	R 92 146	A 39 = 17	-5 146 -180
7.3.1	-2 59 63	10 71 -106	=9 67 78	2 184 -21	•/ /8 •18
	-4 78 -86	9 58 99	•13 33 •71	•4 458 431	-8 157 258
1 84 -130	-10 50 -69	8 33 - 39		-6 110 167	-9 81 119
8 73 79	-14 56 92	7 48 +/1	4,4,L	=12 41 89	-10 36 51
■1 80 =61		6 52 -47			•11 48 +17
•2 46 46	5,8,L	5 93 -107	12 45 -93	3,9,1	•12 33 53
•3 38 91		4 142 -143	11 36 -33		
•4 44 35	0 32 -1	3 135 -104	7 47 72	3 51 +54	3,3,6
-/ 38 -88	-1 32 88	2 08 P34	0 32 20	-3 42 8/	14 13 11
7.2 .	A.7 1	1 07 100		•4 JD 23	14 32 51
11216	31/12	el 44 - 27	2 25 -101	-0 00 93	12 31 84
1 13 54	4 47 +47	=2 112 =144	1 83 =2	3. 8.1	11 41 -04
•1 58 •68	8 59 98	-3 80 -39	0 144 -136	5, 576	9 53 25
+2 63 4K	-2 6/ 74	-4 98 141	-2 43 158	8 57 -97	8 75 +78
•4 63 •96	•7 39 32	•5 75 •172	•3 36 •18	6 34 • 3	6 49 •1
•5 30 •45		-6 95 134	•5 36 35	=6 97 115	5 49 +18
	5,6,L	-7 46 57	-6 117 -112	-7 60 -117	4 49 90
7,1,6		-8 35 40	-7 106 -141		3 166 -165
	5 44 35	-9 97 127	-8 38 -69	3,7,6	2 282 256
7 32 -31	1 71 +119	-10 149 147	•9 78 65		1 47 75
5 29 -21	-1 73 -77	•11 41 34	-10 97 156	9 59 108	8 262 -259
3 31 37	-2 46 67	-12 86 77	=12 31 23	8 124 137	•1 258 •271
2 58 -91	•4 31 •23	-13 41 -89	-14 34 -3	7 78 74	•2 65 ~167
1 91 78	•5 30 31	E 1 1	4.3.4	3 33 3	
•0 34 •03	•/ 36 •13	3,0,1	-,3,6	-2 33 74	
-11 35 -43	5.5.1	12 86 -82	8 54 67	•4 78 •38	*6 125 63
att 22 -42	37370	8 112 1182	7 72 48	-5 185 -146	•7 42 •68
7.0.1	6 31 -56	4 78 27	6 148 297	-6 121 -194	+8 56 +84
	5 53 +43	2 76 =241	5 103 83	=7 54 =51	-18 87 -94
6 42 183	•1 28 •48	P 23 •91	4 24 -30	•9 34 •6	-11 66 66
+6 42 41	•6 28 = 39	-2 34 -195	3 87 -148		-12 39 -118
•8 42 •137	=7 53 =51	#4 52 6B	1 90 92	3,6,6	-15 54 99
-10 33 29		-6 152 231	-2 64 110		•17 38 •12
=14 42 51	5,4,L	-8 48 -36	-4 125 -54	9 104 -167	• • .
		-10 111 -112	-0 80 -/8	8 97 152	3,2,2
6,6,L	7 42 62	•12 97 209		A 61 74	0 12 61
	1 66 65	•14 31 0e	-0 147 -128	4 28 27	A 13 1A
•1 30 •19 •0 30 •19	-1 41 63	4.8.1	-10 29 17	3 31 118	5 98 -149
-1 33 48	-1 -1 -03	-, -, -, -	•11 32 60	2 36 71	4 73 128
6.5.1	-4 49 -99	6 91 =127	-13 54 -65	•1 46 •191	3 313 +248
	•6 78 129	2 34 96		-2 39 -64	2 150 49
4 43 47	-7 47 -86	-6 49 43	4,2,6	-5 238 292	1 72 182
-1 40 -42	-8 30 -25	-7 37 -21		•6 118 •152	8 62 -115
⇒3 79 +81	•9 32 5	-8 53 91	12 43 75	•7 34 55	*1 129 17
•6 48 63	-10 47 50	•9 31 -67	11 83 70	-8 108 -113	-2 242 -298
•7 <u>31</u> •2P	-15 38 -39		18 46 186	•9 28 •/1	•3 312 •234
		4,7,6	4 61 146	3. 5.1	
8,4,L	5,3,1	1 43 43	J J4 110 D 124 00	31311	+6 33 +12
• • • • • •	10 71 -17	/ 42 03	1 117 =52	18 42 .43	•7 25 •11
7 30 64		5 07 113 4 48 A	•1 12 161	9 56 -46	*8 25 +124
0 0/ 052	y 30 -38 6 61 64	2 54 114	•2 24 •77	7 142 -224	•9 58 7
J 29 423	5 188 225	H 35 74	+3 118 +115	6 38 57	•13 76 •92
-0 00 00 -10 17 41	4 215 250	-1 32 109	•4 169 -266	5 61 167	•11 83 73
=12 31 =25	3 103 76	•7 41 =56	•5 74 78	4 58 -92	•12 27 •16
-46 -40	8 64 +62	•9 53 •73	-7 76 69	3 26 67	
6,3.L	-1 41 -29	-	•8 89 52	2 33 -56	3010L
	-3 69 90	4,6,L	-10 94 -178	a 6a 167	
8 51 196	-5 121 120		•11 58 •183	-1 62 -164	13 48 +26
6 38 •32	=8 66 =17	7 38 +57	-12 45 -73	•2 45 96	9 44 57
•9 29 43	-9 148 -204	6 97 132		-3 68 31	8 20 408
•12 36 •46	-10 107 -173	5 50 •2	4,1,1	JU 90	
-13 38 35	•11 58 •53	3 34 -78	12 74 -71	-0 141 100	4 28 -180
•14 45 +94		p 61 63	18 54 -34	•7 253 264	3 21 +110
	3,2,6	-2 JU 78	6 43 53	•9 63 •157	2 63 +48
0,2,L		e13 45 48	7 37 +28	-18 48 97	1 64 79
	7 45 -54	-10 -0 40	5 78 65	-12 59 43	•1 307 178
7 54 0131	6 35 -12		3 34 -2		•2 275 136

Table 6.2.3 (cont'd)

	1.1.1	-1 67 -19	2.1.1	-12 AR 194	2 21 -12	2 29 -1A
		-4 42 56			1 120 .92	
- 3	87 =18	•5 24 58	13 41 74	1.5.6	8 124 52	8.5.L
- 4	47 -113	-6 48 -21	11 47 -36		-3 734 647	
• 5	85 -97	•7 45 56	10 66 37	10 27 -11	-4 78 -43	11 60 -76
	44 37	•12 49 •124	9 4.5 =75	7 32 -41	-5 73 -735	16 51 -83
+11	38 31		8 46 -R4	6 51 40	-6 2/4 -95	9 32 +42
•12	45 =1.5	2.4.6	7 113 •71	5 57 -195	-7 357 -351	8 47 •27
+13	31 - 38		6 257 -289	4 34 - 57	-8 169 -73	7 27 8
•16	44 -41	11 67 98	5 183 203	3 235 215	-9 96 228	6 27 +46
		10 198 -287	4 163 -47	2 56 +283	+18 33 +53	5 36 99
	3,8,6	9 131 142	2 33 36	1 211 235	-11 32 139	4 65 -53
		7 52 +53	P 69 115	-: 71 -38	+15 79 =137	3 191 229
14	28 -46	5 82 29	-2 51 98	-2 156 133	-16 83 128	1 29 +42
16	J5 =72	4 66 116	-3 179 92	=3 165 =145	-17 44 -72	
8	47 79	3 22 -7	-4 124 -4H	•4 26 •49		B.4,L
	337 =138	2 69 -142	-6 38 59	-5 25 163	1.1.4	
2	123 =57	1 107 141	=7 .57 =6	-6 81 -73		15 31 -23
۲	40 157	2 173 132	-R 213 258	-11 87 -193	14 62 -123	11 46 -19
• 2	312 460	-1 139 176	-9 237 -199	-13 34 -76	13 71 64	18 77 •177
-4	210 167	-2 154 93	•11 37 77	-16 42 -58	12 159 169	9 118 +132
-6	60 14	-3 321 -232	-13 44 -21		11 97 -124	8 189 +178
• 8	66 26	-4 579 646		1,4,6	10 39 32	0 784 240
-10	184 91	-5 253 -237	2.0.1		6 200 +200	2 542 4198
-14	27 21	•0 00 04				100 235
-10	24 4103	•• 31 •/0	12 43 442		4 341 443	3 34 42
		PY 34 -14	117 40 44 8 67 -47	10 44 10	4 641 40C	
	e,10,L	•11 J4 •47	6 449 -644	8 AL 38	2 76 187	9 71
,	44 - 30		0 440 4043 A 510 447	7 104 -43	1 12 184	
- 1			- J/E -J42 2 361 646	A 128 -110	0 248 62A	8.3.1
÷1	JZ 11	-15 30 -57	0 106 117	5 54 -15	•1 270 •1A1	
	2 0 1	-16 33 -45	-2 621 -144	4 51 148	-2 557 -177	15 15 -28
	c,,,,	-10 33 -45	=2 021 =304 #4 146 =142	j QA +33	-3 527 449	14 52 +64
1	42 14	2.3.1	•6 37 173	2 2/ 100	#4 39 81	13 65 -56
-2	16 47	ETSTE	-A 11A 290	A 227 238	•5 65 •18	12 36 42
	75 114	14 32 43	•10 125 82	•1 137 -140	-6 521 568	11 42 100
-4	86 110	12 56 71	=12 59 =178	•2 247 273	-7 185 124	18 118 188
		18 188 -113	•14 37 •45	+3 358 +268	-8 152 138	9 39 118
	2.8.1	9 158 185	•••	-4 176 51	•9 98 •72	7 73 30
		8 57 =51	1.18.6	-5 59 87	-18 55 -168	5 320 +371
9	33 •26	7 68 -54		-8 87 122	-11 87 112	4 291 262
4	38 -84	6 78 188	•4 33 •29	-9 26 -31	•12 53 •2	3 281 -535
2	66 108	5 80 -60		-10 36 12	•15 31 44	2 162 42
U	56 11/	3 28 112	1,9,1	-11 35 -22		1 346 184
•2	57 .80	12 149 -188		-12 42 -87	1,0,6	
• 3	59 -102	1 73 170	4 38 21	-14 53 -85		8,2,L
•6	70 11V	0 258 +223	n7 65 73	-16 48 -71	14 138 -132	
•9	31 47	-1 54 64	•3 /8 104	-17 51 78	12 286 -242	16 84 109
		=3 40 59		_	18 132 -185	15 58 66
	2,7,1	•4 269 219	1,8,6	1,3,1	8 189 -114	14 105 12/
		-5 228 -174			0 35 025	12 69 6/
10	65 89	-6 104 14	10 30 -57	13 37 -17	4 438 383	11 110 10/
4	36 -93	•7 132 90	7 32 -19	12 32 19	2 398 •/89	
1	63 -112	-6 66 -282	4 OU 0/		-2 505 443	4 311 -178
•	64 137	-9 81 93	2 /1 /1	9 10 12	-4 601 666	
•	82 -152	•10 /1 •10/		7 22 83		4 284 267
• 3	20 •14	•11 3/ •1/		/ 22 JJ	-8 204 100	3 308 440
	141 -522	•12 83 122	- 39 117	a 111 212	-12 98 146	2 648 -471
• 7	52 457		-10 44 -15	2 62 12	-16 47 -58	1 386 -162
	• 6 69	<i>e121</i> 2		1 272 -269	-18 39 -99	8 698 +847
	2.6.1	12 80 119	1.7.1	P 98 39		
		11 122 =145		•1 235 187	0,10.L	8,1,L
11	35 -15	10 01 111	10 30 0	-2 185 +132		
	59 -44	9 68 •131	8 49 • 37	•3 42 •42	1 35 49	16 32 +43
á	72 109	8 38 52	4 78 -52	-4 118 154	8 68 49	13 64 59
ě	47 .30	7 47 -87	3 85 -111	•5 244 •222		12 73 184
2	118 +164	6 226 91	2 46 89	-6 211 -284	#,8,L	11 24 +57
ī	88 +113	5 187 108	1 58 +97	-8 128 193		18 89 -81
ė	65 -97	4 148 127	-5 43 -98	-9 78 -189	18 48 -26	8 123 211
-1	24 8	3 23 - 38	•6 42 B2	-13 29 16	5 31 77	7 64 +4
• 3	133 146	2 65 -208	-9 34 28	-15 32 -58	1 28 14	6 56 88
. 4	71 .99	1 57 -49	•11 53 84			5 69 268
•6	164 97	0 55 1		1.2.L	#,7,L	4 253 +212
•6	165 -241	-1 373 -515	1,0,6			3 347 344
•7	68 +176	-2 232 -163		14 64 78	8 29 37	2 423 449
		-3 231 265	14 37 -12	13 83 +145	4 /3 -13	1 482 +72
	2,3,1	•4 127 =251	6 34 •9	12 191 234	3 47 •44	
		•5 197 189	4 74 +68	11 175 -298		
	65 61	=6 149 =130	3 91 121	18 38 -14	# #0.i	14 344 - 144
		•7 58 55	2 158 -167	A 155 18A		14 380 428
5	26 +38					
5	26 - 38 45 - 144	-8 77 -41	1 30 -15	8 109 10J 7 374 377		14 11 41
532	26 +38 45 -144 165 188	-8 77 -41 -18 68 -64	1 30 -15 -1 47 -75	7 273 377	9 98 41	10 35 91
532	26 + 38 45 -144 165 188 152 137	-8 77 -41 -10 68 -64 -11 30 28	1 30 -13 -1 47 -75 -2 36 -86	6 159 103 7 273 377 6 159 17	10 32 03 9 96 41 8 27 9 5 28 11	12 50 0 16 35 91 8 243 428
5321	26 + 38 45 - 144 165 188 152 137 25 + 27	-8 77 -41 -18 68 -64 -11 38 28 -12 41 7	i 30 -15 -1 47 -75 -2 36 -86 -5 27 8	<pre> 169 103 7 273 377 6 159 17 5 53 -34 4 53 pt </pre>	10 32 03 9 90 41 8 27 9 5 70 11 4 40 -40	12 DU U 16 35 91 8 243 428 6 62 4134 2 256 44
5 3 2 1 8 -1	26 + 38 45 - 144 165 188 152 137 25 + 27 51 113	-8 77 -41 -12 68 -64 -11 30 28 -12 41 7 -15 63 117	1 30 -15 -1 47 -75 -2 36 -86 -5 27 8 -7 28 79	<pre> 169 103 7 273 377 6 159 17 5 53 -34 4 53 +88 3 164 - 34 </pre>	10 32 03 9 90 41 8 27 9 5 76 11 4 40 -48 3 25 -48	14 34 91 14 33 91 8 243 428 6 62 -134 2 258 44

Table 6.2.4.

Bond lengths $(\overset{o}{A})$ with standard deviations in parentheses.

N(1) - O(1)	1.249(10)	C(6) - C(7)	1.515(9)
N(1) - C(2)	1.434(9)	C(7) - C(8)	1.478(9)
C(1) - C(2)	1.377(9)	C(8) - C(9)	1.499(11)
C(2) - C(3)	1.393(9)	C(9) - N(2)	1.465(8)
C(3) - C(4)	1.378(8)	N(2) - C(5)	1.350(6)
C(4) - C(5)	1.427(8)	N(2) - C(10)	1.468(8)
C(5) - C(6)	1.420(7)	C(10)- C(11)	1.400(14)
C(6) - C(1)	1.343(7)	C(11)- C(12)	1.477(13)
	C(12) - C(4)) 1.506(11)	
C(1) - H(1)	0.96(6)	C(9) - H(8)	0.81(6)
C(3) - H(2)	0.87(6)	C(10) - H(9)	0,95(6)
C(7) - H(3)	1.05(6)	C(10) - H(10)	1.04(6)
C(7) - H(4)	0.92(7)	C(11) - H(11)	1,16(6)
C(8) - H(5)	1.00(6)	C(11) - H(12)	0,87(6)
C(8) - H(6)	1.07(6)	C(12) - H(13)	0.78(7)
C(9) - H(7)	1.15(6)	C(12) - H(14)	0.92(6)

Table 6.2.5

Bond angles (degrees) with standard deviations in parentheses.

C(2)	-	N(1)	- 0(1)	112.6(0.7)	C(7)	-	C(8)	-	C(9)	109.9(0.6)
C(1)	-	C(2)	- N(1)	113.4(0.6)	C(8)	-	C(9)	-	N(2)	112.3(0.5)
C(3)	-	C(2)	- N(1)	128.4(0.6)	C(9)	-	N(2)	-	C(5)	121.8(0.5)
C(1)	-	C(2)	- C(3)	118.1(0.5)	C(9)	-	N(2)	-	C(10)	116.0(0.5)
C(2)	-	C(3)	- C(4)	121.5(0.5)	N(2)		C(5)	-	C(6)	120.2(0.5)
C(3)	-	C(4)	- C(5)	119.0(0.5)	N(2)	-	C(5)	-	C(4)	121.2(0.5)
C(4)	-	C(5)	- C(6)	118.7(0.4)	N(2)		C(10)	-	C(11)	115.2(0.6)
C(5)	-	C(6)	- C(1)	119.3(0.5)	C(10)	-	N(2)	-	C(5)	122.0(0.5)
C(6)	-	C(1)	- C(2)	123.4(0.5)	C(10)	-	C(11)	-	C(12)	115.6(0.9)
C(1)	-	C(6)	- C(7)	121.4(0.5)	C(11)	-	C(12)	-	C(4)	113.0(0.8)
C(5)	-	C(6)	- C(7)	119.3(0.4)	C(12)		C(4)	-	C(3)	123.6(0.6)
C(6)	-	C(7)	- C(8)	112.3(0.6)	C(12)	-	C(4)	-	C(5)	117.4(0.5)
C(2)	-	C(1)	- H(1)	116(3)	C(2)	-	C(3)	-	H(2)	124(4)
C(6)	-	C(1)	- H(1)	120(4)	C(4)	-	C(3)		H(2)	115(4)
C(6)	-	C(7)	- H(3)	106(3)	C(7)	-	C(8)	-	H(5)	104(3)
C(6)	-	C(7)	- H(4)	108(4)	C(7)	-	C(8)	-	H(6)	114(3)
C(8)	-	C(7)	- H(3)	113(3)	C(9)		C(8)		H(5)	112(3)
C(8)	-	C(7)	- H(4)	117(3)	C(9)	-	C(8)	-	H(6)	105(3)
H(3)	-	C(7)	- H(4)	100(5)	H(5)	-	C(8)	-	H(6)	112(5)
C(8)	-	C(9)	- H(7)	106(3)	N(2)	-	C(10)	-	H(9)	100(4)

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Table 6.2.5. (cont'd)

113(4)

117(4)

114(4)

96(5)

116(4)

123(4**)**

103(5)

107(4)

91(6)

C(8)	-	C(9)	- H(8)	114(5)	N(2)	-	C(10) - N(10)
N(2)		C(9)	- H(7)	114(3)	C(11)	-	C(10) - H(9)
N(2)	-	C(9)	- H(8)	111(5)	C(11)	-	C(10) - H(10)
H(7)	-	C(9)	- H(8)	99(5)	H(9)	-	C(10) - H(10)
C(10)	-	C(11)	- H(11)	1 09(3)	C(11)	-	C(12) - H(13)
C(10)	-	C(11)	- H(12)	108(4)	C(11)	-	C(12) - H(14)
C(12)	-	C(11)	- H(11)	110(3)	C(4)	-	C(12) - H(13)
C(12)	-	C(11)	- H(12)	100(4)	C(4)	1	C(12) - H(14)
H(11)	-	C(11)	- H(12)	114(5)	H(13)	-	C(12) - H(14)

Table 6.2.6.

Torsion angles * (degrees) in the saturated rings.

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Atom A	Atom B	Atom C	Atom D	Angle
C(1)	C(6)	C(7)	C(8)	-155 7
c(6)	C(7)	c(8)	C(9)	51.4
c(7)	C(8)	C(9)	N(2)	53.7
C(8)	c(9)	N(2)	C(10)	155.9
C(9)	N(2)	C(10)	C(11)	1 56 . 4
N(2)	C(10)	C(11)	C(12)	41.4
C(10)	C(11)	C(12)	C(4)	-45.8
C(11)	C(12)	C(4)	C(3)	-154.7

*The angle A-B-C-D is defined as positive if when viewed along the B-C bond atom A has to be rotated clockwise to eclipse atom D. Displacements (Δ) of atoms from mean plane through aromatic ring. Equation of plane :

$$0.3540X' + 0.8348Y' - 0.4216Z' = 2.0802 \text{ Å}$$

where X', Y' and Z' are absolute orthogonal co-ordinates (in $\stackrel{o}{A}$, with X' = $\underline{ax}\sin\beta$, Y' = \underline{by} , and Z' = $\underline{cz}\cos\beta + \underline{ax}$).

Atoms in plane $\Delta($	Ă)
--------------------------	----

C(1)	-0.010
C(2)	0.004
C(3)	0.008
C(4)	-0.013
C(5)	0.008
C(6)	0.004

Atoms out of plane

N(1)	0.064
0(1)	0.183
C(7)	0.070
C(8)	-0.488
C(9)	0.141
N(2)	0.029
C(10)	0.090
C(11)	0.477
C(12)	-0.068

Some important intermolecular contacts involving the nitroso group. Standard deviations are in parentheses.

Molecular positions other than x, y, z required to describe these contacts are :

Ι	-x,	2-у,	1-z
II	-x,	1-y,	1-z
III	1-x,	2-y,	1-z

Atom 1	Atom 2	Contact distance (Å)
0(1)	C(9) ^I	3.57(1)
N(1)	C(11) ^I	3.55(2)
N(1)	C(8) ^{II}	3.58(1)
C(3)	0(15) ^{III}	3.45(1)
0(1')	C(10) ^I	3.5(3)
0(1')	C(11) ^I	3.4(3)
0(1)	H(7) ^I	2.7(6)
N(1)	H(12) ^I	2.8(6)
Ó(1')	c(8) ^I	3.5(3)

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Figure 6.2.1 : The E-map of 9-nitroso julolidine obtained from the symbolic-addition solution.

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Figure 6.2.2 : The two overlapping half-weight 9-nitroso julolidine molecules proposed as an explanation of the distribution and height of the E-map peaks in Figure 6.1.1.



. Figure 6.2.3 : The 9-nitroso julolidine molecule projected along the <u>h</u> axis.

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Figure 6.2.4 : The crystal structure of 9-mitroso julolidine projected along <u>a</u>*, showing the head-to-tail molecular pairs. The projection is referred to a left-hand set of axes.

6.3. <u>The Crystal and Molecular Structure of N,N diethyl p-nitroso</u> aniline

6.3.1. Introduction

N,N-diethyl-p-nitrosoaniline was chosen from a number of possible N,N-dialkyl-p-nitrosoanilines as the next p-nitrosoaniline **derivative** to be studied mainly because of the high quality of its crystals. It was also hoped that the bulky ethyl groups would discourage the formation of the head-to-tail molecular pairs which were thought to be the cause of the disordered nitroso group in 9-nitrosojulolidine.

6.3.2. Experimental

Crystal Data

 $C_{20}H_{28}N_4O_2$, M = 356.47. Monoclinic, <u>a</u> = 14.717(8), <u>b</u> = 10.056(5), <u>c</u> = 13.640(6), β = 87.7(0.1)^O. <u>U</u> = 2,016.97 Å³, <u>D</u>_m = 1.17, <u>z</u> = 4, <u>D</u>_c = 1.173, $\mu(MoK_{\alpha}) = 0.83 \text{ cm}^{-1}$. Space group P_{2_1}/n (No. 14).

Data Collection

N,N-diethyl-p-nitrosoaniline forms green, prismatic crystals, with the prism axis along <u>b</u>. The crystal used in the data collection was a prism of dimensions $0.90 \times 0.75 \times 0.75 \text{ m.m}^3$, which was mounted along its prism axis. The space group and initial cell dimensions were obtained from rotation, Weissenberg and precession photographs, while more accurate cell dimensions were obtained from a least-squares treatment of 12 high-order reflections whose θ values had been measured automatically on a P.D.P. 8 - controlled four-circle diffractometer. Integrated intensities were measured on the diffractometer for some 300 reflections out to $\theta = 25^{\circ}$, of which 2,160 $|F| > 3\sigma(|F|)$ were used in the subsequent analysis. No absorption corrections were applied to the data.

6.3.3. Structure Analysis and Refinement

The structure was solved by the symbolic addition method, using the 318 reflections with E-values calculated by DATFIX to be greater than 1.3. An origin was defined by assigning positive phases to the reflections 12 4 3, 4 5 11, 11 1 9, and a solution was obtained using the programs SIGMA2 and PHASE. However, the solution was not unique, the phases of the large number of reflections having been determined in terms of the symbolic phase 0 8 1. Two E-maps had to be calculated, corresponding to the two solutions in which the reflection 0 8 1 has respectively a positive and negative phase. Each E-map showed essentially the same features - two unique sets of peaks in planes approximately normal to each other, corresponding to the two N, N-diethyl-p-nitrosoaniline molecules in the asymmetric unit, each set of peaks being interpretable in terms of two overlapping half-weight molecular images the same effect as was found with 9-nitrosojulolidine. The co-ordinates of each of the two pairs of half molecules in both E-maps were averaged, and structure factors were calculated from these 'averaged' co-ordinates. The structure factors based on the co-ordinates obtained from the first

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E-map (corresponding to the solution in which the phase of $0 \ 8 \ 1 = +1$) gave an R-value of 66 per cent, while those based on the co-ordinates obtained from the second E-map (corresponding to the solution in which the phase of $0 \ 8 \ 1 = -1$) gave an R-value of 44 per cent and this latter solution was subsequently proved by refinement to be the correct one.

Three cycles of full-matrix isotropic least-squares reduced R from 44 per cent to 20 per cent, and a difference map calculated at this stage revealed all the hydrogen atoms and also showed that the nitroso groups of both molecules were disordered, and by different amounts. In the subsequent four cycles of refinement, all of the non-hydrogen atoms in the N,N-diethylaniline residue except C(1) and C(9) were refined by block diagonal least-squares with anisotropic temperature factors; C(1)and C(9) were refined by full-matrix anisotropic least-squares and the disordered nitroso atoms O(1), O(1'), N(1), O(2), O(2') and N(3) by fullmatrix least-squares, with their isotropic temperature factors (U) and population parameters (p) subject to the following constraints :

 $p[0(1)] + p[0(1')] = 1 \qquad U[0(1)] = U[0(1')]$ p[N(1)] = p[0(1)] $p[0(2)] + p[0(2')] = 1 \qquad U[0(2)] = U[0(2')]$ p[N(2)] = p[0(2)]

The co-ordinates of N(1') and N(3') were not refined but their temperature factors and population parameters were assigned the values :

$$U[N(1')] = U[N(1)] \qquad p[N(1')] = p[O(1')]$$
$$U[N(3')] = U[N(3)] \qquad p[N(3')] = p[O(2')]$$

The hydrogen atom co-ordinates only were refined, their temperature factors being fixed at those of their parent carbon atoms at the end of the isotropic refinement. During the final three cycles of leastsquares refinement, the following weighting scheme was applied :

$$W = X \times Y$$

If $A \ge F_{obs} > |F_{calc}|$, W = 0.000000001If $\sin \theta > B$, X = 1, else $X = \sin \theta / B$ If $C > F_{obs}$, Y = 1, else $Y = C/F_{obs}$

The final values of A, B and C were 0.3, 0.5 and 8.0 respectively, and the R-value at the end of the refinement was 8.3 per cent.

The atomic co-ordinates and temperature factors are listed in Tables 6.3.1. and 6.3.2. respectively, and the observed structure amplitudes and calculated structure factors are listed in Table 6.3.3.

6.3.4 Description and Discussion of the Structure

The bond lengths and angles of the two N,N-diethyl-p-nitrosoaniline molecules in the asymmetric unit are listed in Tables 6.3.4. and 6.3.5. respectively. The numbers assigned to the atoms of the asymmetric unit are shown in Figure 6.3.1.

The molecular packing as viewed down \underline{b} is shown in Figure 6.3.2.

Molecules which are symmetrically related to molecule I in Figure 6.3.1. (hereafter referred to as Type I molecules) have their aromatic rings approximately parallel to the 010 plane, while those symmetrically related to molecule II in Figure 6.3.1. (Type II molecules) have their aromatic rings approximately parallel to the 101 plane. Type I and Type II molecules are stacked alternatively on top of each other in the b direction, while in the ac plane, Type I and II molecules alternate along the direction of the n-glide. Also in the ac plane, molecules of each type are arranged head-to-tail in rows parallel to 101. Each molecule of one type is thus surrounded by four molecules of the other type above, below and on both sides of the aromatic plane - with the result that there are no parallel contacts between aromatic rings, as in 9-nitrosojulolidine. the angle between the mean planes through the aromatic rings of Type I and II molecules being 87 degrees. The molecules of N.N-diethyl-p-nitrosoaniline are thus less densely packed than these of 9-nitrosojulolidine, and this is reflected in the lower calculated density of the former (1.173 compared with 1.323). There are no intermolecular contacts worthy of special mention, all such contacts corresponding to normal wan der Waals distances. C •••• C contacts less than 3.80 Å, and C \cdots 0 contacts less than 3.60 Å are listed in Table 6.3.6. In particular, there are no contacts sufficiently close to either of the nitroso groups to force them to adopt exclusively one or other of their two possible orientations (in the planes of the The nitroso groups of both molecules in the asymmetric aromatic rings).

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unit are thus disordered, the relative populations of the two orientations being 83:17 in molecule I and 76:24 in molecule II. The greater disorder of the molecule II nitroso group is reflected in the higher standard deviations of its dimensions. The dimensions of the molecule I nitroso group (C-N = 1.432(9) Å, N-O = 1.231(8) Å, \angle C-N-O = 111.3 $(0.6)^{\circ}$) are in good agreement with the dimensions of the nitroso group in 9-nitrosojulolidine, but the dimensions of the molecule II nitroso group (C-N = 1.463(10) Å, N-O = 1.185(11) Å, \angle C-N-O = $109.9(0.8)^{\circ}$) differ significantly from those of both the molecule I and 9-nitrosojulolidine nitroso groups. It seems likely, therefore, that the standard deviations of the molecule II nitroso atomic positions, as determined from the least-squares residuals, are over-optimistic.

The bond lengths of the two N,N-diethylaniline residues are strongly suggestive of a quinonoid-type structure, but the differences in the bond-lengths of the aromatic rings in each residue are not significant on the basis of the estimated standard deviations. If, however, chemically equivalent bonds in both residues are averaged, the differences in the mean bond lengths thus obtained are significant. These mean bond lengths are shown in Figure 6.3.3. together with the mean bond angles; the C(4)-N(2) bond length of 1.349(4) Å, which is the same as the equivalent bonds in N,N-dimethyl-p-nitroaniline and 9-nitrosojulolidine, and the C(2)-C(3) bond lengths of 1.374(4) Å, which is significantly shorter than the C-C length in benzene, confirm a quinonoid-type structure. The bond at the amino end of the aromatic ring, C(3)-C(4), is significantly longer at 1.413(3) Å than the other

ring bonds, a feature also found in 9-nitrosojulolidine, N,N-dimethylp-nitroaniline and p-nitroaniline. The N(2)-C(7) distances of 1.466(3) \mathring{A} compares with the normal C-N single-bond length of 1.47 \mathring{A} , but the C(7)-C(8) distance of 1.508(4) \mathring{A} is significantly shorter than the normal C-C single-bond length of 1.54 \mathring{A} . This 'apparent' shortening of the ethyl group C-C bonds (there can be no chemical explanation for it) must be due to the rather large vibrational amplitudes of the terminal methyl groups. The conformation of the diethylamine group is the same in both molecules of the asymmetric unit, one C-C bond pointing upwards, the other downwards, with an average torsion angle about the C-N bond of 87°. The individual torsion angles are listed in Table 6.3.7. The average C-H distance in the ethyl groups is 0.98 \mathring{A} , with a root mean square deviation of 0.07 \mathring{A} , and the average aromatic C-H distance is 0.95 \mathring{A} with a root mean square deviation of 0.08 \mathring{A} .

The mean planes of the aromatic ring, amino group and nitroso group of both molecules are listed in Table 6.3.7, together with the deviations of the atoms from the planes, and the angles between the planes. The aromatic rings of both molecules I and II are planar within the limits of experimental error, but the diethyl amino groups are twisted out of the aromatic planes about the C-N bonds by 6.0° and 2.4° respectively. The nitroso group of molecule I is coplanar with the aromatic ring, but that of molecule II is twisted out of the plane by 5.3° . Since the two molecules can be resonably assumed to be chemically identical, these differences in the orientations of the diethylamino and nitroso groups must be due to crystal packing forces, although the significance of the molecule II nitroso group – aromatic ring angle of 5.3° must be considered doubtful, since the estimated standard deviations of the nitroso group nitrogen and oxygen positions are thought to be too low.

Both of the amino groups are planar within experimental error, although the displacements in Table 6.3.8. suggest they are slightly pyramidal.

6.4. Conclusion

The structure analyses of 9-nitrosojulolidine and N.N-diethylnitroscaniline have provided the structural details which confirm the large contribution of the quinonoid structure II (Section 6.1.) to the electronic structure of p-nitrosognilines predicted by their physical and spectroscopic properties. The amino and nitroso groups have been shown to be more or less coplanar with the aromatic ring, and the dimensions of the aromatic ring have been shown to be significantly altered by the concerted effects of the electron-releasing amino and electron-withdrawing nitroso substituents. In addition, the dimensions of a monomeric aromatic nitroso group have been established with reasonable accuracy; the mean values of the dimensions of the 9-nitroso julolidine and the molecule I N.N-diethyl p-nitrosoaniline nitroso groups (which are disordered to exactly the same extent) are : C-N = $^{\circ}$ 1.433(6) $^{\wedge}$; N-0 = 1.240(6) $^{\circ}$ and $^{\vee}$ CNO = 112.0(0.7) $^{\circ}$. These values appear to be more chemically acceptable than those determined for p-iodonitrosobenzene, for which a similar quinonoid structure is postulated, of 1.28 Å for C-N, 1.24 Å for N-O and 125° for \angle CNO.

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TABLES AND DIAGRAMS

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Table 6.3.1.

Fractional co-ordinates $(\underline{x}, \underline{y}, \underline{z})$ with population parameters (\underline{p}) other than unity. Standard deviations are in parentheses.

	<u>x</u>	Y	Z	p
0(1)	0.3106(4)	0.3179(6)	0.5579(4)	0.83(2)
0(1')	0.2339(29)	0.2944(36)	0,4621(26)	0.17(2)
N(1)	0.2912(5)	0.2990(6)	0.4704(5)	0.83(2)
N(1')	0.3080	0.3000	0.4900	0.17(2)
N(2)	0 . 5813(3)	0.2908(4)	0.2194(2)	
C(1)	0.3710(3)	0.2984(4)	0.4136(3)	
C(2)	0.3519(3)	0.2782(5)	0 . 3135(4)	
C(3)	0.4222(3)	0.2751(4)	0.2498(3)	
C(4)	0.5123(3)	0.2939(4)	0.2816(3)	
C(5)	0.5305(3)	0.3153(4)	0.3841(3)	
C(6)	0.4592(4)	0.3184(4)	0.4464(3)	
C(7)	0.6768(4)	0.2973(5)	0.2531(4)	
C(8)	0.7104(4)	0.4394(7)	0.2676(5)	
C(9)	0,5648(4)	0.2799(5)	0.1123(3)	
C(10)	0.5608(5)	0.1377(5)	0.0781(3)	
0(2)	0.3893(5)	0.2084(8)	-0.0866(5)	0.76(2)
0(2')	0.3889(14)	0.3765(21)	-0.0859(14)	0.24(2)
N(3)	0.3583(5)	0,3115(9)	-0.0627(5)	0.76(2)
N(3')	0.3550	0.2680	-0.064	0.24(2)

Table 6.3.1. (cont'd)

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	x	<u>y</u>	<u>Z</u>
N(4)	0.0721(3)	0.2778(3)	0.1946(2)
C(11)	0.2841(3)	0.2890(6)	0.0036(3)
C(12)	0.2412(3)	0.4036(5)	0.0298(3)
C(13)	0.1703(3)	0.4015(4)	0.0915(3)
C(14)	0.167(3)	0.2801(4)	0.1337(3)
C(15)	0.1875(3)	0.1630(4)	0.1072(3)
C(16)	0.2576(3)	0.1677(5)	0.0437(3)
C(17)	0.0270(4)	0.3998(5)	0.2250(4)
C(18)	-0.0488(4)	0.4422(6)	0.1547(5)
C(19)	0.0388(3)	0.1545(4)	0.2376(3)
C(20)	0.0904(5)	0.1166(5)	0.3304(4)
H(1)	0.295(4)	0.263(6)	0.306(4)
H(2)	0.399(4)	0,259(6)	0.178(4)
H(3)	0.582(4)	0.322(6)	0.401(4)
H(4)	0.479(4)	0.332(6)	0.516(4)
H(5)	0.718(4)	0.246(6)	0,210(5)
H(6)	0.691(4)	0.252(6)	0.321(4)
H(7)	0.768(4)	0.437(7)	0.272(5)
H(8)	0.668(4)	0.485(7)	0.312(5)
H(9)	0.697(4)	0.493(7)	0,207(5)
H(10)	0.515(4)	0.332(6)	0.094(4)
H(11)	0.616(4)	0.321(6)	0.085(4)

Table 6.3.1. (cont'd)

	x	X	<u>Z</u>
H(12)	0.500(4)	0.092(7)	0 .1 03(5)
H(13)	0.551(4)	0.141(7)	0.002(5)
H(14)	0.605(4)	0.089(7)	0.097(5)
H(15)	0.272(4)	0.489(6)	0.010(4)
H(16)	0.135(4)	0.484(5)	0.102(4)
H(17)	0.167(4)	0.077(6)	0.132(4)
H(18)	0.287(4)	0.088(5)	0.032(4)
H(19)	0.993(4)	0.380(6)	0.275(4)
H(20)	0.076(4)	0.471(6)	0.240(4)
H(21)	0.965(4)	0.458(7)	0.085(5)
H(22)	0.909(5)	0.373(7)	0.147(5)
H(23)	0,909(4)	0.518(7)	0.179(5)
H(24)	0.978(4)	0.163(6)	0.249(4)
H(25)	0.039(4)	0.084(6)	0.188(4)
H(26)	0.104(5)	0.178(7)	0.379(5)
H(27)	0 .1 63(4)	0.091(7)	0.312(5)
H(28)	0.053(4)	0.047(7)	0.356(5)

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Vibrational parameters $(\stackrel{02}{\Lambda^2})$ with standard deviations in parentheses.

	U ₁₁ or U is	uo ^U 22	U ₃₃	^U 12	U ₁₃	U ₂₃
0(1)	0.105(3)					·
0(1')	0.105					
N(1)	0.092(2)					
N(1')	0.092					
N(2)	0.074(2)	0.062(2)	0.047(2)	-0.002(2)	0.010(2)	-0.002(1)
C(1)	0.066(3)	0.057(2)	0.071(3)	0.002(2)	-0.021(2)	0.002(2)
C(2)	0.062(2)	0.063(3)	0.081(3)	-0.003(2)	0.005(2)	0.002(2)
C(3)	0.074(3)	0.055(2)	0.057(2)	-0.003(2)	-0.001(2)	0.001(2)
C(4)	0.065(2)	0.044(2)	0.044(2)	-0.001(2)	0.003(2)	0.002(2)
C(5)	0.059(2)	0.066(2)	0.047(2)	0.005(2)	-0.001(2)	0.004(2)
C(6)	0.097(3)	0.057(2)	0.046(2)	0.005(2)	0.013(2)	0.001(2)
C(7)	0.076(3)	0.079(3)	0.070(3)	0.006(2)	0.021(2)	-0.003(2)
C(8)	0.098(4)	0.095(4)	0.100(4)	-0.027(3)	0.022(3)	-0.004(3)
C(9)	0.098(3)	0.064(3)	0.042(2)	-0.008(2)	0.008(2)	0.002(2)
C(10)	0.136(5)	0.066(3)	0.053(2)	0.001(3)	0.013(3)	0.008(2)
0(2)	0.123(4)					
0(2')	0.123					
N(3)	0.100(2)					
N(3')	0.100					

Table 6.3.2. (cont'd)

	U ₁₁ or U _{iso}	U22	U ₃₃	^U 12	^U 13	U ₂₃
N(4)	0.079(2)	0.043(2)	0.057(2)	-0.004(2)	0.019(2)	-0.005(1)
C(11)	0.056(2)	0.107(4)	0.046(2)	-0.012(2)	0.007(2)	0.001(2)
C(12)	0.071(3)	0.082(3)	0.059(2)	-0.012(2)	0.006(2)	0.007(2)
C(13)	0.072(3)	0.055(2)	0.062(2)	-0.010(2)	0.014(2)	0.001(2)
C(14)	0.058(2)	0.053(2)	0.044(2)	-0.004(2)	0.007(2)	-0.005(2)
C(15)	0.065(2)	0.059(2)	0.053(2)	0.002(2)	0.002(2)	-0.008(2)
C(16)	0.068(3)	0.085(3)	0.057(2)	0.013(2)	-0.002(2)	-0.019(2)
C(17)	0.104(4)	0.056(3)	0.076(3)	-0.003(2)	0.038(3)	-0.012(2)
C(18)	0.102(4)	0.069(3)	0.123(5)	0.017(3)	0.033(4)	-0.003(3)
C(19)	0.082(3)	0.054(2)	0.065(2)	-0.017(2)	0.020(2)	-0.001(2)
C(20)	0.145(5)	0.072(3)	0.060(3)	-0.021(3)	0.014(3)	0.007(2)

- H(1) 0.07
- H(2) 0.06
- H(3) 0.06
- H(4) 0.07
- H(5) 0.08
- H(6) 0.08
- H(7) 0.10
- H(8) 0.10
- H(9) 0.10
- H(10) 0.07
- H(11) 0.07

Table 6.3.2. (cont'd)

U iso

- H(12) 0.08
- H(13) 0.08
- H(14) 0.08
- H(15) 0.07
- H(16) 0.06
- н(17) 0.06
- H(18) 0.07
- н(19) 0.08
- H(20) 0.08

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- H(21) 0.10
- H(22) 0.10
- H(23) 0.10
- H(24) 0.07
- H(25) 0.07
- H(26) 0.09
- H(27) 0.09
- H(28) 0.09

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Table 6.3.3

Observed structure amplitudes and final calculated structure factors. (x10)

	17.2.L	15,816	13,0,L	3 37 34	•7 274 •227	
	35 - 10		4 17 - 17	0 54 -42	-4 96 87	11 54 -38
- 3	29 - 32	5 25 12	1 43 -46	-3 28 -31	-5 43 -41	7 23 -38
-		-3 42 -38	e 184 +98	-4 27 24		4 23 +44
	17,1,1	=5 35 =26	-1 91 -85	•6 26 22	11,9,6	5 69 -86
	41 - 26	14 7.1	•7 36 31	•7 42 -47	2 44 - 18	2 26 •19
	-1 -20	147772	13.5.L	12.6.1	1 24 -15	2 54 38
	17,0,1	•1 34 25			-2 34 -23	•1 58 •35
-			8 35 =21	P 55 -56	-3 52 -57	-2 21 -9
*3	42 49	14,0,1		-1 54 -54	11.8.1	•3 337 311
	10,4,1	2 68 53	+2 32 +24	-3 189 178		•5 32 •43
		8 67 -68	-3 31 27	-5 25 -18	6 26 16	*6 22 24
3	52 42	=1 75 +78		•6 33 36		•7 54 65
- 5	28 €18	2/ -10	131416	•/ 2/ 30	110/02	•1# 47 •61
		14,5,L	6 48 -33	12,5,L	2 39 41	•12 29 18
	16,3,L		5 25 24		•2 98 93	
	24 - 25	5 20 20	4 54 45	8 57 40	•3 77 79	11, 0 ,L
1	28 = 27	1 63 -58	2 25 -19	5 35 37	-5 33 2R	11 53 44
•		-1 94 -84	1 85 79	3 35 +53	-8 85 +76	9 24 26
	10,2,1		0 248 189	•3 73 69		3 103 128
,	58 -47	14,4,L	=1 0/ =3/ =2 26 25	•• /5 •/5 •5 21 •#	11,0,1	1 125 121
2	52 39	4 34 25	-3 74 -78	•7 30 30	8 28 =28	•3 135 138
1	28 -26	0 131 124	-6 25 -25	-10 25 20	•1 68 62	•5 22 •23
•2	26 -25	-1 97 96	•7 24 •2H	19 4 1	=5 39 38	•7 49 •59
•6	28 15	14.5.1	13.3.L	121996	-7 20 -13	
-0	L. 1.			9 46 45	11,5,1	18,9,L
	16,1,L	7 24 21	8 36 29	7 28 21	· ·· ··	
	34 P	6 34 =29	6 24 -28	6 43 -39	9 33 25	•3 68 62 •4 34 -39
-	32 + 26	3 24 -26	4 37 -50	1 45 -40	6 48 •48	•• 20 •27
1	27 21	2 39 32	2 27 25	•1 98 97	5 38 +32	10.8.L
+2	72 56	•1 125 108	1 53 =53	-2 241 -199	4 39 50	
•3	31 27	•2 55 •58	P 57 66	=3 313 =389 =4 195 181	2 34 • 35	1 55 55
	02 30	-5 48 30	-2 87 80	+6 51 +45	-1 58 -57	•4 88 =79
	16.0.L	•7 32 •23	-3 49 -43	■7 43 ●58	-2 147 -141	•7 39 =37
		-8 29 17	-7 35 -29	•A 52 57	-3 109 -119	
6	26 -24	14.2.1	-8 26 -28	-9 /6 /0	•0 42 •00 •8 73 67	141/16
-4	61 •61	14,2,6	13,2.1	•10 J# •11	•• ••	3 39 58
	••••••	6 35 =26		12,3,L	11,4,6	2 27 •28
	15,6,6	4 48 -47	6 30 22	• • •	• ·· ··	
	30 10	3 48 - 36	5 30 •44 3 58 75	2 24 26	1 20 30	•1 21 •28
é	28 26	1 50 48	1 44 •47	-1 64 61	•1 98 •95	+4 88 92
		0 89 -87	B 63 =64	•3 91 •79	•2 219 •223	•5 26 21
	15,5.L	-2 67 67	-1 184 160	•4 128 113	•3 127 122	•9 57 53
	11 27	=3 23 19 =6 60 =61	•3 52 48	•7 55 •46	-5 93 88	10,6,1
•1	28 -34		•7 40 •34		-8 26 23	
		14,1,L		12,2,L	■1€ 59 41	18 45 42
	15,4,2	A 58 65	13,1,L	9 48	11.3.1	8 24 23
2	29 -25	5 28 29	6 27 26	8 28 28		4 42 +43
ē	41 - 39	3 26 26	5 81 83	2 55 55	11 32 23	•3 87 85
•1	54 54	e 58 -54	3 36 •44	•1 27 •48 •2 140 205	8 25 +8 7 86 41	P4 47 41
	15.1.1	•1 42 •44 •3 34 •31	e1 134 •127	-2 304 290	3 35 57	•9 71 •72
		•4 48 •48	-2 88 -76	•4 147 •137	-1 89 88	
5	41 32	-6 39 -25	-3 96 89	-6 37 31	-2 79 79	18,5,6
2	51 -49		•7 129 112	•8 28 •33	•3 37 •20	12 55 43
.,	31 -15	14,016	13.0.6	•9 36 •26	-8 42 -36	8 24 -12
•3	24 18	8 26 -16		-18 24 42	-9 58 58	7 44 +43
		6 27 30	3 69 -76		-10 32 50	5 /3 •98
	15,2,L	4 61 66	1 59 - 59	12,1,1	11.2.6	-1 98 91
3	26 -6	•2 83 •76	-5 31 56	9 24 +23		•2 72 •77
e	32 23	-6 101 98	-7 58 44	4 80 -125	18 39 -39	•3 93 •95
•1	48 •42	-10 29 53	+11 41 27	3 22 •29	3 28 +26	•7 38 32
-3	26 28	13.8.1	12.8.1	2 38 +47 8 76 +78	2 30 -03	/9
•7	28 6	131015	12/0/6	-1 76 -64	8 48 -48	18,4,L
•		-1 44 41	1 26 •21	•2 167 147	-1 37 34	• ·• ••
	15,1,L	·	P 47 41	• 3 32 24	•7 1/1 144 •3 111 -180	4 27 11
,	28 - 24	13,7,6	•1 03 32 •2 26 26	•6 71 87	•4 142 131	8 30 29
3	41 • 33	4 47 •46	•3 26 •34	•7 61 63	-5 184 -97	•2 31 37
2	36 35	2 31 =34	-4 25 -10	•5 42 •63	+6 49 52	-3 68 -66
	30 26	•2 79 75	-5 35 34	12.0.1	•12 25 •24	•5 283 283
- 12	27 •22		12./.L	117.75		+6 135 +138

Table 6.3.3 (cont'd)

	18.4.6	2 40 -43	•10 66 •71	3 120 182	-1 62 -61	1 67 59
		-2 41 41	-11 65 58	1 94 -96	•2 87 •82	a 24 27
-9	89 96	•6 28 •22	-13 26 17	-1 64 64	-3 49 -57	•1 29 26
-10	34 - 36	-16 57 48	B 1 1	-2 58 -40	•4 75 77	•2 44 47
-11	30 -44	9.6.1	41110	-4 41 42	-3 40 -37	•5 27 35
	10.3.1	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	12 51 49	-5 52 69	-8 117 -120	•7 48 52
		8 62 -53	11 163 142	-6 62 64	-9 63 55	•8 27 38
10	59 -56	7 36 -32	16 91 87	•/ 95 86	-10 77 84	•9 59 •58
9	55 -51	6 42 -46	9 31 -42	-8 33 29	•13 24 18	
	32 38	5 74 -72	6 32 -41	-11 35 33		7,6,L
2	55 93		3 2/ • 32		6,1,1	12 11 - 18
3	27 45	-5 66 71	1 101 -125	87370	14 27 16	9 15 -12
2	55 50	•6 68 •66	0 55 55	9 127 115	10 27 -32	8 100 -91
	118 -125	-7 39 39	-1 192 -192	7 88 -198	8 365 -413	7 27 +25
•1	28 = 3.5	-8 32 47	-6 34 39	6 25 28	7 34 -41	6 29 28
•2	35 - 34	-10 25 -22	-7 37 -35	5 72 87	6 69 81	5 46 52
• 3	38 39		•9 31 •35	4 26 • 35	5 31 • 31	4 33 36
	38 -39	4,57L	-11 116 125	2 74 -71	3 30 - 15	2 241 226
•6	98 -93	12 87 74	-11 100 100	0 73 76	2 264 251	1 26 +21
•11	25 19	9 37 +43	9,0,L	-1 53 49	1 60 -67	8 18A +97
-12	33 17	8 57 +32		•2 103 •87	8 194 -189	=1 3A =39
		5 40 49	13 49 42	-3 113 -197	•1 67 =61	•2 43 •42
	16.2.1	2 26 25	11 44 -24	-4 97 87	-2 418 - 398	•3 25 •30
	52 -43	1 49 40	/ 53 = 65	-5 64 -5		
11	11 .11	-3 27 -28	3 36 53	•8 44 •41	*5 61 55	
10	86 •79	-4 153 144	1 299 -289	-12 28 -28	+6 54 51	7,5,6
9	46 -35	-5 109 110	-1 01 -56		-7 58 56	
5	23 54	-6 225 224	•3 42 41	8,4,L	-9 28 25	10 22 67
- 4	22 28	-7 66 -63	•5 182 171		#18 57 6P	8 80 -77
2	54 -47	-18 28 -16	•7 25 •J0	11 48 -31	•12 56 •72	7 127 137
•2	26 •20	-12 44 -19	•9 68 96	10 31 29	8. P. 1	0 23 28
• 3	176 178	9.4.1	-13 103 -80	9 110 133 8 80 -AA	0,0,1	3 42 +38 4 75 -49
	190 0190	y,-,L	•13 •6 •56	7 17 -17	14 20 30	3 103 -105
-6	42 29	11 43 +32	8.18.L	5 56 63	10 46 39	2 117 -116
•7	33 33	18 41 -38		4 142 -165	8 126 -116	1 67 -68
•8	62 -71	9 68 49	4 25 -18	3 168 -161	6 25 44	-1 35 38
-9	41 =46	8 37 51	# 37 39	2 110 98	4 70 -75	•2 144 •151
•18	35 40	6 34 41	_	0 26 -21	2 145 122	•3 148 •149
		5 47 56	8,9,L	-1 61 64	0 257 -258	•4 30 20
	10,1,1	4 75 113	• • • - 67	•3 80 /6	•2 399 337	-3 3/ -22
• •		3 /4 =80	7 70 -02			-7 42 -51
10	58 47	1. 3 79 55	3 54 +49	•6 124 •139	-12 117 -111	•8 191 •285
Å	31 -16	4 158 158	1 77 79	•7 241 -234	-14 40 63	-9 129 135
š	20 •2	-5 231 -224	-1 28 -23	-8 71 65		
2	118 131	•7 60 - 63	-3 30 -28	-9 24 37	7,10,L	7,4,L
1	76 74		-4 24 -31	-11 86 -74		
ø	245 208	9,3,L	•5 47 •45	•12 58 62	4 31 -33	12 55 49
•1	33 39	12 10 -12	•7 33 •26	8.3.1	3 50 449	9 71 75
-2	78 -130		8.8.1	07572	•2 27 •34	8 185 206
-11	30 -15	10 156 -139	01012	18 81 -65		7 67 -82
-11	30 -30	8 52 68	7 69 +64	9 49 -64	7,9,1	6 102 -95
	10.0.1	7 42 •68	6 44 41	8 116 157		5 29 26
		6 36 66	5 29 24	7 76 107	6 121 +95	3 122 -111
12	79 67	5 51 -90	4 44 4P	6 45 +58	3 58 +48	2 419 400
10	113 103	4 52 85	2 38 -29	5 28 442		1 214 198
	24 • 47	1 /3 83	-2 40 2/	3 26 1		•2 4P •30
2	107 -04	=1 88 =85	-4 28 -33	2 28 -20	7,8,L	• 3 44 38
•2	101 -102	•2 75 •72	•7 26 29	Ø 65 56		•4 70 •67
• 4	208 205	-4 114 -109	_	-1 130 135	9 52 •47	•5 68 •58
•8	117 141	-5 93 -97	8,7,L	-2 150 134	8 26 29	-6 143 -152
-10	23 24	-6 269 -198		•3 145 152	7 48 46	•7 21/ 222 •# 05 #*
-12	27 . 35	-7 158 151	9 99 -92	-5 152 -152	5 24 -14	-0 00 00
		-10 58 46	7 124 114	-7 22 -18	4 35 35	+10 137 155
	¥,¥,L	=11 30 =31 =12 25 =4	3 68 62	-8 53 58	2 23 •19	•14 29 •6
3	37 • 32	•13 26 •21	1 78 •76	•10 26 •34	0 34 +41	
2	23 18		•1 56 •51	-12 55 68	•1 73 72	7.3.L
•5	26 28	9,2,L	-3 98 106		-2 130 138	·
-6	51 -34		•5 55 52	8,2,L	•/ 54 •28	11 35 +35
		13 29 -30	•6 33 •33	13 27 26	•o /j •/j	10 JU +24
	9,8,L	10 66 64	•18 34 •31	11 59 50	7.7.1	8 122 135
-		/ 24 39	-11 p1 -51	18 44 -43		6 35 11
7	31 27	CP= C3 - 43	8,6,1	9 23 20	11 27 •11	5 34 35
1	38 10	2 39 •54	.,	8 104 146	18 53 +51	3 124 128
Å	64 =61	1 48 63	11 36 24	7 25 +25	9 60 =61	2 55 -43
•5	49 - 52	0 108 84	9 89 -68	5 21 +36	8 158 139	1 18 -22
		-1 27 26	8 43 -34	4 123 176	7 83 465	7 24 31
	9,7,L	-2 18 3	7 72 68	3 93 121	0 47 444 4 ki ka	•1 27 •23 •2 80 80
		•3 35 •29	6 47 -44	1 11 +42	3 45 44	•3 67 •63
?	27 24	-5 112 123	0 JE #J/	6 68 75	2 32 41	
1	25 13	+0 49 +48	• 30 •28			

Table 6.3.3 (cont'd)

7,3,1	6 42 -33	11 4.3 33	4 4/ 48	•1 71 •55	5,1,1
	2 33 39	18 44 -47	2 25 -18	•2 46 45	
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	-4 55 -58	A 57 -53	01110	-1 74 17	3 62 652
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-10 32 -24		2 282 254	4 30 -25	-18 153 154	9 168 197
•12 39 •25	6,8,L	1 91 /4	2 47 34	-11 87 -92	-1 118 93
		P 61 - 34	3 81 +8A	•12 49 +59	-2 32 32
7.2.1	8 35 32	+1 62 +73	•1 39 42		-3 48 47
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13 43 -27			- 40 +4		
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9 146 -151	2 49 -48	-5 146 -13/	•9 34 39	12 29 404	•/ 149 •156
8 216 +257	8 74 =/2	-6 106 99		10 32 -47	-8 111 116
5 60 -89	●2 95 98	-7 77 81	5,8,L	9 84 83	-9 84 -98
4 26 39	-5 30 -46	-11 50 36		6 72 •74	-18 34 -23
3 151 175	-8 48 -44	+12 54 52	9 42 -35	5 23 -15	•11 94 •77
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1 140 100	1 26 -18	******	5 116 117	4 49 58	-4 38 20
3 140 196	23 -10		5 156 157	1 252 -243	
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9 55 •51	E 401 397	-1 24 33	a2 46 a41	•12 55 •54	2.6.1
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1 275 258 8 137 140 -1 65 -54 -2 128 -123 -3 76 -62 -4 53 56 -5 275 284 -6 118 -12P -7 64 -64 -8 50 57 -9 165 173 -0 165 -108 -11 317 -313 -12 102 107 -13 73 -72 -4,4,L 	+) 160 +172 +12 38 38 +13 24 +16 4,1,+L 14 98 -77 13 39 -21 11 76 88 9 33 +15 8 76 78 7 125 +122 6 331 +347 5 175 -171 4 466 +466 3 257 -243 2 342 +343 1 235 -228	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-11 52 61 -14 26 25 3.3.L 13 68 61 12 38 33 10 49 50 9 227 -219 8 163 -163 7 145 91 6 33 30 5 58 43 4 71 67 2 95 95 1 215 194 8 134 143 -1 494 49 2 496 574	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
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$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} \bullet & 1 & 69 & \bullet 102 \\ \bullet & 11 & 69 & \bullet 67 \\ \bullet & 12 & 38 & 38 \\ \bullet & 13 & 24 & -16 \\ \hline & 4, 1, r, L \\ 14 & 98 & -77 \\ 13 & 30 & -21 \\ 11 & 76 & 86 \\ 9 & 33 & -15 \\ 8 & 78 & 78 \\ 7 & 125 & -122 \\ 6 & 331 & -347 \\ 5 & 175 & -171 \\ 4 & 466 & -468 \\ 3 & 2342 & -343 \\ 2 & 342 & -343 \\ 1 & 235 & -228 \\ -1 & 490 & 579 \\ -2 & 342 & -343 \\ 1 & 235 & -228 \\ -1 & 490 & 579 \\ -2 & 56 & -35 \\ -1 & 193 & 17h \\ -5 & 95 & 68 \\ -6 & 28 & -29 \\ -7 & 37 & -39 \\ -6 & 28 & -18 \\ -7 & 37 & -39 \\ -8 & 281 & 182 \\ -10 & 323 & -357 \\ -11 & 169 & -167 \\ -12 & 108 & 104 \\ -4 & -16 \\ -4 & -$	3,7,L 12 45 36 9 24 -22 8 51 -00 7 27 -27 6 34 30 5 28 36 4 186 182 3 28 25 2 36 36 1 23 16 P 56 52 -1 38 -33 -2 139 -133 -3 32 -37 -7 63 -73 -11 60 -67 -12 72 69 3,6,L 18 65 -61 9 23 -23 8 68 -71 6 59 65 5 22 -15 4 25 34 3 75 -71	-11 52 61 -14 26 25 3.3.L 13 68 61 12 38 33 10 49 50 9 227 -219 8 105 -163 7 165 -163 7 165 -163 7 5 58 43 4 71 67 2 95 95 1 215 194 8 134 143 -1 454 406 -2 406 574 -3 244 -223 -4 27 23 -5 1.58 114 -6 82 -79 -7 1 -58 -9 25 -37 -12 133 129 -13 129 -13 2.L 15 20 -25	11 86 87 7 68 -66 5 5 λ 3 497 1 440 -527 -1 21 15 -3 905-1281 -5 240 201 -7 91 -94 -11 208 -2293 -15 55 -44 2,11.L 4 27 -23 3 26 -27 2 37 39 1 32 37 -1 26 29 -2 39 39 +4 26 28 -5 26 -33 -6 25 -29 2,16.L 5 24 27 3 178 -188 2 186 -188 1 59 57 -7 39 38 -8 39 57 -7 39 38	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
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Table 6.3.3 (cont'd)

	2,5,1	-	•12	61	63		1.8,L		-14	52	52	9	115	-107	5	61	65
+ 8	48	45	-14	42	4 1	11	25	19		1.4.6		5	438	414		47	•46
-10	24	15	-15	39	36	10	30	- 33	15		26	4	98	186	2	277	279
=12	110	108		2,1,1		7	34	33	12	43	-38	2	20	27	é	25	16
-13	120	121		17	- 11	÷	74	•77	11	d1	78	1	69 228	=78 274		a	
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	2,4,1	•	12	91	0 () 7 ()	3	115	114	8 7	45	36	-2	198	-284	14	48	36
13	56	67	18	65	-58	i	195	-205	6	243	+226	-4	178	177	· 9	69	-86
12	87	•83	9	20	57	6	283	-286	5	187	175	-5	173	-162	,	81	-84
٠ <u>;</u>	68	66	7	101	-87	-3	43	-41	š	84	+#2	- 7	114	184	6	125	117
8	72	=69 08	6	95	-99	•4	87	-94 50	2	109	-173	9- - 0	68	78 •152	5	47	+5J 157
6	81	•72	4	784	726	=6	58	68	ø	315	- 514	= 1 8	40	• 34	3	110	84
5	242	+226	3	256	248	•8	49	= 5 ki .5 1	•1 •2	23	-66	-11	39	-44	2	78 491	+64
3	95	•87	1	16	25	•11	20	•24	•3	255	•232	•14	75	•75	•		
2	156	-163	P - 1	185	-199		1.7.1		-4	37 195	•24 •86		1.0.1			8,4,L	
ē	53	•47	•2	676	161				•7	46	51				11	99	-89
-1	27	276	-3	445	476	19	62	-55	-8	142	-141	13	265	-119	10	38	32
• 3	456	449	•5	385	- 370	4	85	•79	-11	53	51	9	35	-29	8	69	67
-4	372	-338	-6 -7	143	127	3	82 22	-14	-14	44	44	5	512	486	6	142	125
•7	58	3.R	•8	403	• 377	1	164	167				3	1824	-998	5	95	101
-8	44	40 • 37	-9 -10	126	+117	•1	110	=100		1,3,6		- 3	29	•12	4	75	105
-10	43	56	•12	89	85	•2	25	22	15	61	59	-5	151	156	2	353	-332
=11 =12	124	128	-14	49	45	-4	A Y	-88	12	45	58	•9	210	187	à	150	159
•13	29	•29	••			•5	27	-33	.0	85	98	-11	37	23			
•14 •15	76	•75 •60		51010	-	•7	41	-46	8	144	-114	•••		30		0,31	•
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	2, 3, 1	L	12	53	-52	•10	33	-27	5	145	•135	3	29	•26	13	33	25
14	26	14	8	403	387	•13	45	43	4	49	41	2	36	36	11	47	51
12	25	-27	4	931	•471 •873		1,8,1		2	332	299	•		30		52	53
9	189	+114	e	286	311			- 14	1	957-	1998		P,18,	L	P.	38	36
6	207	208	•2	128	133	10	34	26	-1	530	508	7	31	•26	6	147	-139
5	35	42	-6	172	-155	,	59	58	• 3	458	•437	6	27	-24	5	238	258
2	221	-218	-10	74	52	5	88	+82	-5	87	75	3	48	•51	3	267	-236
0	469	-476				4	193	-96	•6	127	85	1	100	184	2	375	+378 +765
-2	289	-283		17117		2	212	283	-8	72					•	•••	-,
- 3	18	•10	5	31	24	1	118	110	=13	6 S 3 A	65 45		0,9,L			0,2,1	•
-5	19	27	3	30	- 53	•2	31	54	•15	45	51	9	56	•51	12	59	68
•6	138	124	2	41	45	-3	76	60 80		1.2.1		7	26	26	11	133	130
•11	51	59	-i	28	-31	-5	P.6	-98		1.		4	58	• 57	9	66	79
-12	245	+247	•2	38 49	44	-6	94	94	15	13	-35	5	48	-54	;	169	-148
-14	43	44	•5	33	- 32	-9	44	43	13	61	58	1	139	-146	6	378	347
-15	26	• 32		1.10.	. 1	-13	38 55	•33 53	11	34	-40		8,8,L		34	253	-228
	2,2,	L			-				9	93	86			47	3	345	• 321
15	55	•53	6	29	29		1,5,6		7	155	154		49	-48	1	761	687
13	112	•111	4	60	-61	14	33	• 34	é	94	114	7	93 64	91 6.4			
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10	35	- 38	-1	45	45	e	105	93	3	57	-39	3	22	-26	12	23 58	-18
ě	154	-135	•3	44	45	6	471	-45B	÷	247	234	2	65	•67	10	176	•178
7	77	-88	-4	40	51	5	35	48	•1	3p9 28	-311	1	283	-397	9	90 10	22
5	488	389		1,9,1	-	3	299	-282	•3	252	254				,	191	+188
4	92	-95	-		28	5	277	•?67 97	•4	35	46 •19		0,7,L	•	6	66 161	+176
- 1	415	440	7	30	31	÷	679		•6	55	-65	1	48	43	4	144	142
é	191	-188	5	25	•26	•1	111	•129	-7	109	•110	8	69	•72	3	215	-214
•2	328	-330	3	38	75	- 3	263	248	-18	120	124	6	29	28	-		
•3	335	• 348	· 2	35	31	-4	367	295	•11 •12	37	•34 58	3	68 68	-74		4 ,8,	L
-5	586	184	-1	73	70	•6	162	-150	•14	51	45	2	108	97	14	43	+42
•6	166	149	•2	94	•100 43	•7	112	110		1,1,1		1	112	1.07	10	80 58	42
-8	191	98	• 9	31	31	-9	44	-58							6	718	+747
-10	67	-51				-10	23	-93	. 11 1#	23	•24	12	24	•22	4	479	399 •247
-11	23	-33				-13					·	10	46	-48	-	- • •	
													149	-137			

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Table 6.3.4.

Bond lengths $(\overset{O}{\mathbb{A}})$ with standard deviations in parentheses.

N(1) - O(1)	1.231(8)	N(3) - O(2)	1.185(11)
C(1) - N(1)	1.432(9)	C(11) - N(3)	1.463(9)
C(1) - C(2)	1.399(7)	C(11) - C(12)	1.369(7)
C(2) - C(3)	1.378(7)	C(12) - C(13)	1.367(7)
C(3) - C(4)	1.391(6)	C(13) - C(14)	1.420(6)
C(4) - C(5)	1.429(5)	C(14) - C(15)	1.411(6)
C(5) - C(6)	1.376(6)	C(15) - C(16)	1.375(6)
C(6) - C(1)	1.371(7)	C(16) - C(11)	1.398(7)
C(4) - N(2)	1.351(5)	C(14) - N(4)	1.346(5)
N(2) - C(7)	1.462(6)	N(4) - C(17)	1.462(6)
C(7) - C(8)	1.522(8)	C(17) - C(18)	1,503(8)
N(2) - C(9)	1.472(5)	N(4) - C(19)	1.465(6)
C(9) - C(10)	1.506(7)	C(19) - C(20)	1.499(7)
H(1) - C(2)	0.86(5)	H(15) - C(12)	1.01(6)
H(2) - C(3)	1.03(6)	H(16) - C(13)	0,99(6)
H(3) - C(5)	0.79(6)	H(17) - C(15)	0,98(6)
H(4) - C(6)	0.97(5)	H(18) - C(16)	0.93(6)
H(5) - C(7)	1.01(6)	H(19) - C(17)	0.88(6)
H(6) - C(7)	1.04(6)	H(20) - C(17)	1.03(6)
H(7) - C(8)	0.84(7)	H(21) - C(18)	0.99(7)

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Table 6.3.4. (cont'd)

H(8)	- C(8)	1.00(7)	H(22) - C(18)	0.94(7)
H(9)	- C(8)	1.00(7)	H(23) - C(18)	1.05(7)
H(10)	- C(9)	0.93(6)	H(24) - C(19)	0.92(6)
H(11)	- C(9)	0.96(6)	H(25) - C(19)	0.98(6)
H(12)	- C(10)	1.08(7)	H(26) - C(20)	0.92(7)
H(13)	- C(10)	1.05(6)	H(27) - C(20)	1.14(7)
H(14)	- C(10)	0.85(7)	H(18) - C(20)	0.97(7)

1.1

Table 6.3.5.

Bond angles (degrees) with standard deviations in parentheses.

C(1)-N(1)-O(1)	111.3(0.6)	C(11)-N(3) -O(2)	109.9(0.8)
C(2)-C(1)-N(1)	113.1(0.4)	C(12)-C(11)-N(3)	113.3(0.5)
C(6)-C(1)-N(1)	127.6(0.5)	C(16)-C(11)-N(3)	127.2(0.5)
C(6)-C(1)-C(2)	119.4(0.4)	C(16)-C(11)-C(12)	119.5(0.4)
C(1)-C(2)-C(3)	119.5(0.4)	C(11)-C(12)-C(13)	121.5(0.5)
C(2)-C(3)-C(4)	122.0(0.4)	C(12)-C(13)-C(14)	120.6(0.4)
C(3)-C(4)-C(5)	117.7(0.4)	C(13)-C(14)-C(15)	117.4(0.4)
C(4)-C(5)-C(6)	119.3(0.4)	C(14)-C(15)-C(16)	120.7(0.4)
C(5)-C(6)-C(1)	122.1(0.4)	C915)-C(16)-C(11)	120.4(0.4)
C(3)-C(4)-N(2)	122.2(0.4)	C(13)-C(14)-N(4)	120.1(0.4)
C(5)-C(4)-N(2)	120.2(0.4)	C(15)-C(14)-N(4)	121.8(0.4)
C(4)-N(2)-C(7)	122.6(0.4)	C(14)-N(4) -C(17)	121.7(0.4)
C(4)-N(2)-C(9)	121.7(0.4)	C(14)-N(4) -C(19)	122.5(0.3)
N(2)-C(7)-C(8)	112.7(0.4)	N(4) -C(17)-C(18)	113.0(0.4)
N(2)-C(9)-C(10)	112.5(0.4)	N(4) -C(19)-C(20)	112.8(0.4)
C(7)-N(2)-C(9)	115.7(0.4)	C(17)-N(4) -C(19)	115.8(0.4)
C(1)-C(2)-H(1)	108(4)	C(11)-C(12)-H(15)	115(3)
C(3)-C(2)-H(1)	133(4)	C(13)-C(12)-H(15)	123(3)
C(2)-C(3)-H(2)	112(3)	C(12)-C(13)-H(16)	120(3)
C(4)-C(3)-H(2)	126(3)	C(14)-C(13)-H(16)	119(3)
C(4)-C(5)-H(3)	116(4)	C(14)-C(15)-H(17)	119(3)
С(6)-С(5)-Н(3)	124(4)	C(16)-C(15)-H(17)	120(3)

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Table 6.3.5. (cont'd)

C(5) -C(6) -H(4)	113(3)	C(15)-C(16)-H(18)	116(3)
C(1) -C(6) -H(4)	125(3)	C(11)-C(16)-H(18)	123(3)
N(2) -C(7) -H(5)	113(3)	N(4) -C(17)-H(19)	108(4)
C(8) -C(7) -H(5)	111(4)	C(18)-C(17)-H(19)	97(4)
N(2) -C(7) -H(6)	114(3)	N(4) -C(17)-H(20)	108(3)
C(8) -C(7) -H(6)	104(3)	C(18)-C(17)-H(20)	11 6(3)
H(5) -C(7) -H(6)	101(5)	H(19)-C(17)-H(20)	114(5)
C(7) -C(8) -H(7)	107(5)	C(17)-C(18)-H(21)	119(4)
C(7) -C(8) -H(8)	107(4)	C(17)-C(18)-H(22)	1 09(4)
C(7) -C(8) -H(9)	110(4)	C(17)-C(18)-H(23)	116(4)
H(7) -C(8) -H(8)	1 28(6)	H(21)-C(18)-H(22)	100(6)
H(7) -C(8) -H(9)	105(6)	H(21)-C(18)-H(23)	11 0(5)
H(8) -C(8) -H(9)	96(5)	H(22)-C(18)-H(23)	· 1 00(6)
N(2) -C(9) -H(10)	109(4)	N(4) -C(19)-H(24)	1 09(4)
C(10)-C(9) -H(10)	115(4)	C(20)-C(19)-H(24)	110(4)
N(2) -C(9) -H(11)	105(4)	N(4) -C(19)-H(25)	109(4)
C(10)-C(9) -H(11)	115(4)	C(20)-C(19)-H(25)	112(3)
H(10)-C(9) -H(11)	106(5)	Н(24)-С(19)-Н(25)	1 02(5)
C(9) -C(10)-H(12)	109(4)	C(19)-C(20)-H(26)	121(4)
C(9) -C(10)-H(13)	106(4)	C(19)-C(20)-H(27)	108(3)
C(9) -C(10)-H(14)	116(5)	C(19)-C(20)-H(28)	1 02(4)
H(12)-C(10)-H(13)	104(5)	H(26)-C(20)-H(27)	98(5)
H(12)-C(10)-H(14)	107(6)	H(26)-C(20)-H(28)	110(6)
H(13)-C(10)-H(14)	114(6)	H(27)-C(20)-H(2')	118(5)

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Table 6.3.6.
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Torsion angles * (degrees) in the diethylamino groups.

Atom A	Atom B	Atom C	Atom D	Angle
C(4)	N(2)	C(7)	C(8)	85.4
C(4)	N(2)	C(9)	C(10)	89.7
C(14)	N(4)	C(17)	C(18)	87 .1
C(14)	N(4)	C(19)	C(20)	86.0

*The angle A-B-C-D is defined as positive if when viewed along the B-C bond atom A has to be rotated in a clockwise direction to eclipse atom D.

Table 6.3.7.

Closest intermolecular contacts $(\stackrel{o}{A})$ with standard deviations in parenthesis. Only C · · · C contacts less than 3.8 $\stackrel{o}{A}$ and C · · · 0 contacts less than 3.6 $\stackrel{o}{A}$ have been included.

Equivalent positions other than x, y, z required to describe these intermolecular contacts are :

- 1. -x, -y, -z
- 2. 1-x, 1-y, 1-z
- 3. $\frac{1}{2}+x$, $\frac{1}{2}-y$, $\frac{1}{2}+z$
- 4. $-\frac{1}{2}+x$, $\frac{1}{2}-y$, $\frac{1}{2}+z$

Atom 1	Atom 2	Distance
0(1)	c(7) ⁴	3. 569(8)
0(1)	C(8) ²	3.432(9)
0(1)	C(18) ³	3.556(8)
0(2)	c(8) ⁶	3.560(10)
0(2)	c(17) ⁵	3.557(9)
0(2)	c(19) ⁵	3,594(9)

5.	$\frac{1}{2}+x$, $\frac{1}{2}-y$, $-\frac{1}{2}+z$
6.	$-\frac{1}{2}+x$, $\frac{1}{2}-y$, $-\frac{1}{2}+z$
7.	$\frac{3}{2}$ -x, $\frac{3}{2}$ +y, $\frac{3}{2}$ -z
8.	$\frac{3}{2} - x$, $\frac{1}{2} + y$, $\frac{3}{2} - z$

Atom 1	Atom 2	Distance
C(1)	c(15) ⁷	3.774(6)
C(3)	C(20) ⁷	3.607(7)
C(4)	C(18) ⁸	3.677(6)
C(4)	c(19) ⁷	3.710(7)
C(5)	C(15) ¹	3.751(6)
C(6)	C(14) ¹	3.763(6)
C(12)	c(20) ⁷	3.740(7)

Table 6.3.8.

Mean planes, referred to orthogonal co-ordinates X', Y and Z' (where X' = $axsin\beta$, Y = by, Z' = $ax + czcos\beta$), displacements of the atoms from the planes (Å) and angles between the planes (degrees).

Plane 1 : -0.0987X' + 0.9856Y - 0.1373Z' = 1.6830 A

Atoms in plane

C(1)			-0 .0080		
C(2)			0.0054		
C(3)			-0.0021		
C(4)			0.0013		
C(5)			-0.0039		
C(6)			0.0074	r.m.s. distance from	
					plane = 0.005 Å	
Plane 2 : -0.0281X	' +	0.9972Y	-	0.06942'	o = 2.4909 A	
N(2)			0,0018		
c(4)			-0.0003		
C(7)			-0,0008		

 $C(9) \qquad -0.0008 \quad r.m.s. \text{ distance from} \\ plane = 0.001 \text{ A}$

		Table	6.3.8. (co	nt'd)		
Plane 3 :	-0.6523X -	0.1277Y -	- 0.7471Z'	-3. 01	о 48 А	
	C(11)		0.0084			
	C(12)		-0.0128			
	C(13)		0.0099			
	C(14)		-0.0030			
	C(15)		-0.0011			
	C(16)		-0.0015	r.m.s.	distance	from
				plane	= 0.008	o A
Plane 4 :	-0.6525X' -	0,0960Y	- 0.75132'	≈ -2. 9]	0 334 A	
	N(4)		-0.0121			
	C(14)		0,0025			
	C(17)		0.0049			
	C(19)		0.0047	r.m.s.	distance	from
				plane	- 0. 007	o A
Plane 5 :	-0.0911X' +	0•9864Y	- 0.1367 Z'	≖ 1 .72	0 223 A	
	Atoms in plan	e : C(1),	N(1), O(1)			
Plane 6 :	-0.6519X' -	0.0352Y	- 0.75752'	= -2.73	о 345 Л	
	Atoms in plan	e: C(9),	N(3), O(2).	•		

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Table 6.3.8. (cont'd)

Interplanar angles

Angle	1 2	N.	6.0°
Angle	3^4	æ	2.4°
Angle	1 ⁵	*	0.4 ⁰
Angle	3 ~ 6	21	5.3°
Angle	1^3		87.6 ⁰



Figure 6.3.1 : The two molecules of N, N-diethyl p-nitroscaniline in the asymmetric unit, showing the atomic numbering system employed.



Figure 6.3.2 : The molecular packing of N, N-diethyl p-nitrosoaniline projected along the <u>b</u> axis, from $y = \frac{1}{2}$ to $y = -\frac{1}{2}$. The hydrogen atoms have been omitted for clarity.



